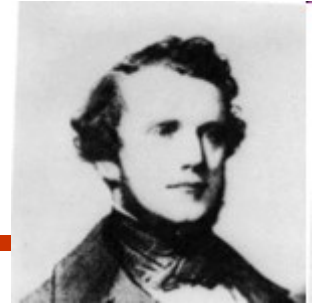
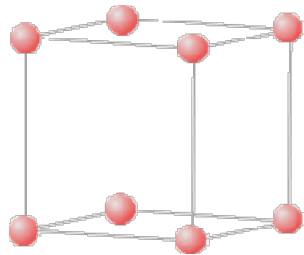
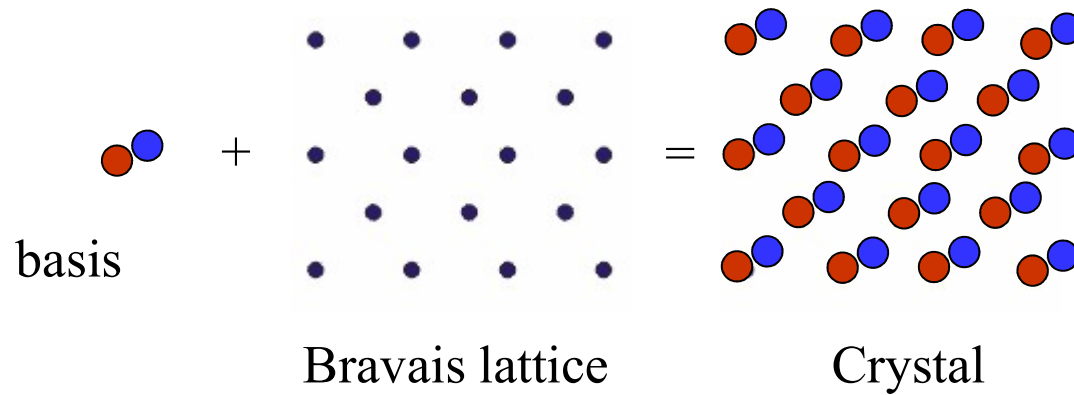


