

# Hamiltonian matrix

$$\begin{bmatrix} \langle \psi_{1,1} | H | \psi_{1,1} \rangle & \langle \psi_{1,1} | H | \psi_{1,2} \rangle & \cdots & \langle \psi_{1,1} | H | \psi_{2,1} \rangle & \langle \psi_{1,1} | H | \psi_{2,2} \rangle & \cdots & \langle \psi_{1,1} | H | \psi_{M,N} \rangle \\ \langle \psi_{1,2} | H | \psi_{1,1} \rangle & \langle \psi_{1,2} | H | \psi_{1,2} \rangle & & \langle \psi_{1,2} | H | \psi_{2,1} \rangle & \langle \psi_{1,2} | H | \psi_{2,2} \rangle & & \langle \psi_{1,2} | H | \psi_{M,N} \rangle \\ \vdots & & \ddots & & & & \vdots \\ \langle \psi_{2,1} | H | \psi_{1,1} \rangle & \langle \psi_{2,1} | H | \psi_{1,2} \rangle & & \langle \psi_{2,1} | H | \psi_{2,1} \rangle & \langle \psi_{2,1} | H | \psi_{2,2} \rangle & & \langle \psi_{2,1} | H | \psi_{M,N} \rangle \\ \langle \psi_{2,2} | H | \psi_{1,1} \rangle & \langle \psi_{2,2} | H | \psi_{1,2} \rangle & & \langle \psi_{2,2} | H | \psi_{2,1} \rangle & \langle \psi_{2,2} | H | \psi_{2,2} \rangle & & \langle \psi_{2,2} | H | \psi_{M,N} \rangle \\ \vdots & & & & & \ddots & \vdots \\ \langle \psi_{M,N} | H | \psi_{1,1} \rangle & \langle \psi_{M,N} | H | \psi_{1,2} \rangle & \cdots & \langle \psi_{M,N} | H | \psi_{2,1} \rangle & \langle \psi_{M,N} | H | \psi_{2,2} \rangle & \cdots & \langle \psi_{M,N} | H | \psi_{M,N} \rangle \end{bmatrix}.$$

$$\langle \psi_{1,2} | H | \psi_{3,4} \rangle = \langle \psi_{1,2} | -\frac{\hbar}{2m} \nabla^2 + V(\vec{r}) | \psi_{3,4} \rangle$$