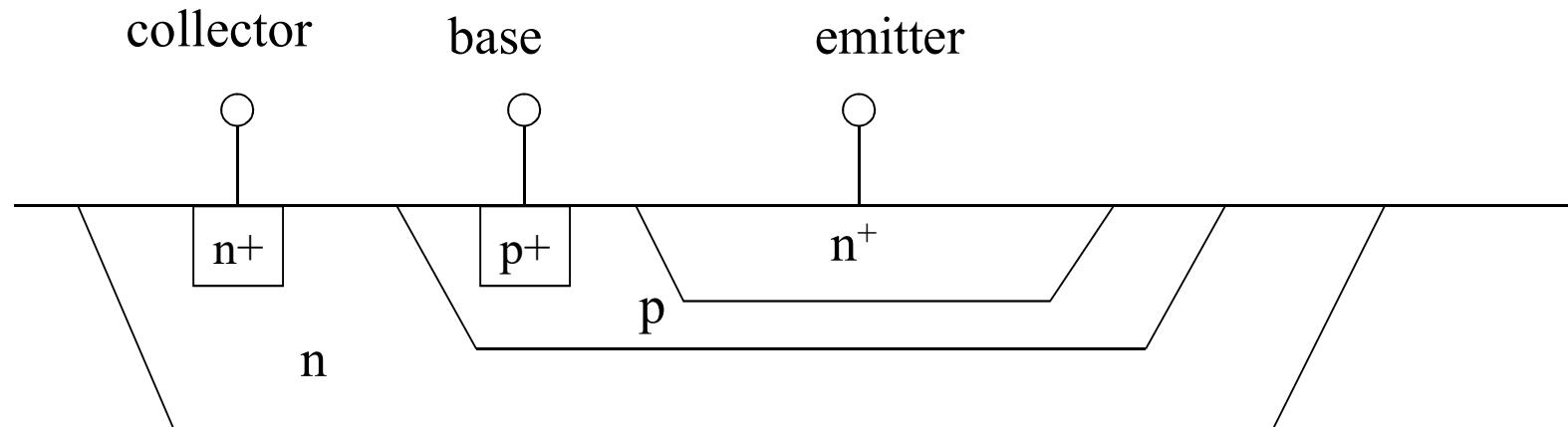


Bipolar transistors

bipolar transistors

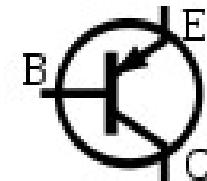
npn transistor



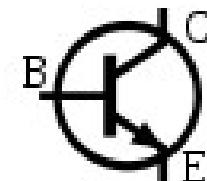
lightly doped p substrate

Used in front-end high-frequency receivers (mobile telephones), low input impedance amplifiers, power devices.

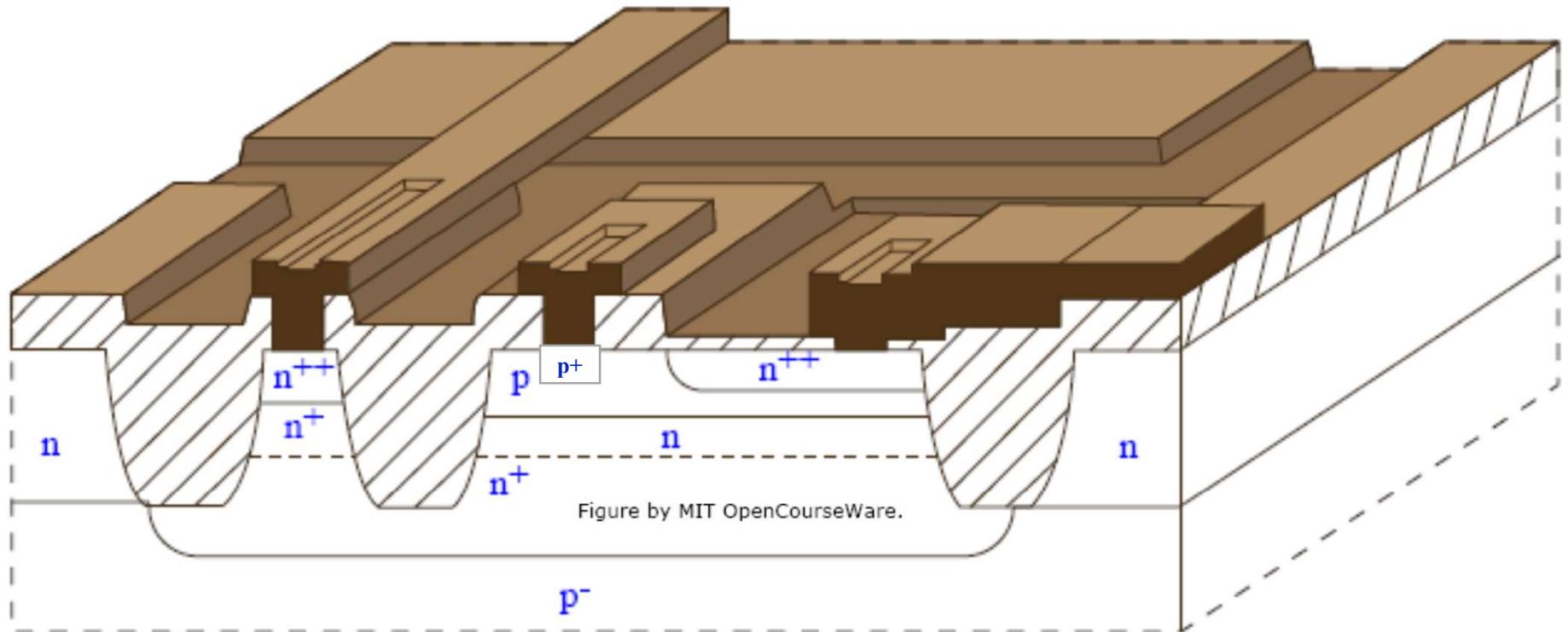
bipolar transistors



PNP

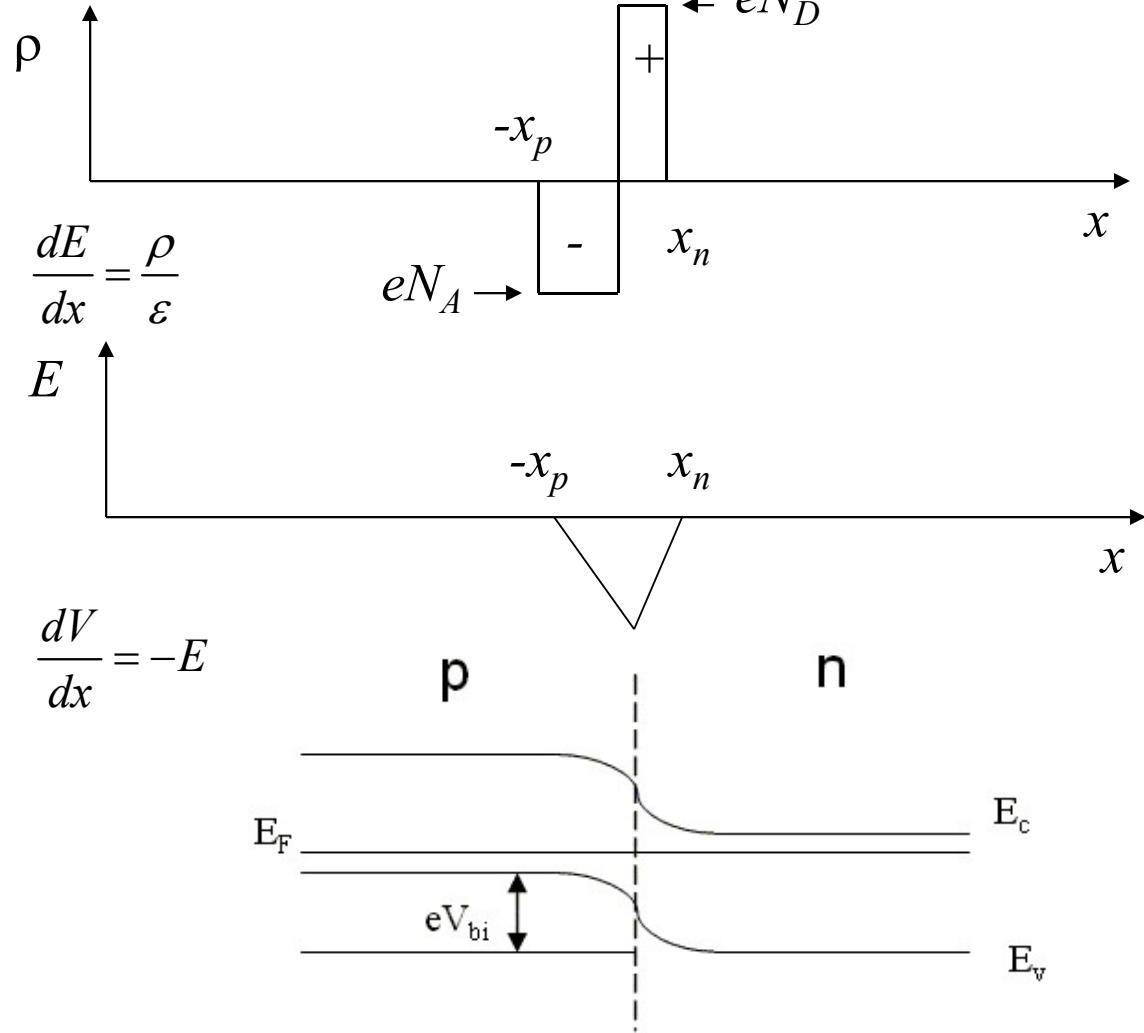


NPN



Oxide isolated integrated BJT - a modern process

abrupt junction



$$eV_{bi} = k_B T \ln \left(\frac{N_D N_A}{n_i^2} \right)$$

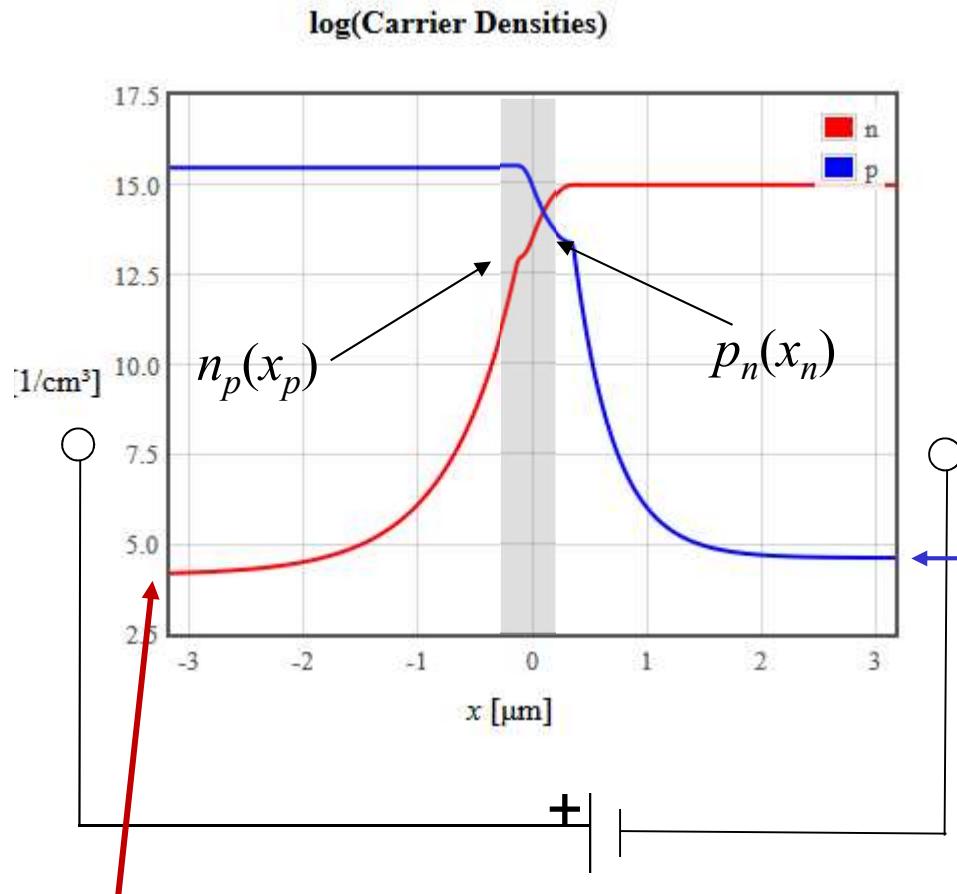
$$E = -\frac{eN_A}{\varepsilon}(x + x_p) \quad -x_p > x > 0$$

$$E = \frac{eN_D}{\varepsilon}(x - x_n) \quad 0 > x > x_n$$

$$V = \frac{eN_A}{\varepsilon} \left(\frac{x^2}{2} + xx_p \right) \quad -x_p > x > 0$$

$$V = \frac{-eN_D}{\varepsilon} \left(\frac{x^2}{2} - xx_n \right) \quad 0 > x > x_n$$

Forward bias, $V > 0$



$$n_{p0} = \frac{n_i^2}{N_A}$$

Minority electrons are injected into the p-region
Minority holes are injected into the n-region