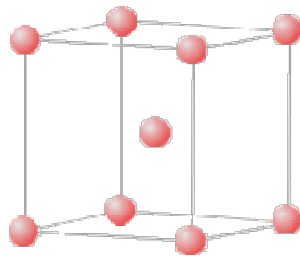
# Bravais lattice



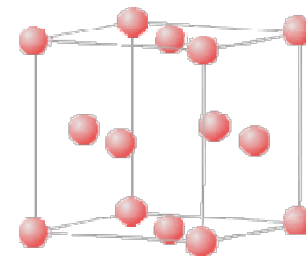
Auguste Bravais



simple cubic



body centered  
cubic, bcc



face centered  
cubic, fcc

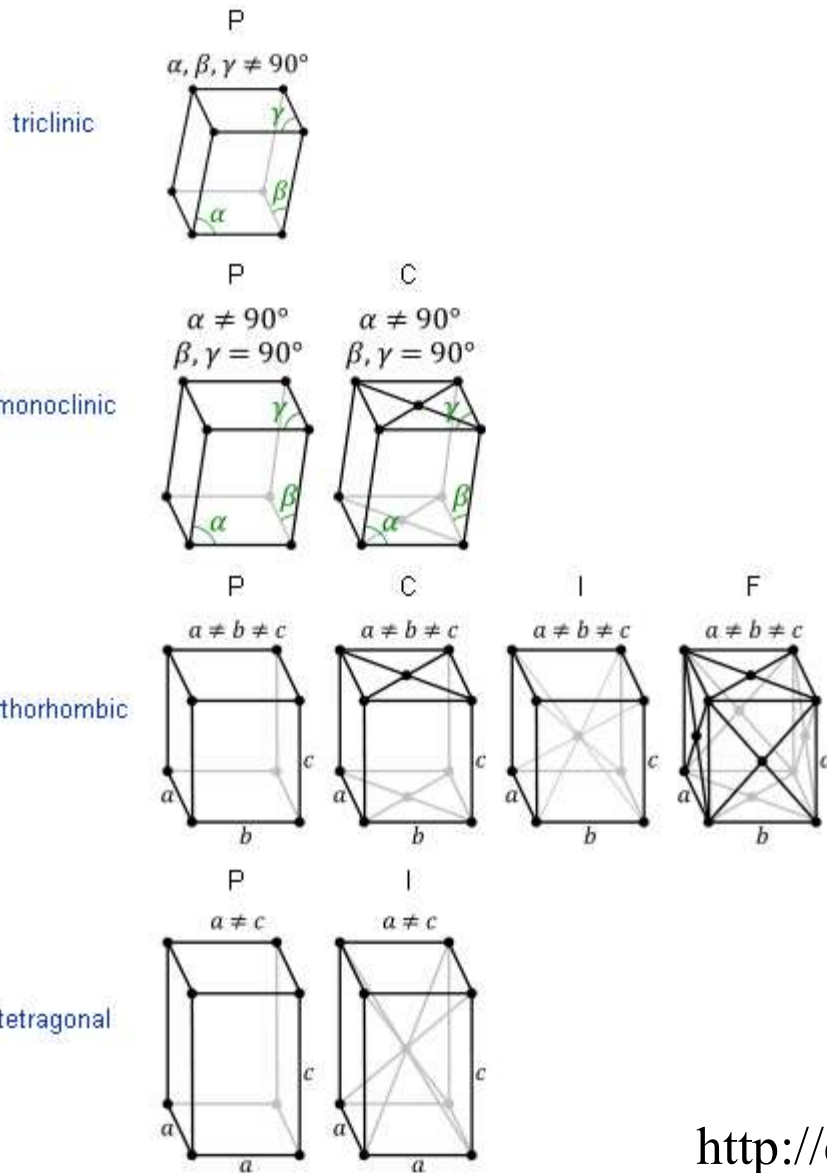
# 14 Bravais lattices

Crystal system

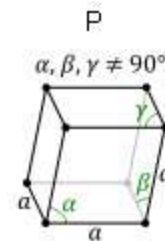
Bravais lattices

Crystal system

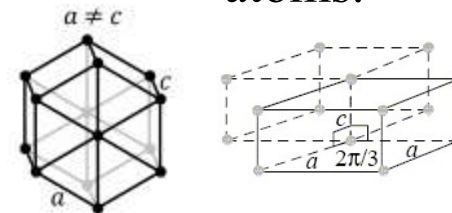
Bravais lattices



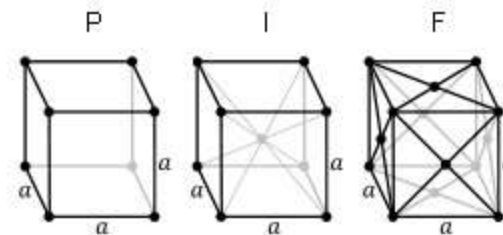
rhombohedral  
(trigonal)



hexagonal



cubic



Points of a Bravais lattice do not necessarily represent atoms.

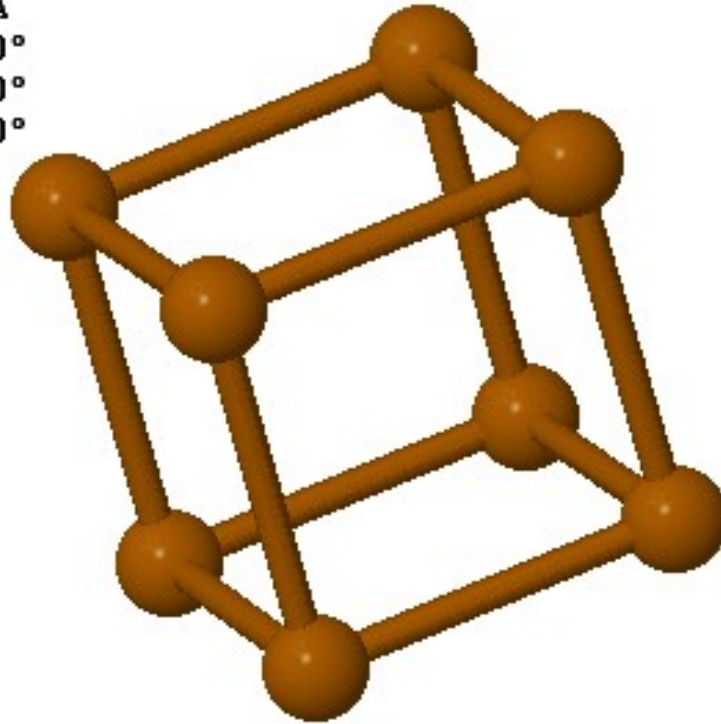
- P ... primitive
- I ... body centered
- F ... face centered
- C ... centered