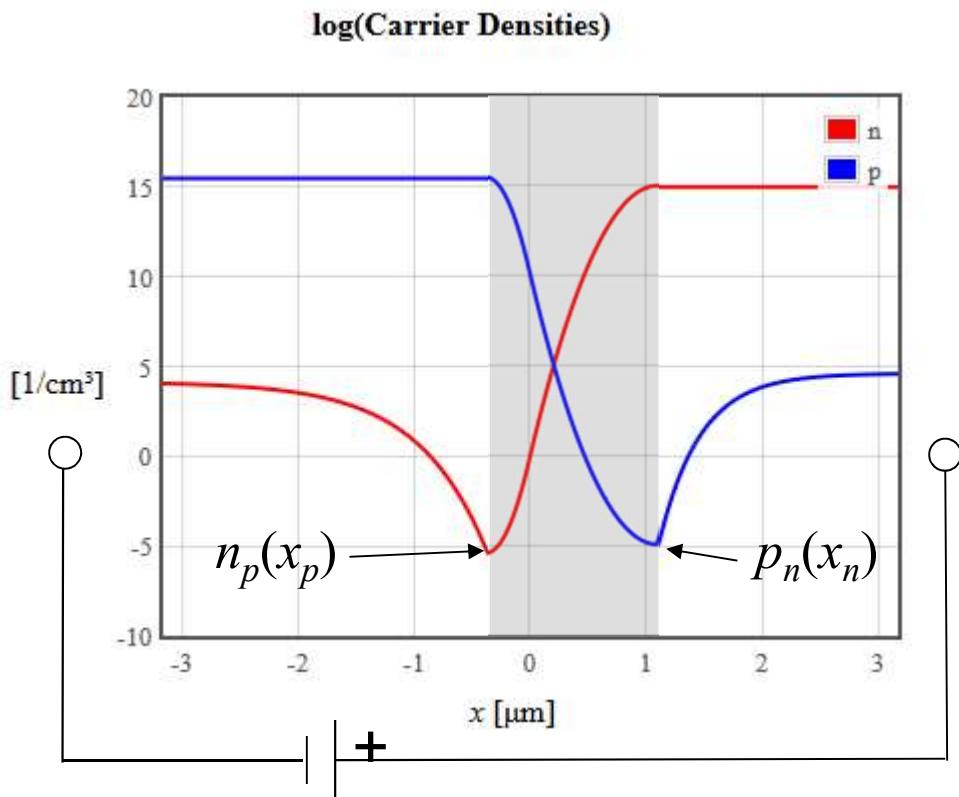
Electrons and holes are driven towards the junction.
The depletion region becomes narrower

$$n_p(x_p) = n_{p0} \exp\left(\frac{eV}{k_B T}\right)$$

$$p_{n0} = \frac{n_i^2}{N_D}$$

$$p_n(x_n) = p_{n0} \exp\left(\frac{eV}{k_B T}\right)$$

Reverse bias, $V < 0$



Electrons and holes are driven away from the junction.
The depletion region becomes wider

$$n_p(x_p) = n_{p0} \exp\left(\frac{eV}{k_B T}\right)$$

$$p_n(x_n) = p_{n0} \exp\left(\frac{eV}{k_B T}\right)$$

Minority electrons are extracted from the p-region by the electric field
Minority holes are extracted from the n-region by the electric field

Long/Short diodes

$N_A =$ <input type="text" value="1E15"/> 1/cm ³	$N_D =$ <input type="text" value="1E15"/> 1/cm ³	$E_g =$ <input type="text" value="1.166-4.73E-4*T*T/(T+636)"/> eV	$d_p =$ <input type="text" value="-2"/> μm
$N_v(300) =$ <input type="text" value="9.84E18"/> 1/cm ³	$N_c(300) =$ <input type="text" value="2.78E19"/> 1/cm ³	$\epsilon_r =$ <input type="text" value="12"/>	$T =$ <input type="text" value="300"/> K
$\mu_p =$ <input type="text" value="480"/> cm ² /V s	$\mu_n =$ <input type="text" value="1350"/> cm ² /V s	$\tau_p =$ <input type="text" value="1E-7"/> s	$\tau_n =$ <input type="text" value="1E-7"/> s
<input type="text" value="0.2"/> V Submit			

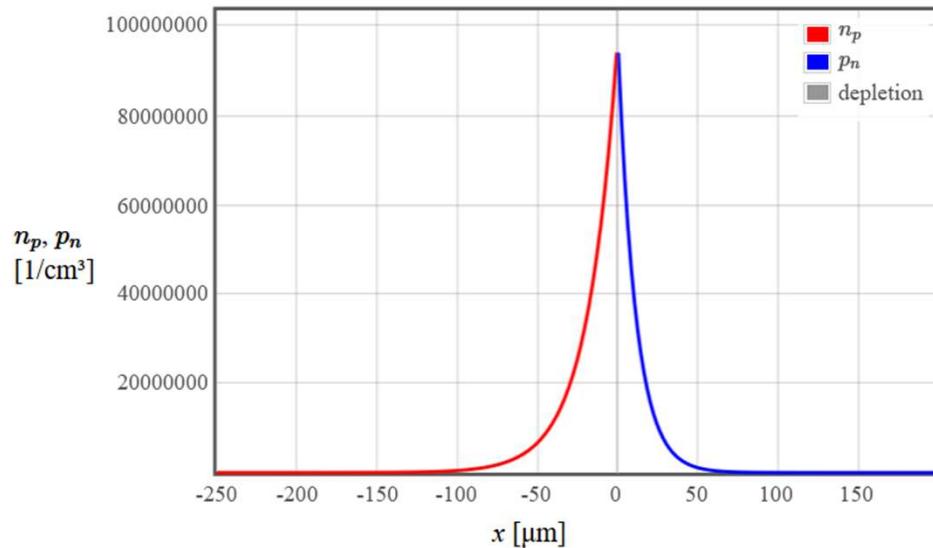
$$E_g = 1.12 \text{ eV} \quad W = |x_n| + |x_p| = 1.05 \text{ } \mu\text{m} \quad x_p = -0.527 \text{ } \mu\text{m} \quad x_n = 0.527 \text{ } \mu\text{m} \quad V_{bi} = 0.618 \text{ V} \quad n_i = 6.41e+9 \text{ cm}^{-3}$$

$$D_p = 12.4 \text{ cm}^2/\text{s} \quad D_n = 34.9 \text{ cm}^2/\text{s} \quad L_p = 11.1 \text{ } \mu\text{m} \quad L_n = 18.7 \text{ } \mu\text{m} \quad n_{p0} = 4.10e+4 \text{ cm}^{-3} \quad p_{n0} = 4.10e+4 \text{ cm}^{-3}$$

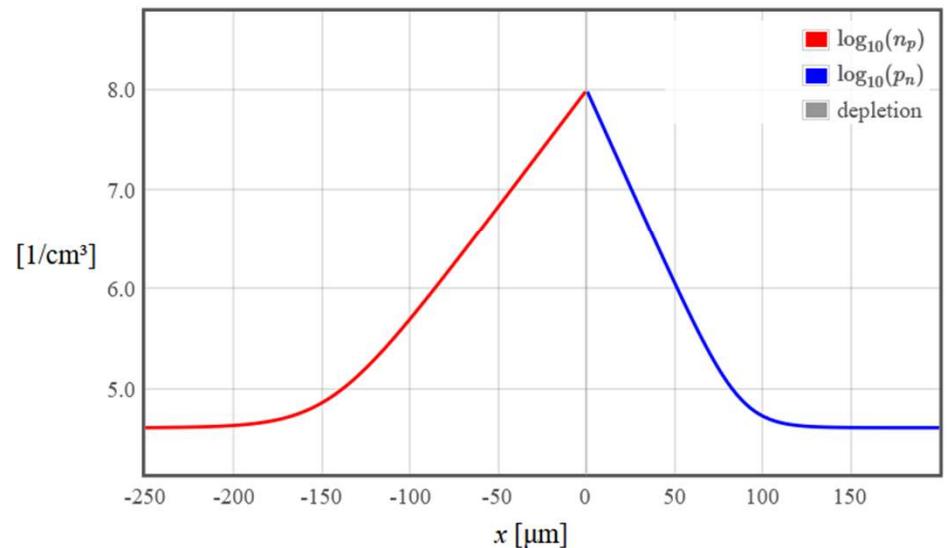
$$A_n = -5.35e+8 \text{ cm}^{-3} \quad B_n = 6.62e+8 \text{ cm}^{-3} \quad A_p = 4.24e+8 \text{ cm}^{-3} \quad B_p = -2.96e+8 \text{ cm}^{-3}$$

$$j_n = 0.00000357 \text{ A cm}^{-2} \quad j_p = 0.00000128 \text{ A cm}^{-2} \quad j_{\text{diff}} = 0.00000485 \text{ A cm}^{-2}$$

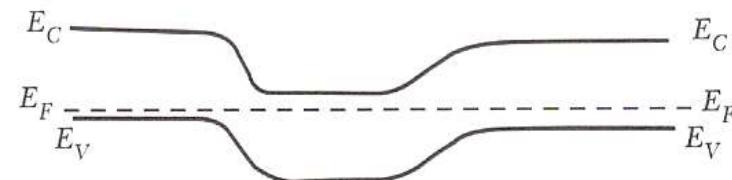
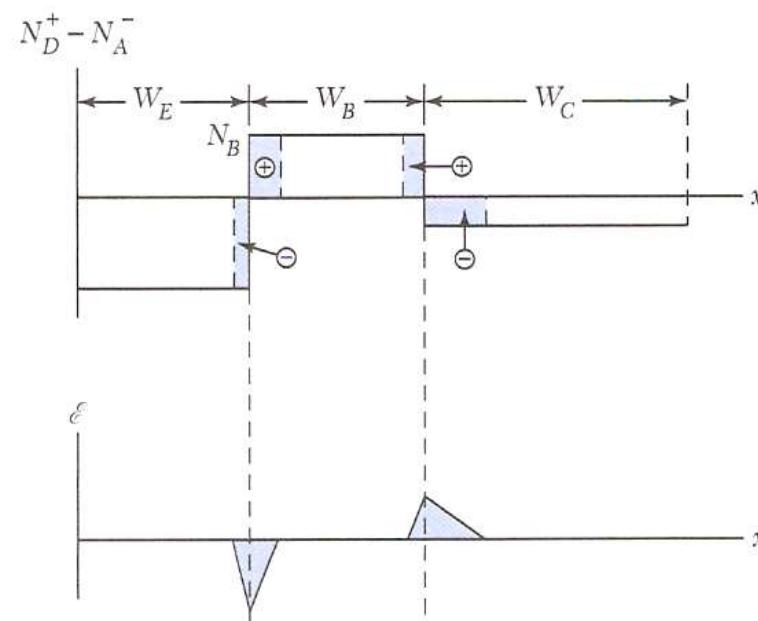
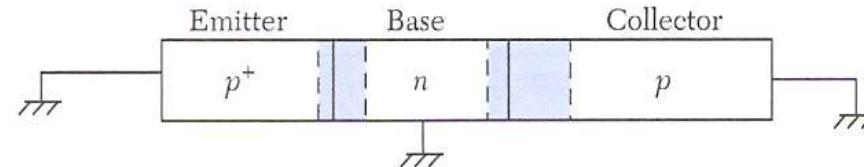
Minority Carrier Densities



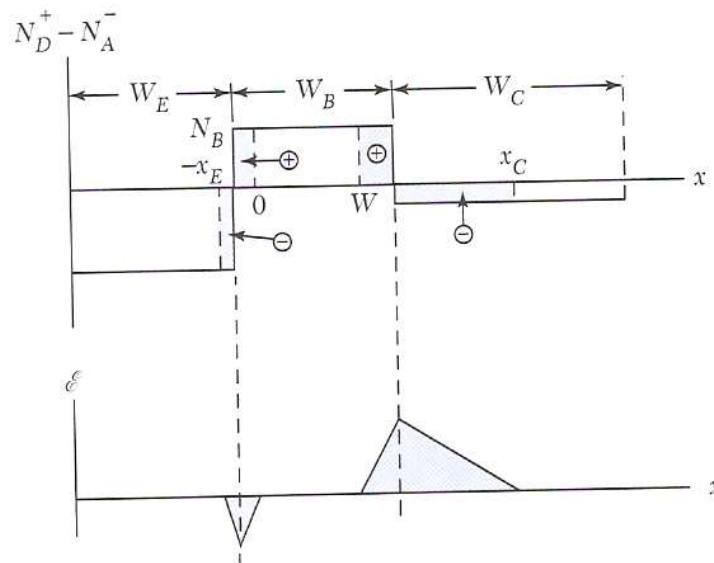
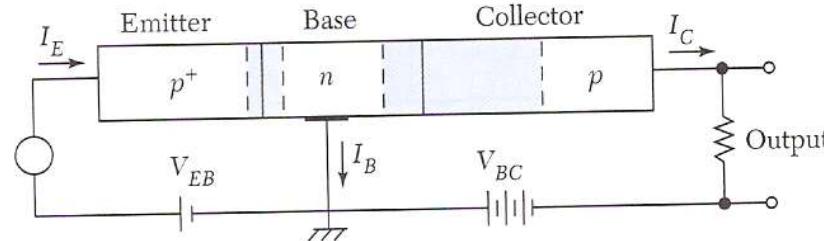
$\log_{10}(\text{Minority Carrier Densities})$



pnp transistor, no bias

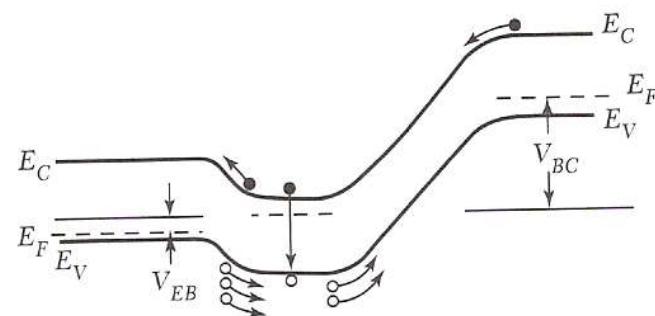


pnp transistor, forward active bias

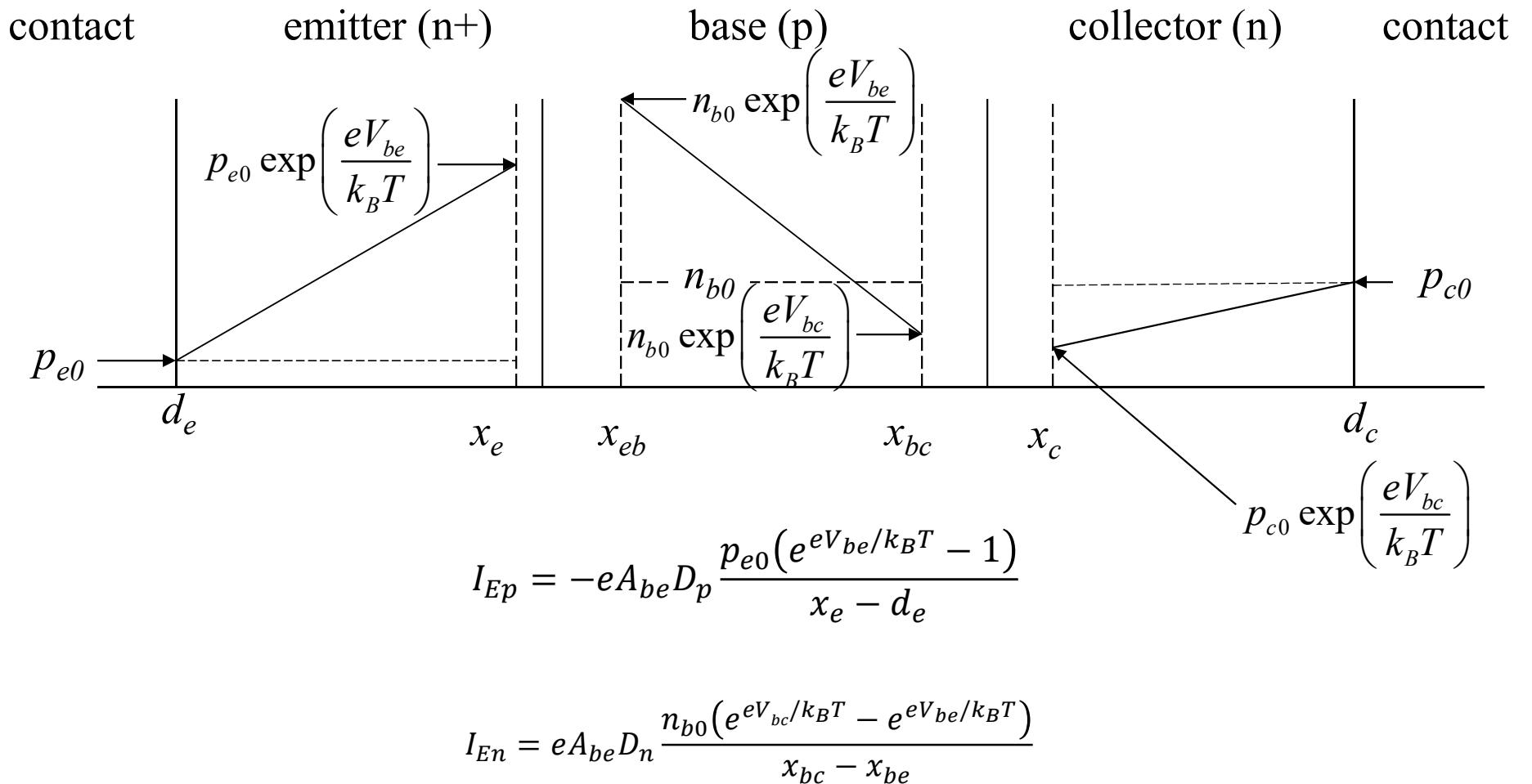


Always dissipate power due to the forward bias

The base-emitter voltage controls the minority carriers injected from the emitter to the base. These diffuse to the base-collector junction and are swept into the collector.



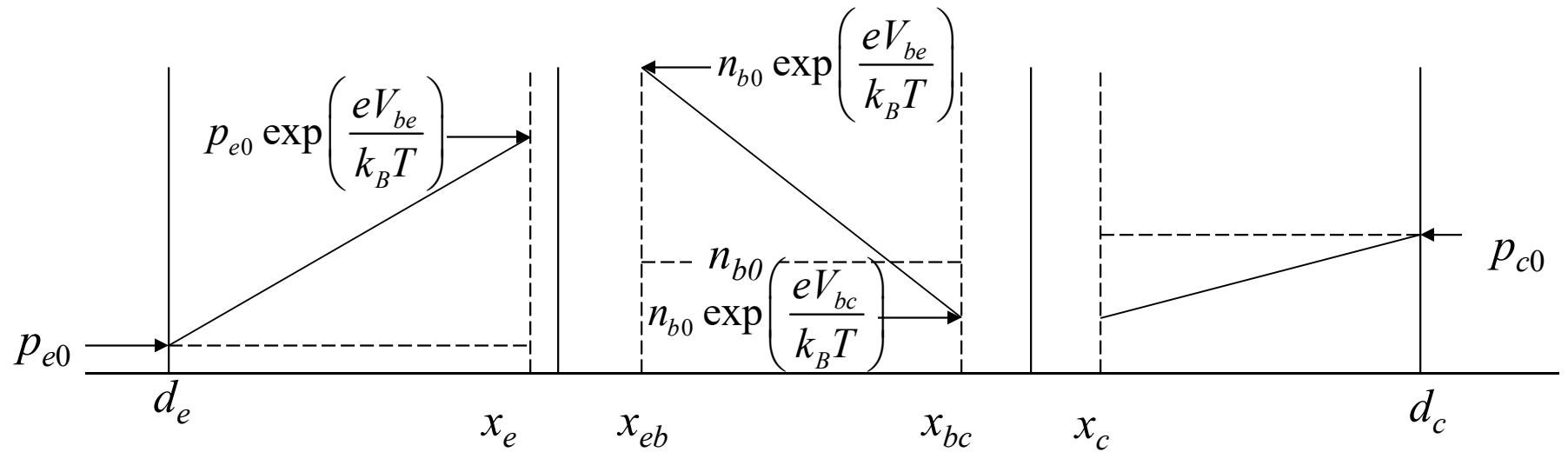
Minority carrier concentration



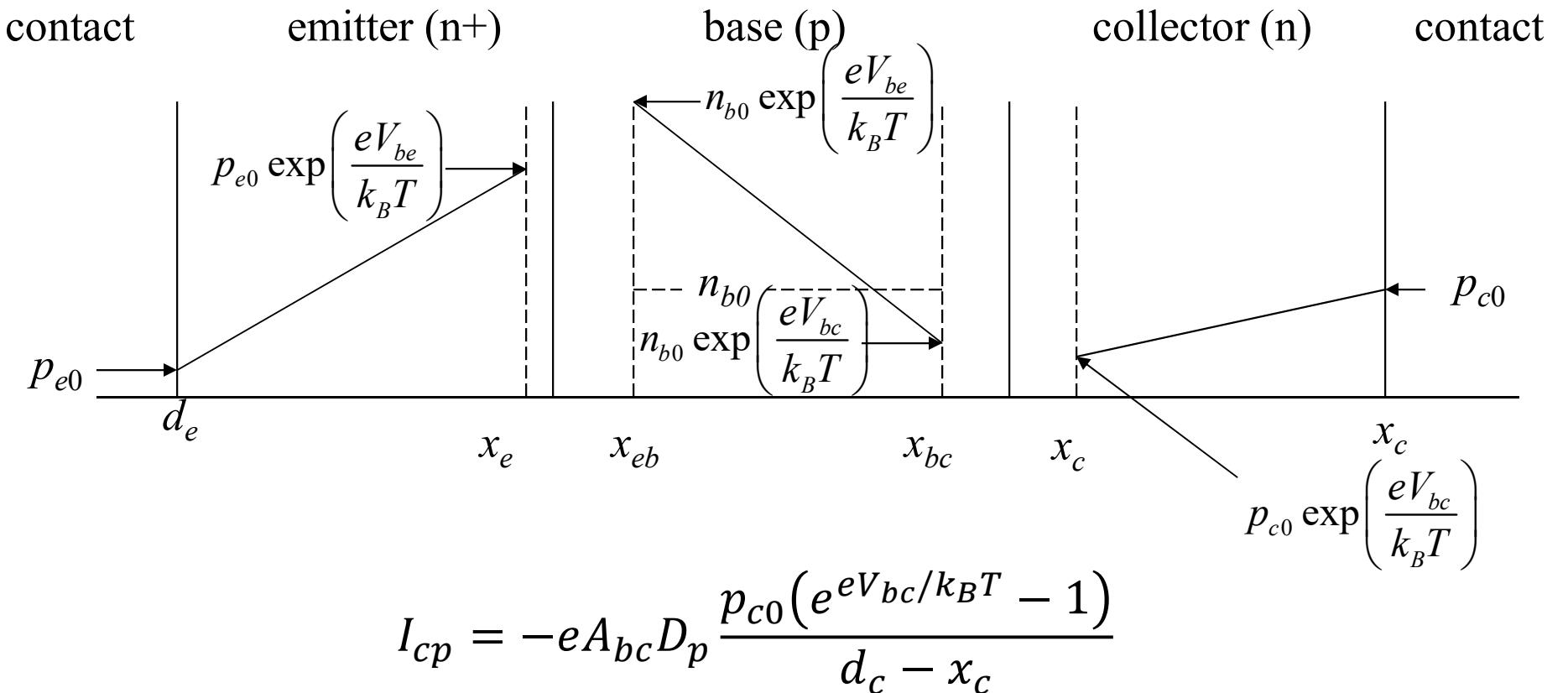
Emitter current

$$I_E = I_{En} + I_{Ep} = \left[\frac{eA_{be}D_p p_{e0}}{x_{eb} - d_e} + \frac{eA_{be}D_n n_{b0}}{x_{bc} - x_{be}} \right] \left(e^{eV_{be}/k_B T} - 1 \right) - \frac{eA_{be}D_n n_{b0}}{x_{bc} - x_{be}} \left(e^{eV_{bc}/k_B T} - 1 \right)$$

$$I_E = I_{ES} \left(e^{eV_{be}/k_B T} - 1 \right) - \alpha_R I_{CS} \left(e^{eV_{bc}/k_B T} - 1 \right)$$



Collector current

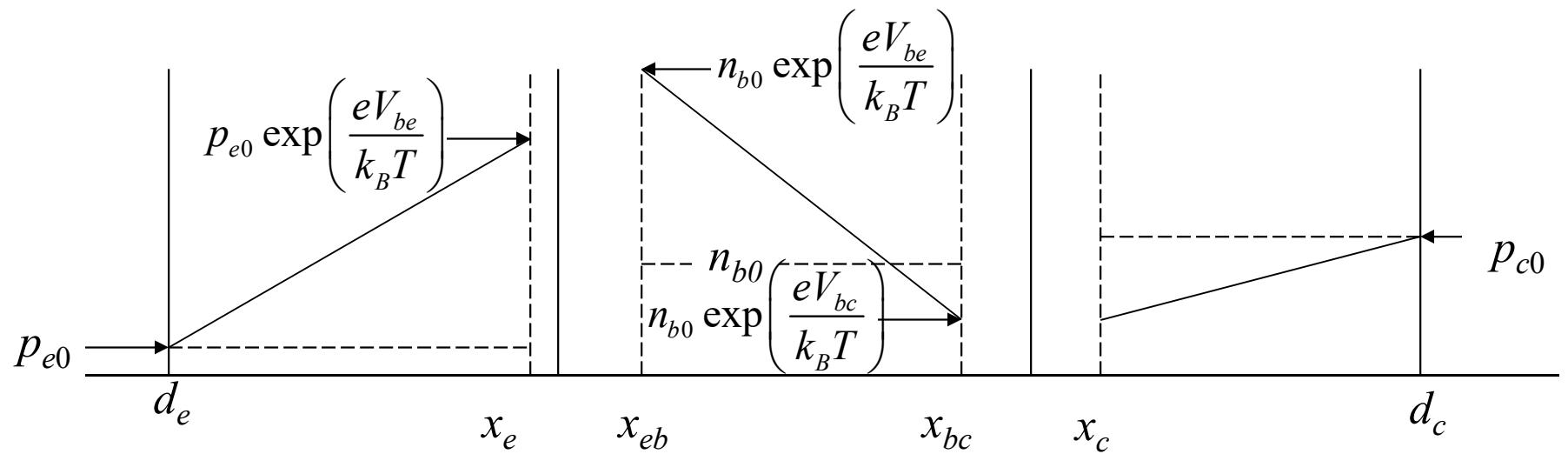


$$I_{cn} = -eA_{bc}D_n \frac{n_{b0}(e^{eV_{be}/k_B T} - e^{eV_{bc}/k_B T})}{x_{bc} - x_{eb}}$$

Collector current

$$I_c = I_{cp} + I_{cn} = \frac{eA_{bc}D_n n_{b0}}{x_{bc} - x_{be}} \left(e^{eV_{be}/k_B T} - 1 \right) - \left[\frac{eA_{bc}D_p p_{c0}}{d_c - x_c} + \frac{eA_{bc}D_n n_{b0}}{x_{bc} - x_{be}} \right] \left(e^{eV_{bc}/k_B T} - 1 \right)$$

$$I_c = I_{cp} + I_{cn} = \alpha_F I_{ES} \left(e^{eV_{be}/k_B T} - 1 \right) - I_{CS} \left(e^{eV_{bc}/k_B T} - 1 \right)$$