[http://en.wikipedia.org/wiki/Bravais\\_lattice](http://en.wikipedia.org/wiki/Bravais_lattice)

# simple cubic

Po

HM: P m  $\bar{3}$  m  
a=3.359Å  
b=3.359Å  
c=3.359Å  
 $\alpha=90.000^\circ$   
 $\beta=90.000^\circ$   
 $\gamma=90.000^\circ$



Number: 221

Primitive Vectors:

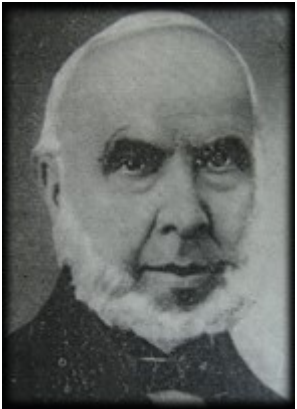
$$\vec{a}_1 = a\hat{x}$$

$$\vec{a}_2 = a\hat{y}$$

$$\vec{a}_3 = a\hat{z}$$

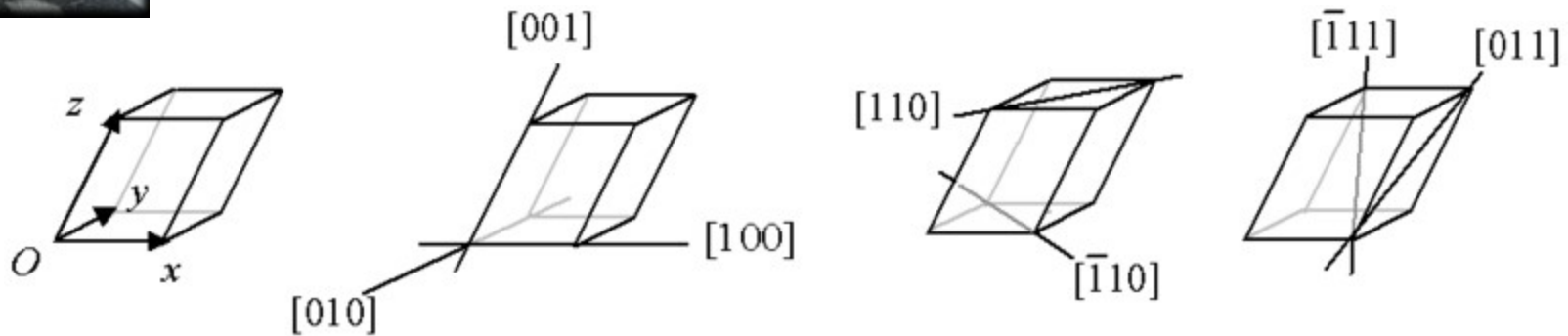
Basis Vector:  $\vec{B}_1 = (0, 0, 0)$

# Miller indices: Crystal direction $[uvw]$



$[uvw] = \text{vector in direction } u \mathbf{a} + v \mathbf{b} + w \mathbf{c}$

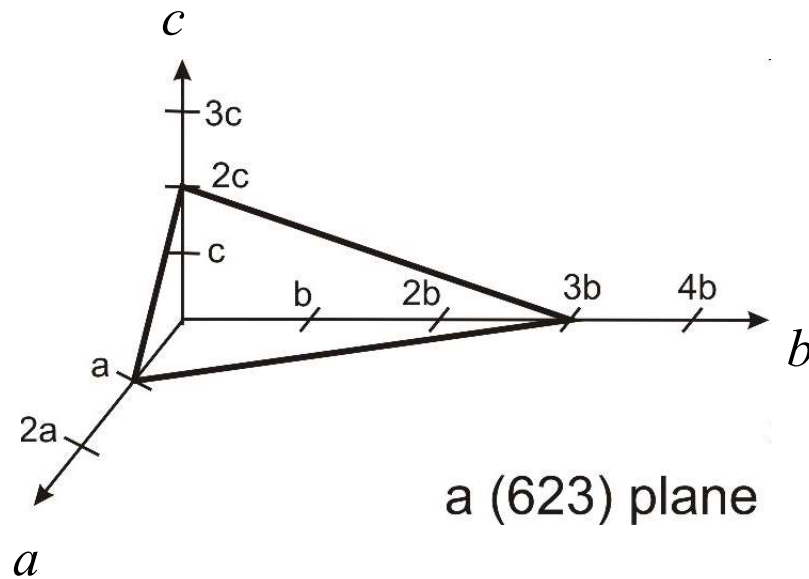
$\swarrow$        $\swarrow$        $\swarrow$   
 lattice vectors of the  
 crystallographic unit cell