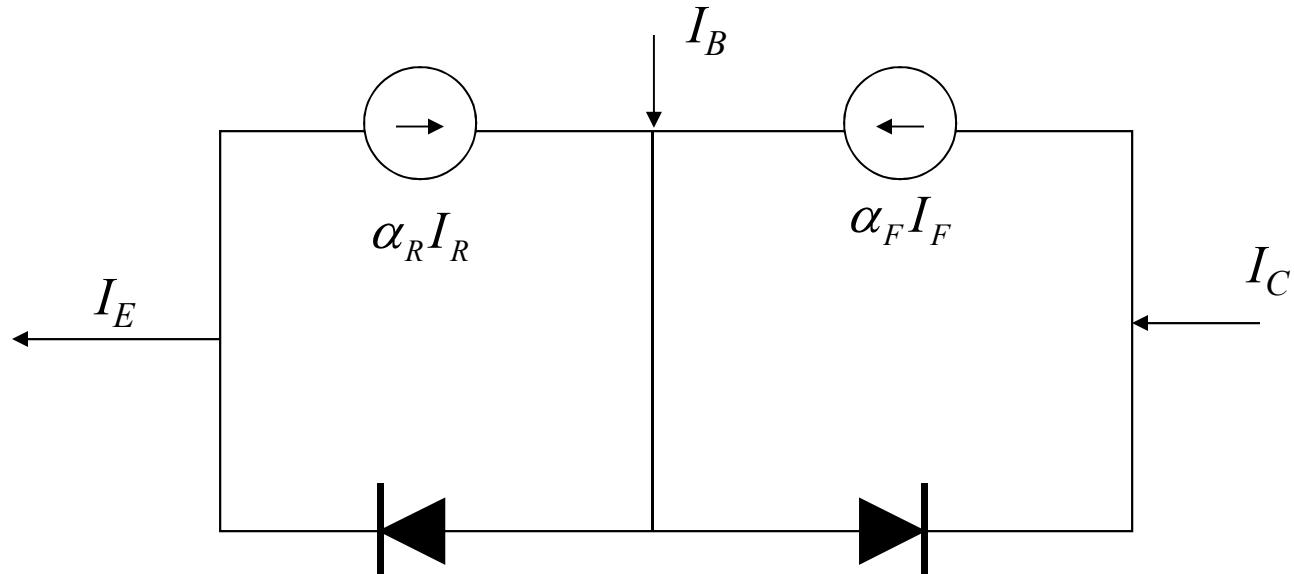


Ebers-Moll model

$$I_E = I_{ES} \left(e^{eV_{be}/k_B T} - 1 \right) - \alpha_R I_{CS} \left(e^{eV_{bc}/k_B T} - 1 \right)$$

$$I_C = \alpha_F I_{ES} \left(e^{eV_{be}/k_B T} - 1 \right) - I_{CS} \left(e^{eV_{bc}/k_B T} - 1 \right)$$

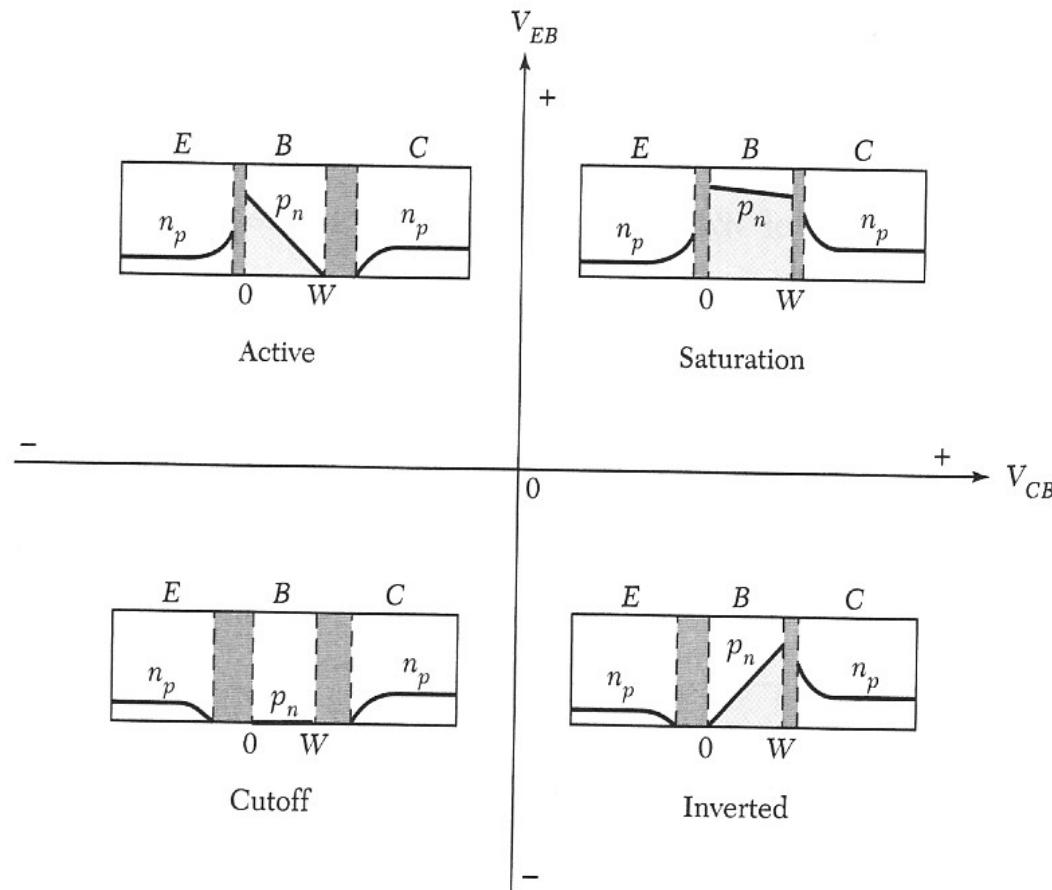
$$I_B = I_E - I_C$$



$$I_F = I_{ES} \left(e^{eV_{be}/k_B T} - 1 \right) \quad I_R = I_{CS} \left(e^{eV_{bc}/k_B T} - 1 \right)$$

Transistor modes

1. Forward active: emitter-base **forward**, base-collector **reverse**
2. Saturation: emitter-base **forward**, base-collector **forward**
3. Reverse active: emitter-base **reverse**, base-collector **forward**
4. Cut-off: emitter-base **reverse**, base-collector **reverse**

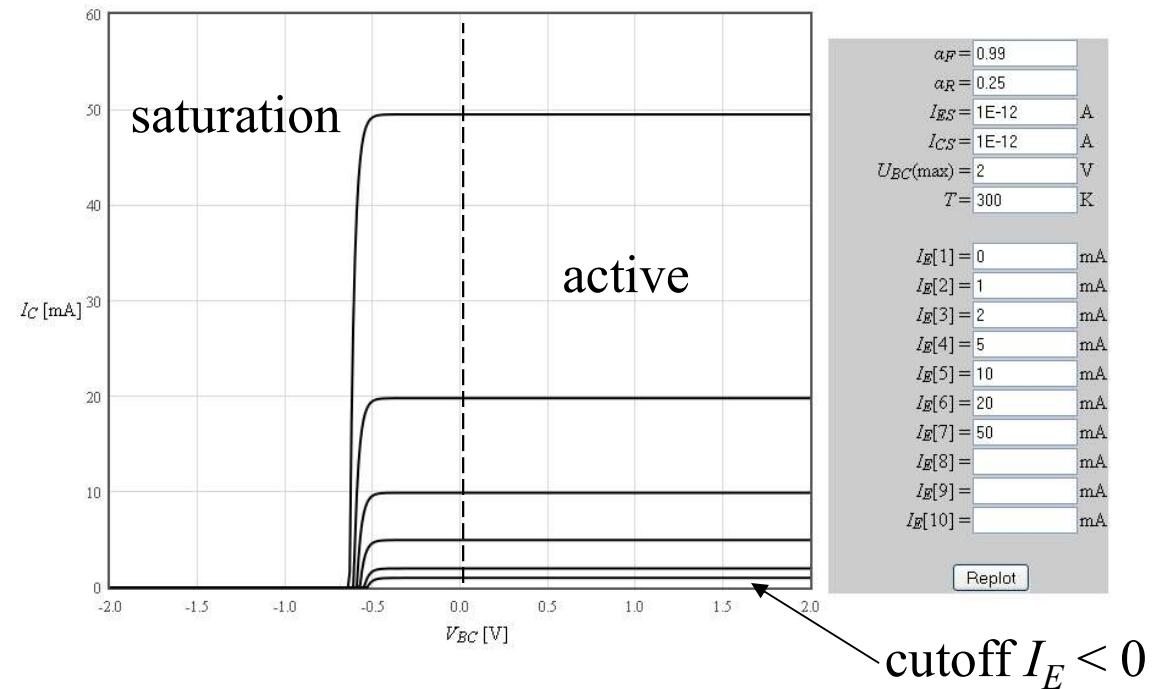
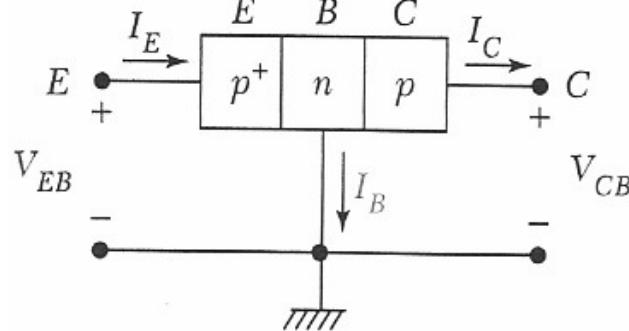


Common base configuration

$$I_E = I_{ES} \left(e^{eV_{be}/k_B T} - 1 \right) - \alpha_R I_{CS} \left(e^{eV_{bc}/k_B T} - 1 \right)$$

solve for V_{be}

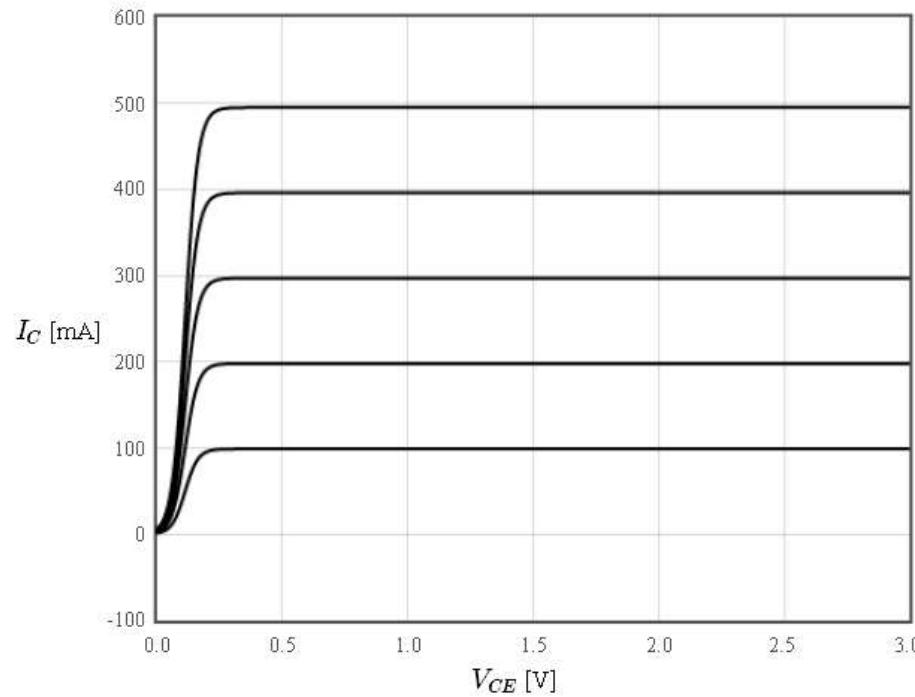
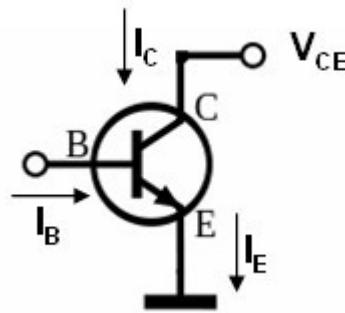
$$I_c = \alpha_F I_{ES} \left(e^{eV_{be}/k_B T} - 1 \right) - I_{CS} \left(e^{eV_{bc}/k_B T} - 1 \right)$$



Common emitter configuration

$$I_E = I_{ES} \left(e^{eV_{be}/k_B T} - 1 \right) - \alpha_R I_{CS} \left(e^{eV_{bc}/k_B T} - 1 \right) \quad I_B = I_E - I_C$$

$$I_c = \alpha_F I_{ES} \left(e^{eV_{be}/k_B T} - 1 \right) - I_{CS} \left(e^{eV_{bc}/k_B T} - 1 \right)$$



$\alpha_F =$	0.99
$\alpha_R =$	0.25
$I_{ES} =$	1E-12 A
$I_{CS} =$	1E-12 A
$V_{CE(max)} =$	3 V
$T =$	300 K
$I_B[1] =$	1 mA
$I_B[2] =$	2 mA
$I_B[3] =$	3 mA
$I_B[4] =$	4 mA
$I_B[5] =$	5 mA
$I_B[6] =$	mA
$I_B[7] =$	mA
$I_B[8] =$	mA
$I_B[9] =$	mA
$I_B[10] =$	mA

Replot

current amplification ~ 100

Emitter efficiency

$$\gamma_e = \frac{I_{En}}{I_{En} + I_{Ep}} = \frac{1}{1 + I_{Ep} / I_{En}} \quad \leftarrow \text{for npn}$$

$$I_{Ep} = eA_{be}D_p \frac{p_{e0}(e^{eV_{be}/k_B T} - 1)}{x_{eb} - d_e}$$

$$I_{En} = -eA_{be}D_n \frac{n_{b0}(e^{eV_{be}/k_B T} - e^{eV_{bc}/k_B T})}{x_{bc} - x_{be}}$$

For $\gamma_e \sim 1$, $x_{bc} - x_{be} \ll L_b$, $x_{eb} - d_e$ and $n_{b0} \gg p_{e0}$

neutral base width

$$\frac{n_i^2}{N_{Ab}} \quad \frac{n_i^2}{N_{De}}$$

Small base width and heavy emitter doping

Base transport factor

$$B = \frac{I_c}{I_{En}}$$

ratio of the injected current to the collected current

recombination in the base would reduce the base transport factor

A thin base with low doping results in a base transport factor ~ 1

Current transfer ratio

$$\alpha = \frac{I_C}{I_E} = B\gamma_e$$

$\alpha \sim 1$ for a good BJT

Current amplification factor

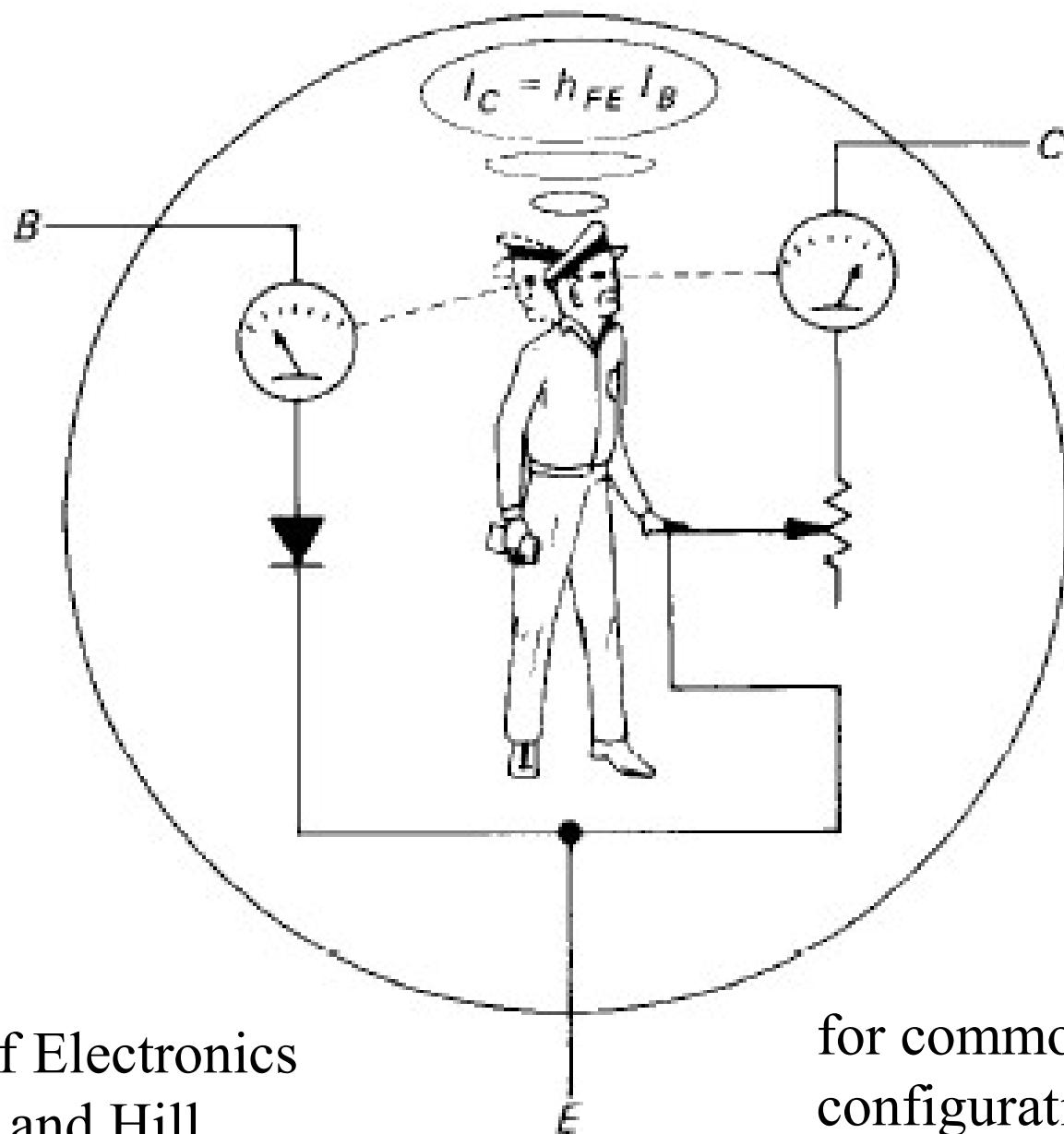
$$\beta = h_{fe} = \frac{I_C}{I_B}$$

$$I_B = I_E - I_C \quad I_C = \alpha I_E$$

$$I_B = \left(\frac{1}{\alpha} - 1 \right) I_C$$

$$\beta = \frac{I_C}{I_B} = \frac{\alpha}{1 - \alpha} = \frac{B\gamma_e}{1 - B\gamma_e}$$

$$\beta \sim 50 - 500$$



The Art of Electronics
Horowitz and Hill

for common emitter
configuration

"Transistor man"

Transconductance

$$g_m = \frac{\partial I_C}{\partial V_{be}}$$

$$I_c = \alpha_F I_{ES} \left(e^{eV_{be}/k_B T} - 1 \right) - I_{CS} \left(e^{eV_{bc}/k_B T} - 1 \right)$$

The first term depends on V_{be}

$$g_m = \frac{e\alpha_F I_{ES}}{k_B T} e^{eV_{be}/k_B T} \approx \frac{eI_C}{k_B T} = \frac{e\beta I_B}{k_B T}$$

The transconductance can be very high.

Early effect

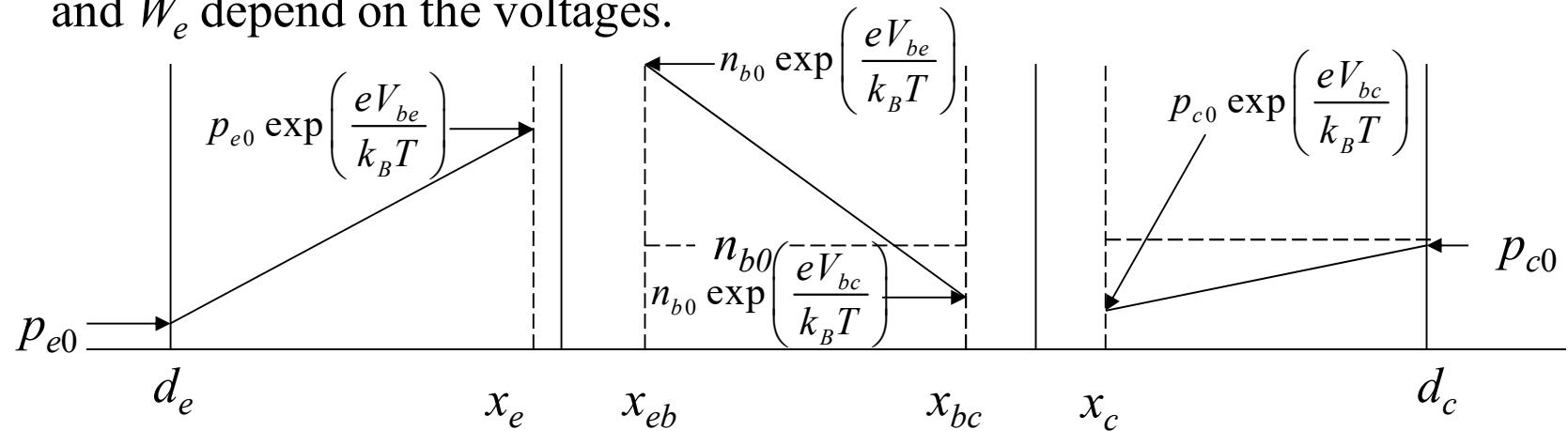
Ebers - Moll:

$$\begin{aligned}
 I_E &= I_{ES} \left(e^{eV_{be}/k_B T} - 1 \right) - \alpha_R I_{CS} \left(e^{eV_{bc}/k_B T} - 1 \right) \\
 I_c &= \alpha_F I_{ES} \left(e^{eV_{be}/k_B T} - 1 \right) - I_{CS} \left(e^{eV_{bc}/k_B T} - 1 \right) \\
 I_B &= I_E - I_C
 \end{aligned}$$

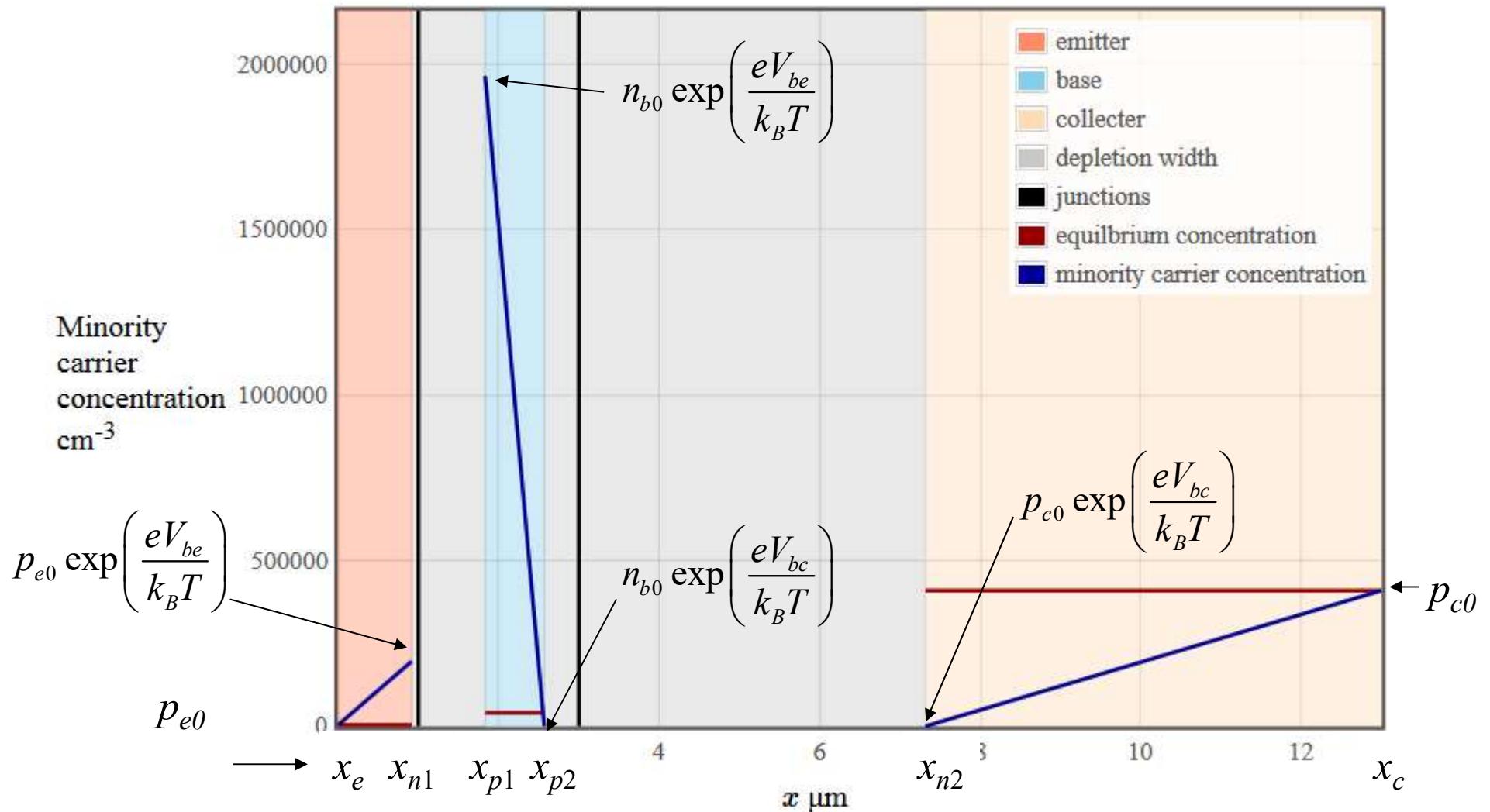
$$I_{ES} = \left[\frac{eA_{be}D_p p_{e0}}{x_{eb} - d_e} + \frac{eA_{be}D_n n_{b0}}{x_{bc} - d_{be}} \right]$$

$$I_{CS} = \left[\frac{eA_{bc}D_p p_{c0}}{d_c - x_c} + \frac{eA_{bc}D_n n_{b0}}{x_{bc} - x_{be}} \right]$$

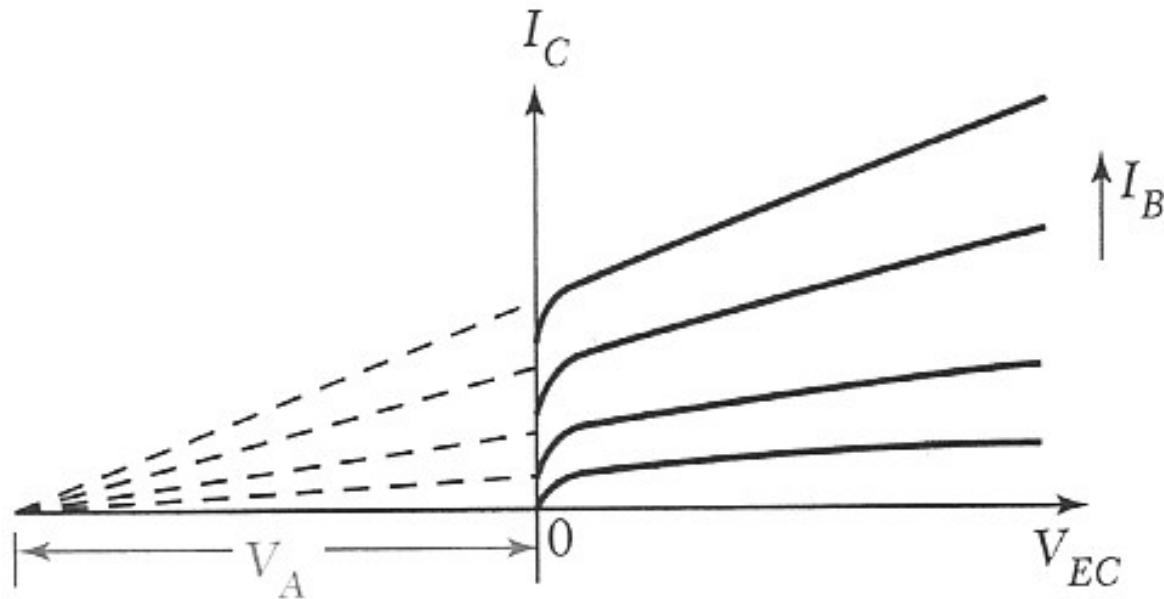
I_{ES} and I_{CS} are treated as constants but the depletion widths W_{bc} , W_{be} , W_c , and W_e depend on the voltages.