notation:  $-1 = \bar{1}$

$[ ]$  specific direction  
 $\langle \rangle$  family of equivalent directions

# Miller indices: Crystal planes



( ) specific plane

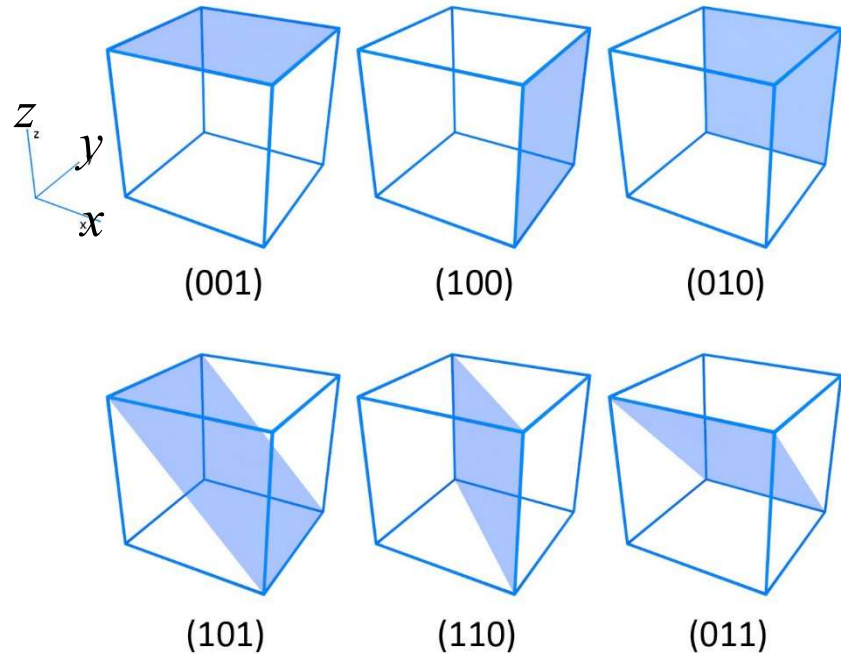
{ } family of equivalent planes



MOSFETs are made on <100> wafers

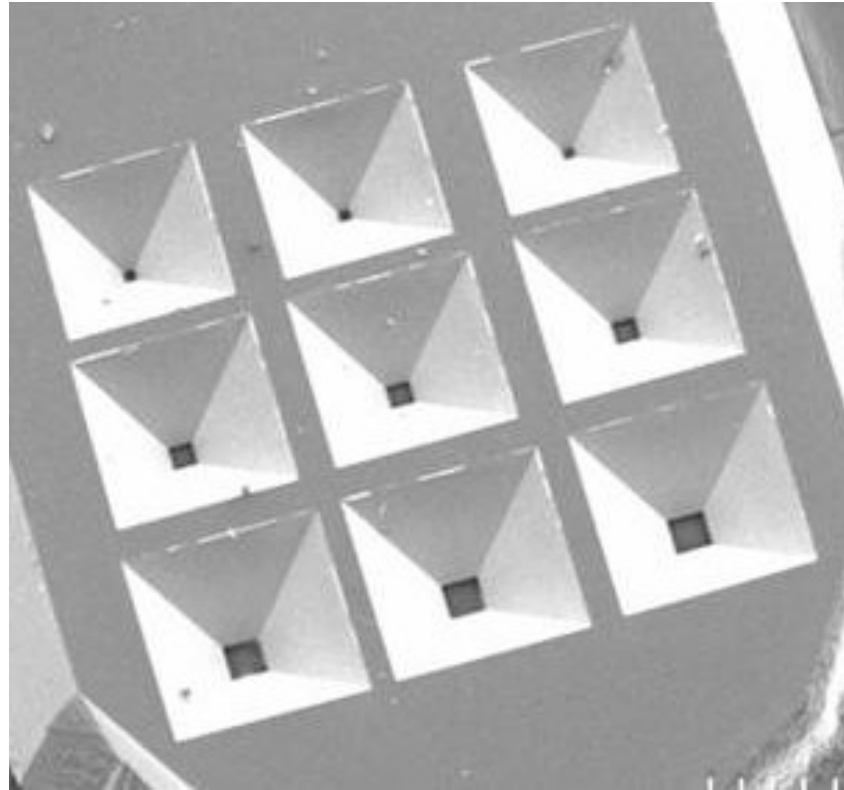
A plane with the intercepts  $1/h, 1/k, 1/l$  is the  $(h, k, l)$  plane.

always use integers for  $h, k, l$