Minority carrier concentration



Early effect



Common emitter configuration

Base width modulation: smaller width increases the diffusion current and increases the gain.

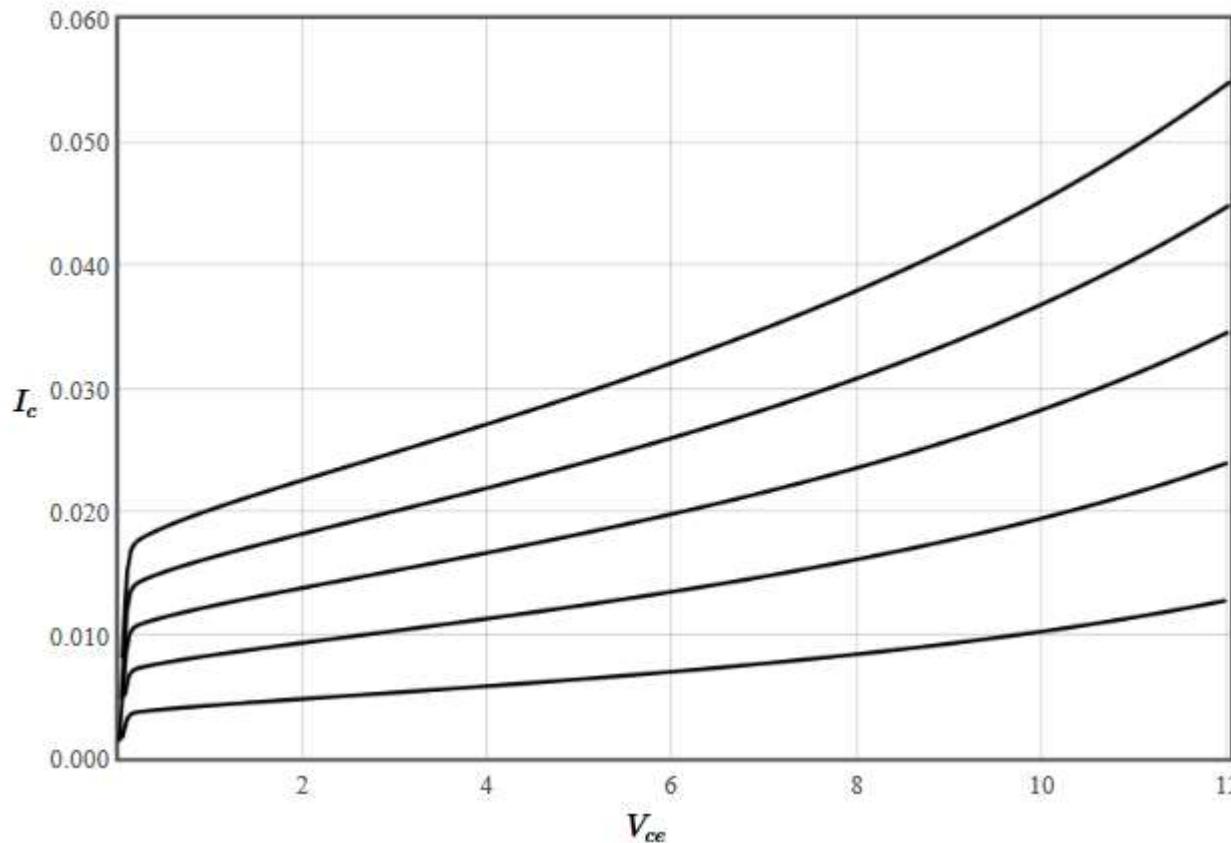
Punchthrough: The neutral base width goes to zero and all gain is lost.

Lightly dope the collector -> voltage drops in collector. Makes circuit slower.

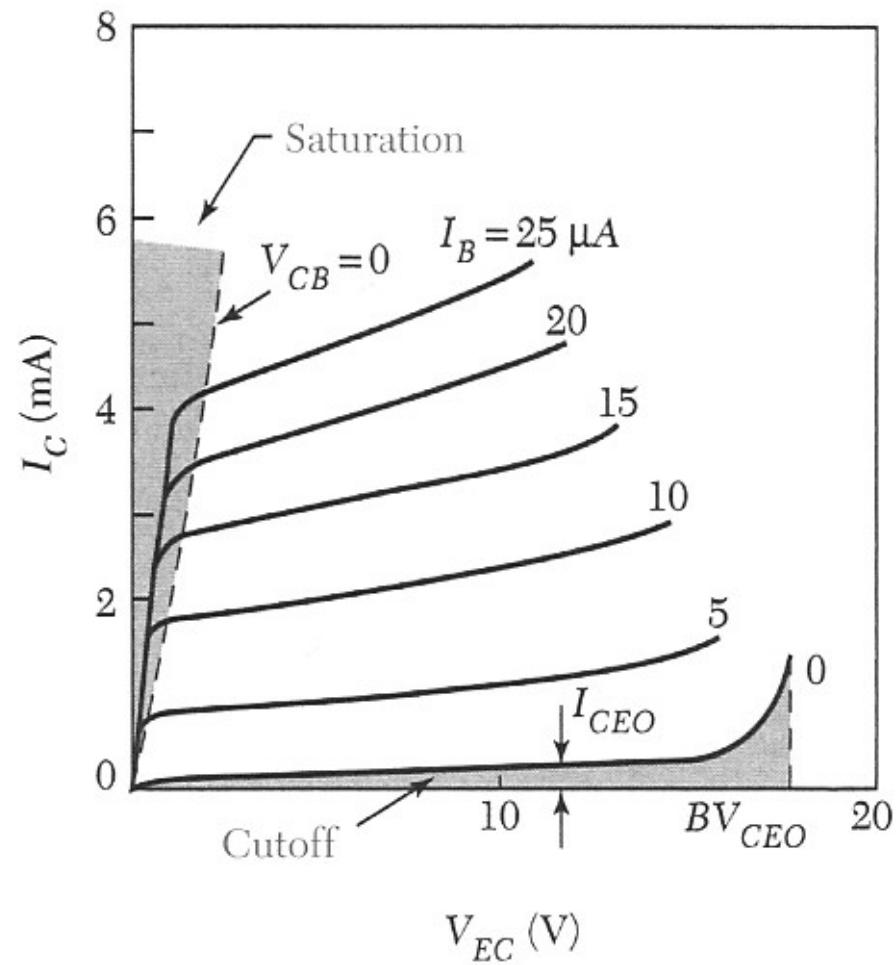
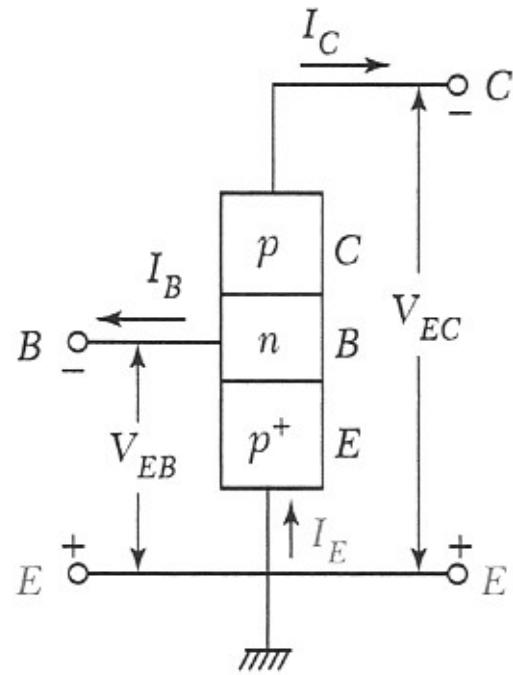
NPN common emitter configuration

n-Emitter		$A_{eb} = 1E-3 \text{ cm}^2$	
Minority $\mu_{pe} = 480$	cm^2/Vs	$N_c(300K) = 2.78\text{E}19$	cm^{-3}
$N_{de} = 1\text{E}16$	cm^{-3}	$N_e(300K) = 9.84\text{E}18$	cm^{-3}
$\tau_{pe} = 1E-5$	s	$E_g = 1.166 - 4.73E-4 * T^2 / (T + 636)$	eV
		$\epsilon_r = 11.9$	
p-Base		$I_b \text{ max} = 0.001 \text{ eV}$	
Minority $\mu_{nb} = 1350$	cm^2/Vs	$V_{ce} \text{ max} = 12 \text{ eV}$	
$N_{ab} = 1\text{E}15$	cm^{-3}	$x_1 - x_e = 1 \text{ } \mu\text{m}$	
$\tau_{nb} = 1E-5$	s	$x_2 - x_1 = 2 \text{ } \mu\text{m}$	
n-Collector		$x_c - x_2 = 10 \text{ } \mu\text{m}$	
Minority $\mu_{pc} = 480$	cm^2/Vs	$T = 300 \text{ K}$	
$N_{dc} = 1\text{E}14$	cm^{-3}	<input type="button" value="Calculate"/>	
$\tau_{pc} = 1E-5$	s		

$$I_C \sim \beta I_B$$

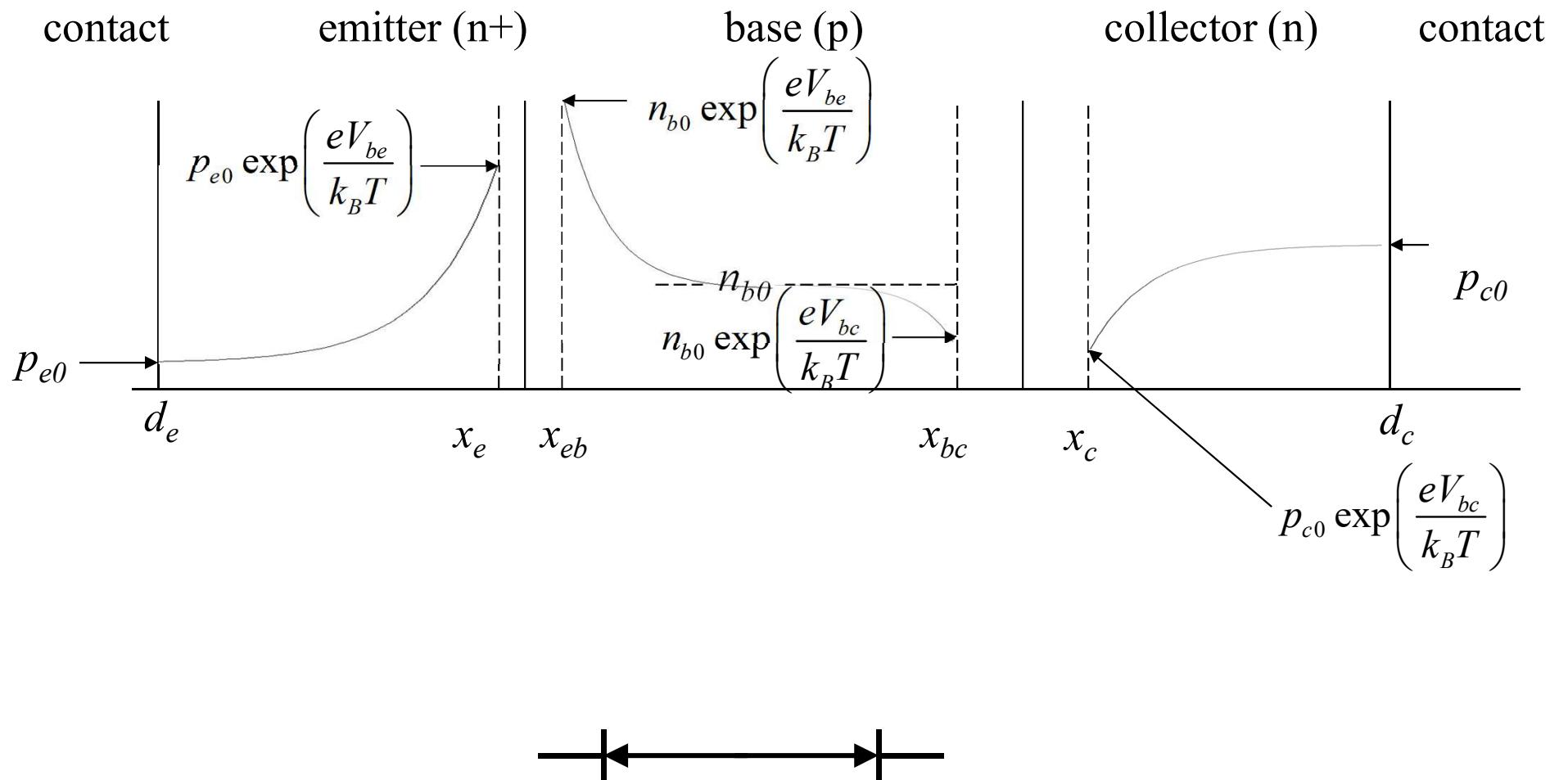


Common emitter configuration

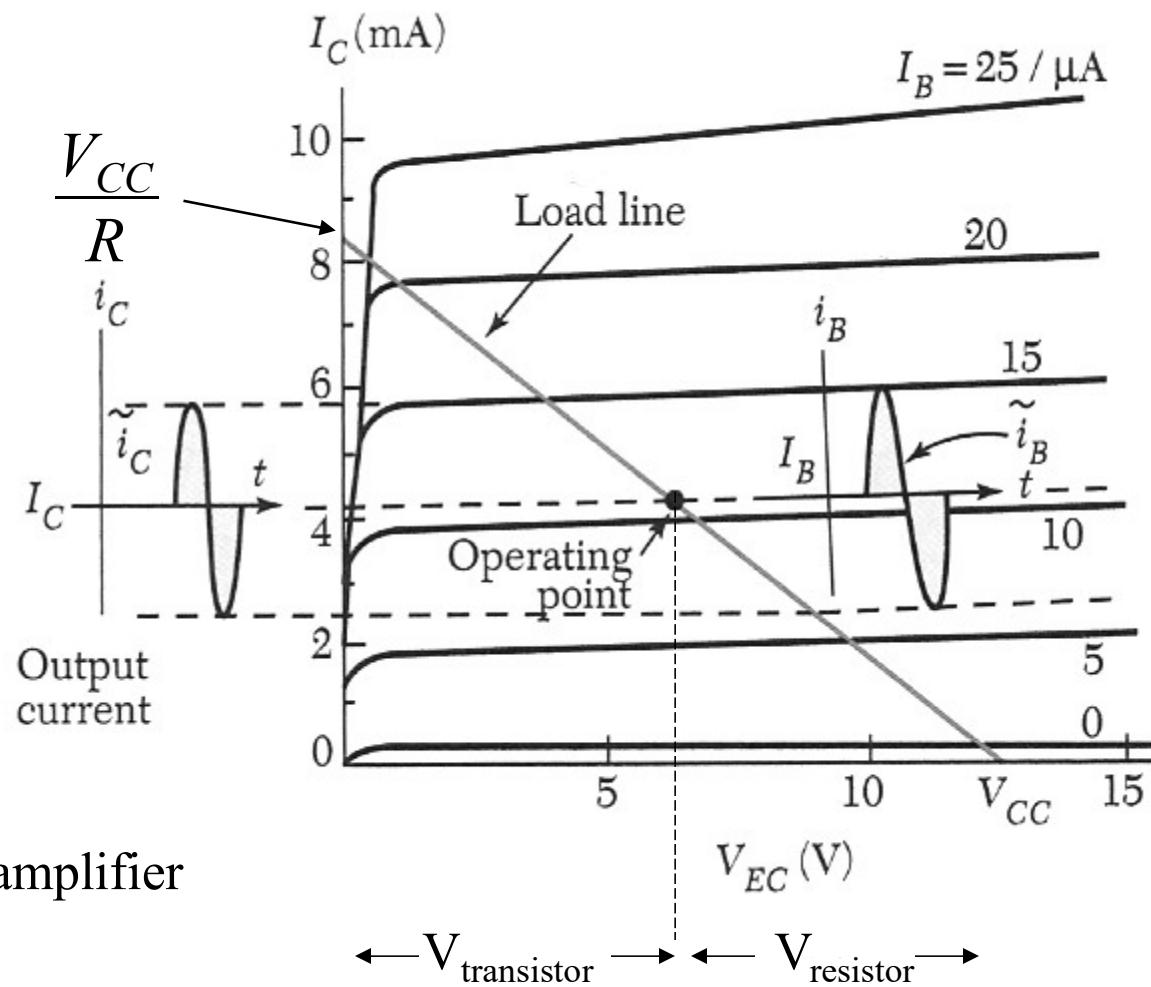
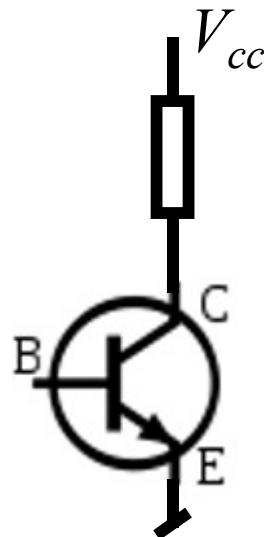


$I_C \sim \beta I_B$ amplifier

Not an npn transistor



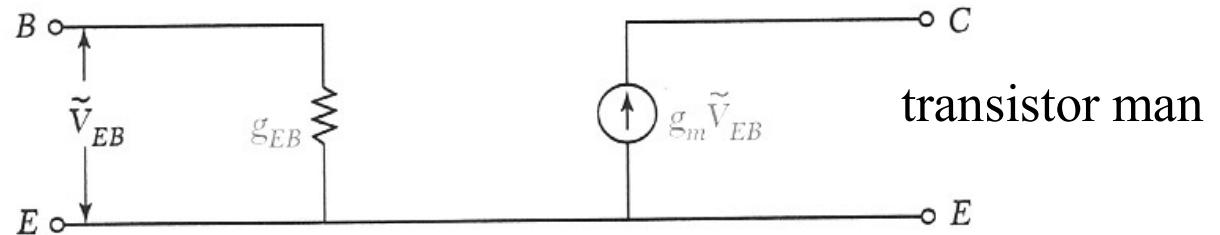
Small signal response



Low input impedance amplifier

Small signal response

$$\tilde{i}_c = \beta \tilde{i}_B = \beta g_{EB} \tilde{v}_{EB}$$

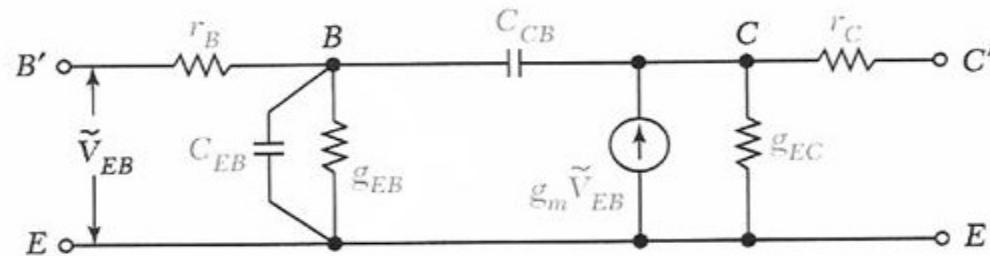
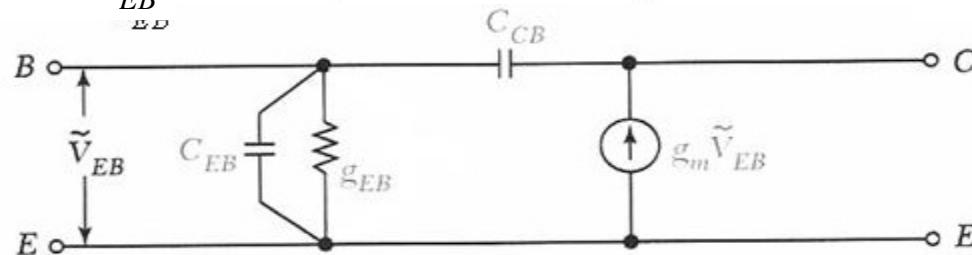


input conductance:

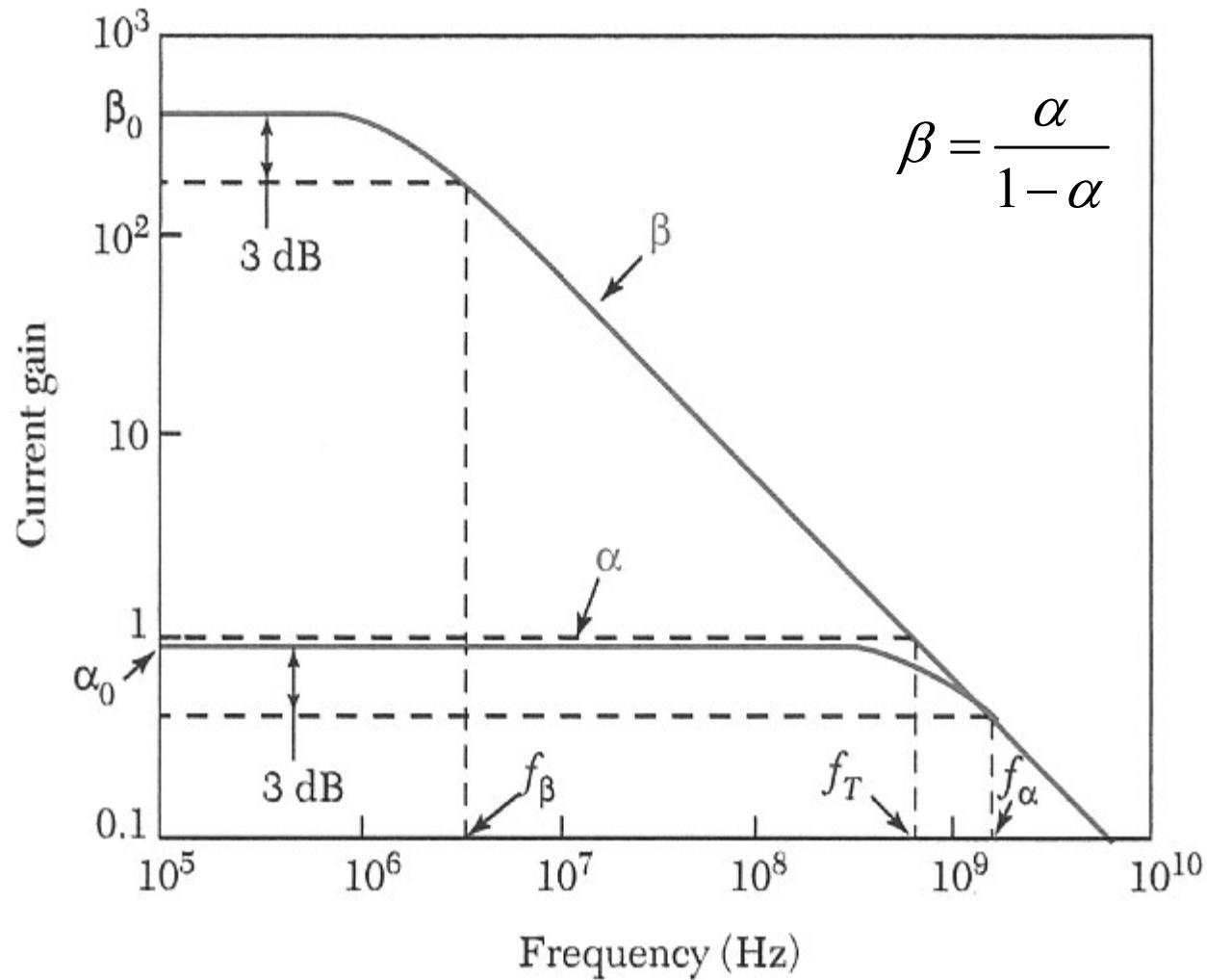
$$g_{EB} = \frac{\tilde{i}_B}{\tilde{v}_{EB}}$$