# KOH etching of silicon

---



KOH etches Si  $\{110\} > \{100\} > \{111\}$ , producing a characteristic anisotropic V-etch, with sidewalls that form a  $54.7^\circ$  angle with the surface ( $35.3^\circ$  from the normal).

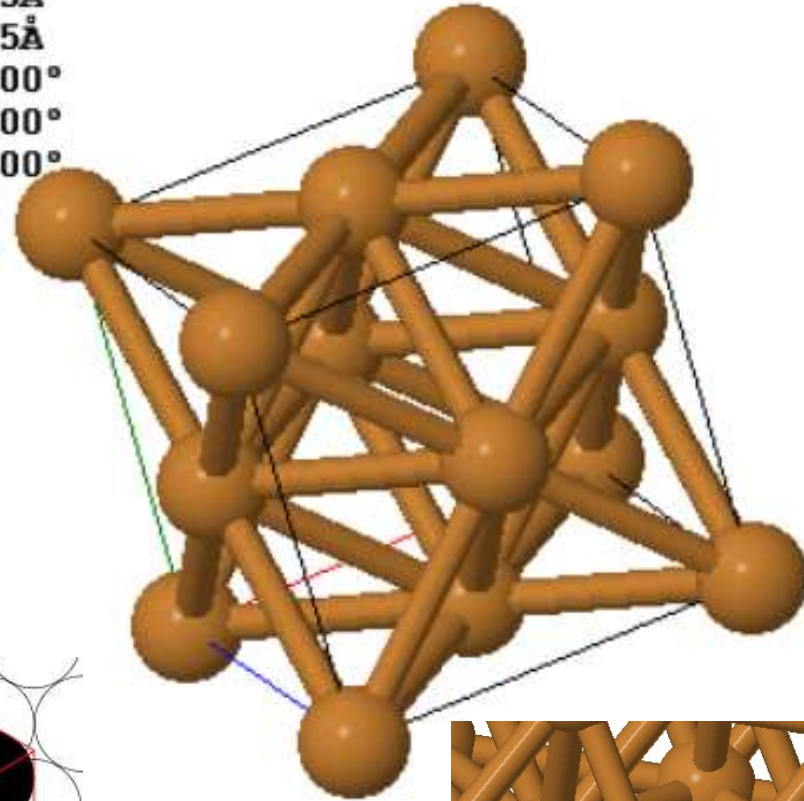
[http://www.ece.uncc.edu/research/clean\\_room/fabprocesses/KOH-EtchingAndDecon.pdf](http://www.ece.uncc.edu/research/clean_room/fabprocesses/KOH-EtchingAndDecon.pdf)