transistor man

$$g_m = \frac{\tilde{i}_c}{\tilde{v}_{EB}}$$



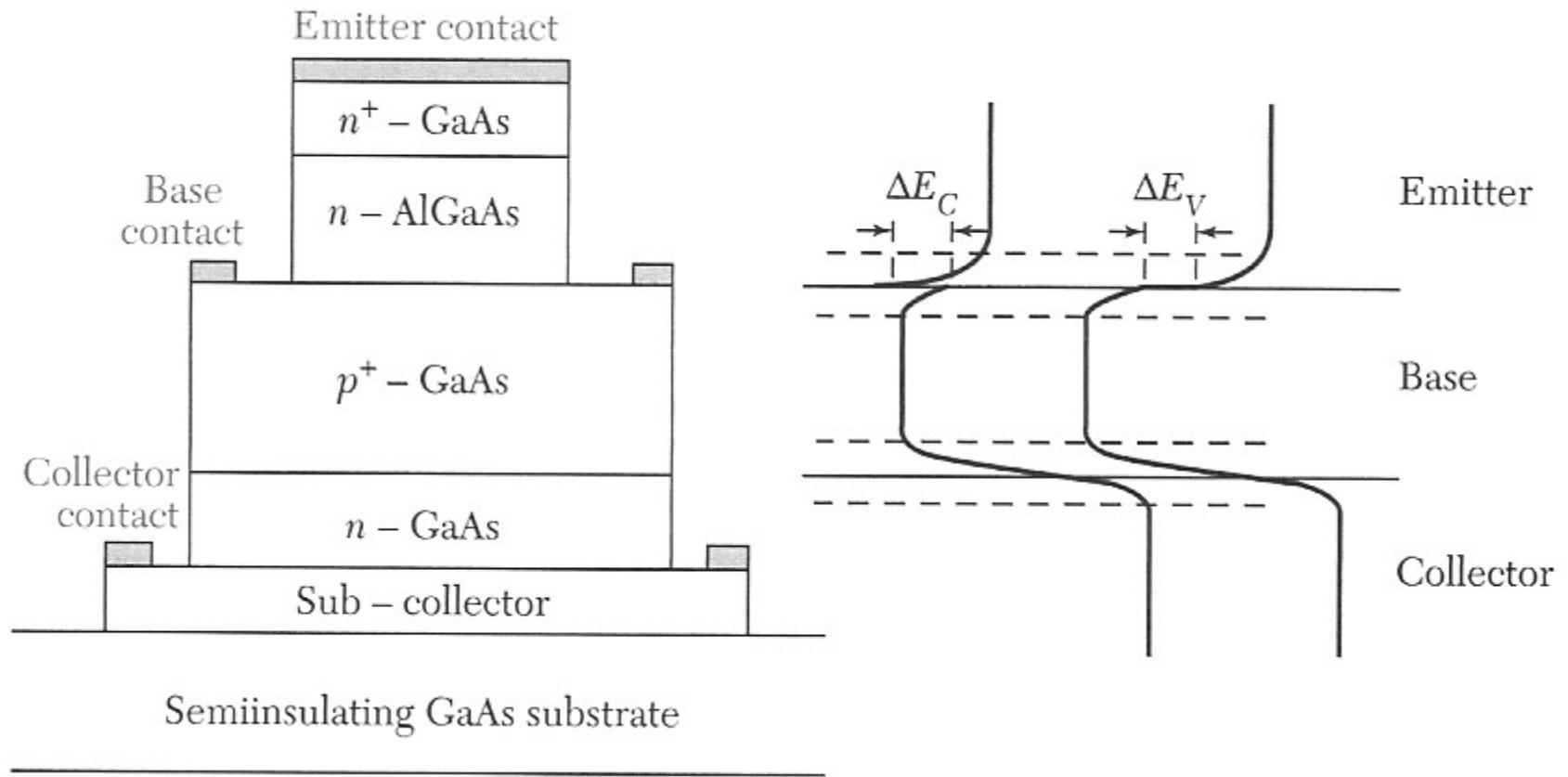
Small signal response



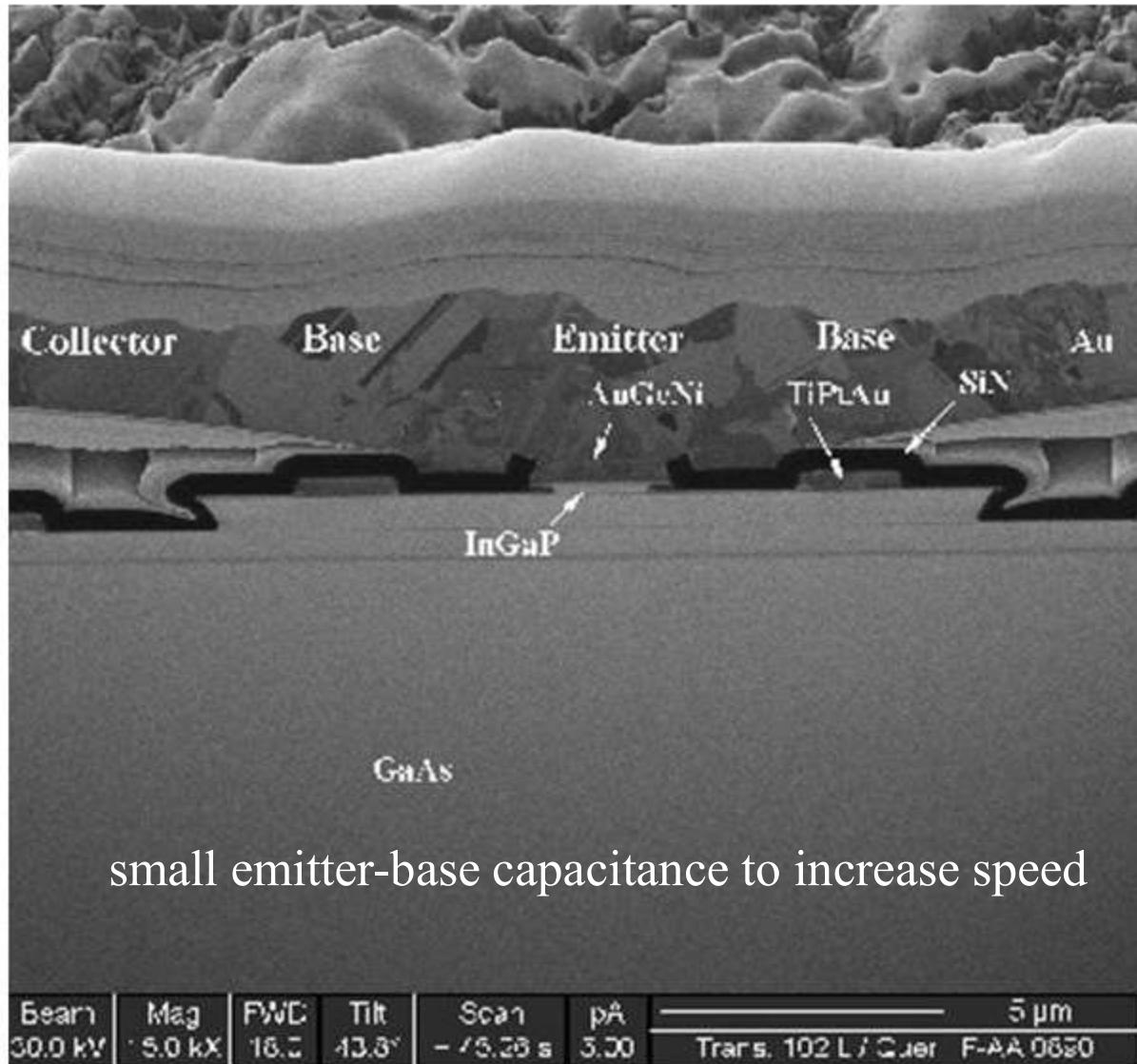
$$f_\beta = (1 - \alpha_0) f_\alpha$$

$$f_T = \alpha_0 f_\alpha$$

Heterojunction bipolar transistors



Heterojunction bipolar transistor



HBT current gain

$$I_C = \beta I_B$$

$$\beta = \frac{\alpha}{1-\alpha} \approx \frac{n_{B0}}{p_{E0}} \quad (\text{npn})$$

Higher doping in the emitter makes the minority carrier concentration lower in the emitter.

$$n_{B0} = \frac{n_i^2}{N_A} = \frac{N_C N_V \exp(-E_{gB} / k_B T)}{N_A}$$

$$p_{E0} = \frac{n_i^2}{N_D} = \frac{N'_C N'_V \exp(-E_{gE} / k_B T)}{N_D}$$

If the emitter and the base have different band gaps

$$\beta = \frac{N_E}{N_B} \frac{N_c N_v}{N'_c N'_v} \exp\left(\frac{\Delta E_g}{k_B T}\right) \sim 100000$$

HBT current gain

A HBT has an emitter bandgap of 1.62 and a base bandgap of 1.42.

A BJT has an emitter bandgap of 1.42 and a base bandgap of 1.42.

Both have an emitter doping of 10^{18} cm^{-3} and a base doping of 10^{15} cm^{-3} .

How much larger is the gain in the HBT?

$$\frac{\beta(\text{HBT})}{\beta(\text{BJT})} = \exp\left(\frac{\Delta E_g}{k_B T}\right) = \exp\left(\frac{1.62 - 1.42}{0.0259}\right) = 2257$$

Heavy doping narrows the bandgap so if in a normal transistor the bandgap is smaller in the emitter.

HBT

Trade off gain for higher speed

Higher base doping

- lower base resistance

- reduced Early effect

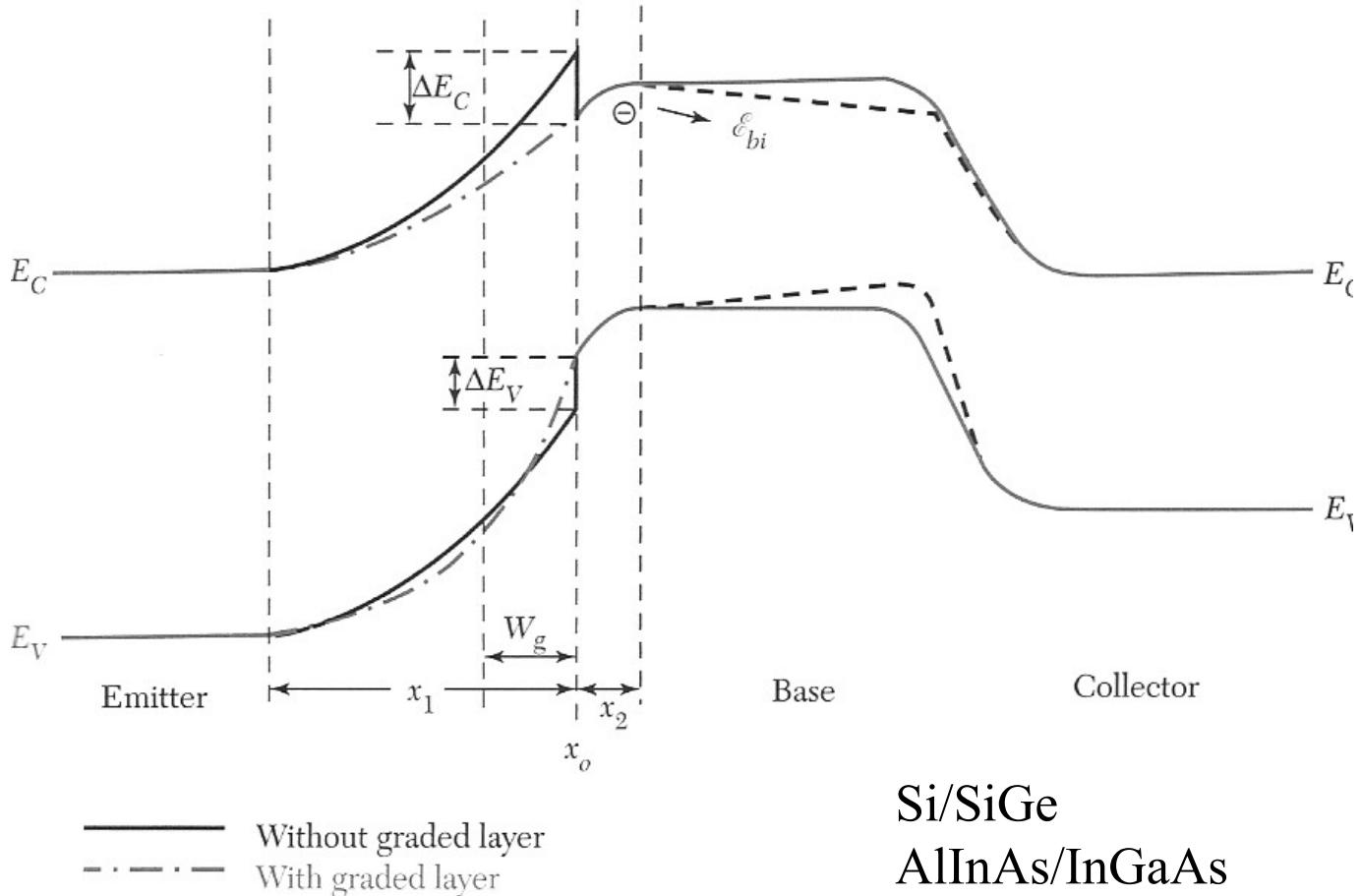
- less trouble with punch through

- base can be made thinner -> faster transistors

Because of higher base doping, a higher collector doping is possible without punch through

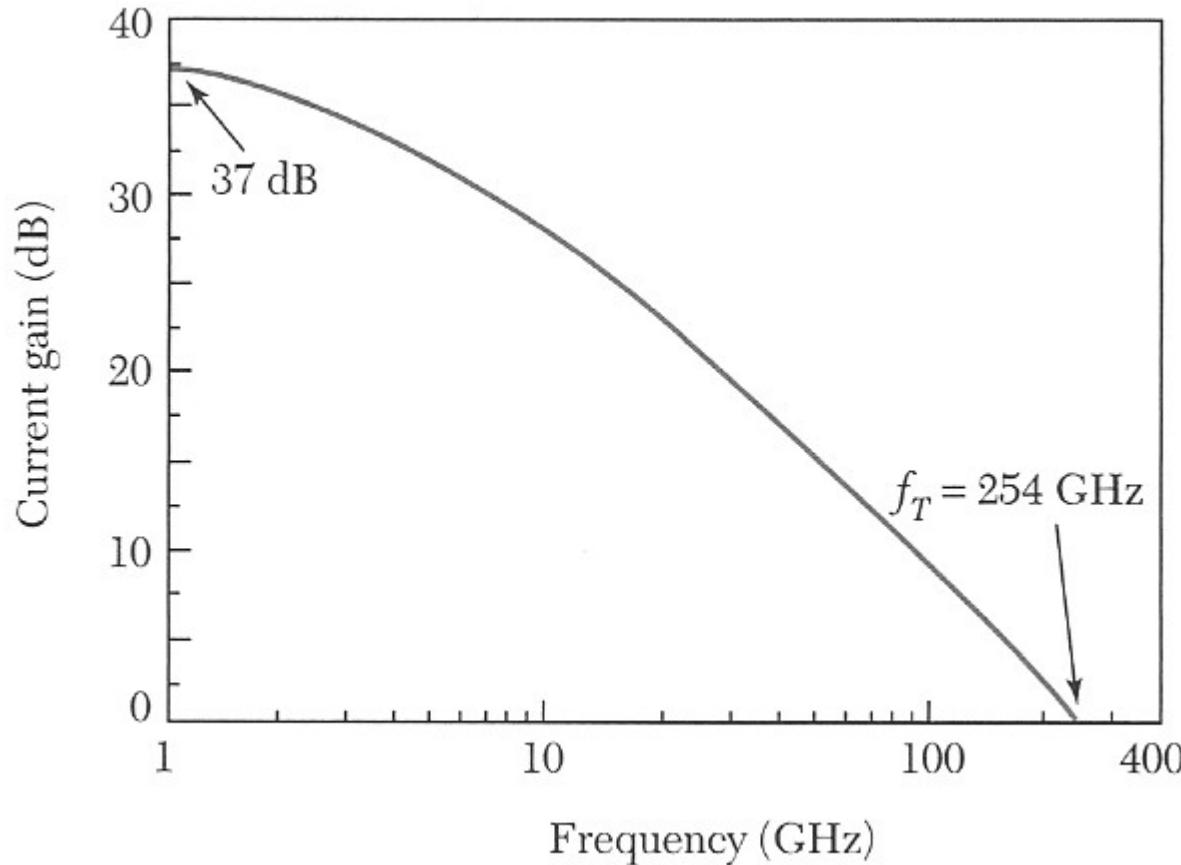
- lower collector resistance

HBT current gain



band discontinuity reduces emitter efficiency
Graded layer emitter and base improve performance

Heterojunction bipolar transistors



Fastest InP/InGaAs HBT's have an f_T of 710 GHz.

Higher doping in the base allows for a thinner base without punch through and lower base resistance and thus higher frequency operation

Microwave engineering

Electronics: $L \ll \lambda$ $f < \sim 10 \text{ GHz}$

Microwave: $\lambda < L$ $10 \text{ GHz} < f < 1 \text{ THz}$

TeraHertz: $\lambda \ll L$ $1 \text{ THz} < f < 100 \text{ THz}$

Optics: $\lambda \ll L$ 100 THz