# fcc

Number 225

Al, Cu,  
Ni, Sr,  
Rh, Pd,  
Ag, Ce,  
Tb, Ir,  
Pt, Au,  
Pb, Th

HM:  $F m \bar{3} m$   
 $a=3.615\text{\AA}$   
 $b=3.615\text{\AA}$   
 $c=3.615\text{\AA}$   
 $\alpha=90.000^\circ$   
 $\beta=90.000^\circ$   
 $\gamma=90.000^\circ$



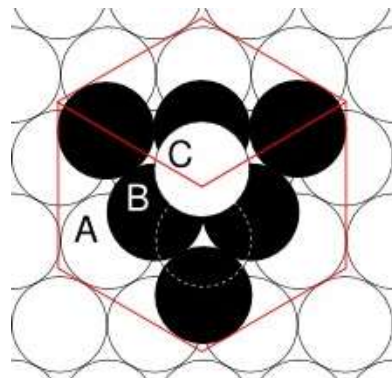
[111]

Primitive Vectors:

$$\vec{a}_1 = \frac{a}{2} \hat{y} + \frac{a}{2} \hat{z}$$

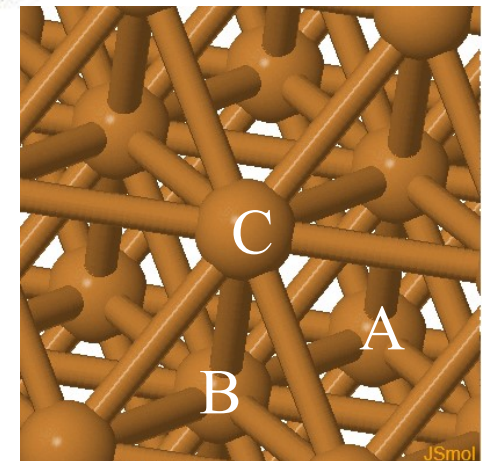
$$\vec{a}_2 = \frac{a}{2} \hat{x} + \frac{a}{2} \hat{z}$$

$$\vec{a}_3 = \frac{a}{2} \hat{x} + \frac{a}{2} \hat{y}$$



Basis Vector:

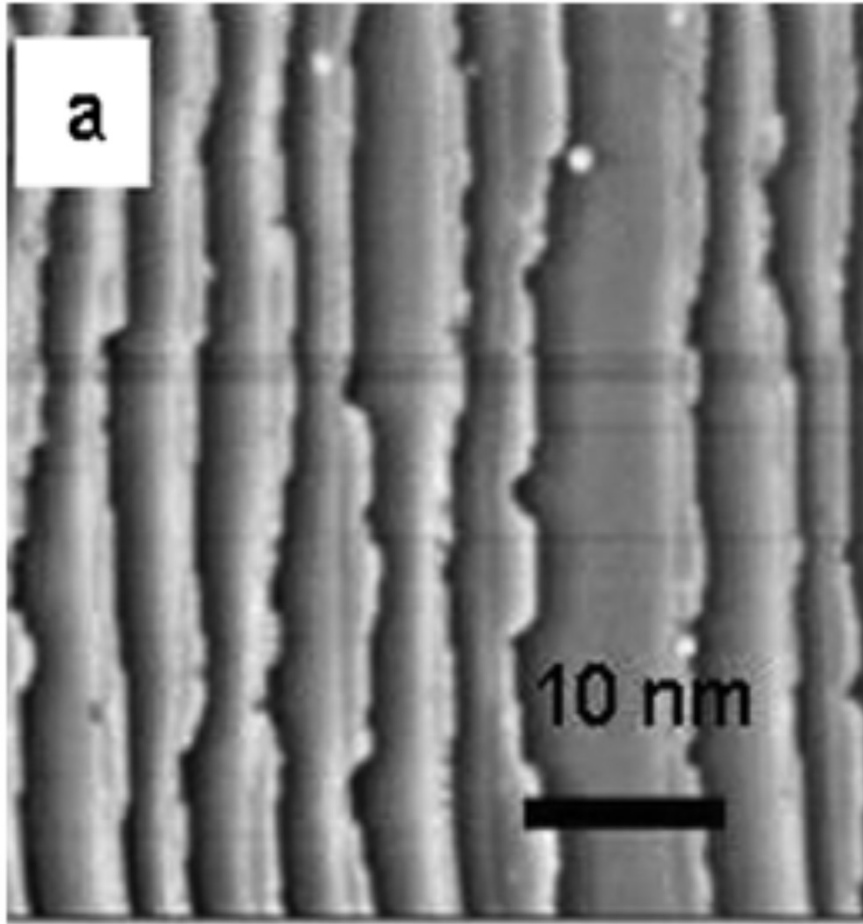
$$\vec{B}_1 = (0, 0, 0)$$



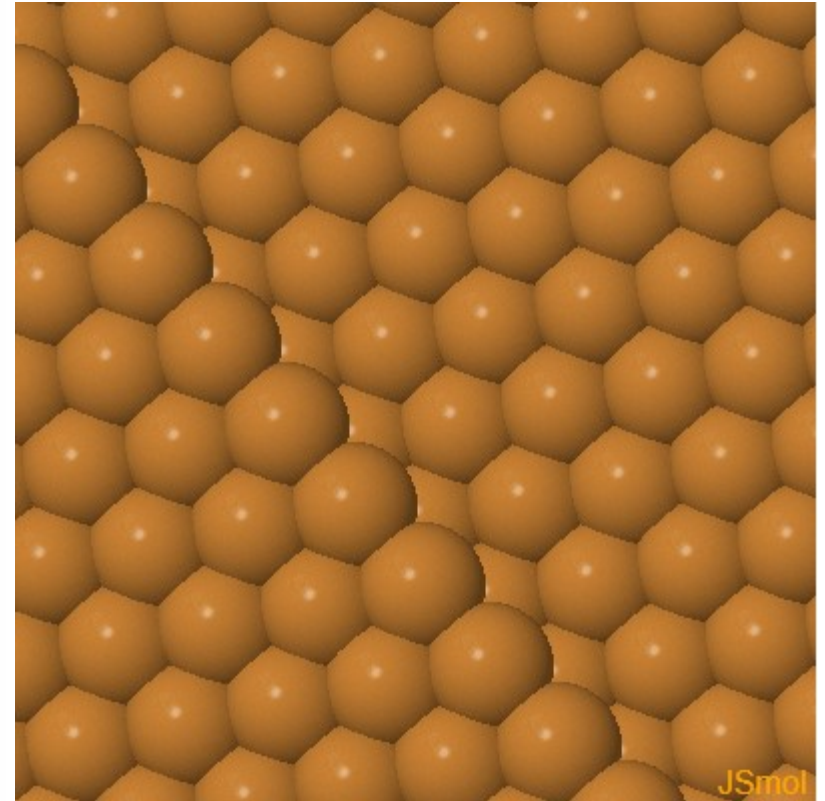
JSmol

# Crystal planes: Miller indices

---



Rh(15,15,13) fcc



(15,15,13) fcc

Reaction studies on nanostructured surfaces, Adolf Winkler, in *The Oxford Handbook of Nanoscience and Technology*, A. V. Narlikar and Y. Y. Fu ed., 2009.

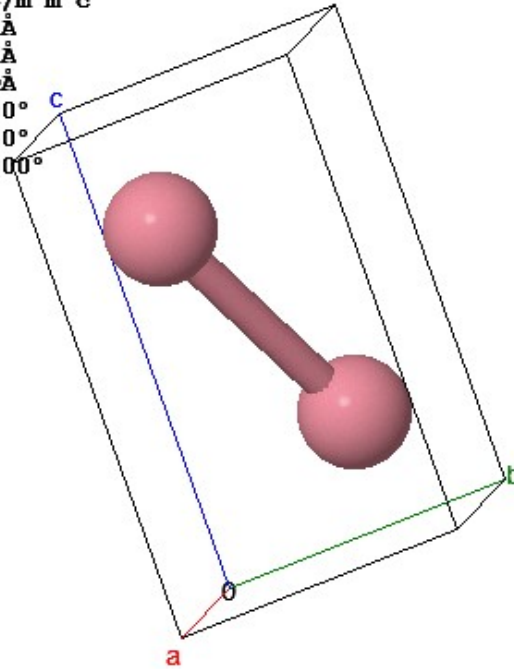


# hcp

Space group 194 Crystallographic unit cell

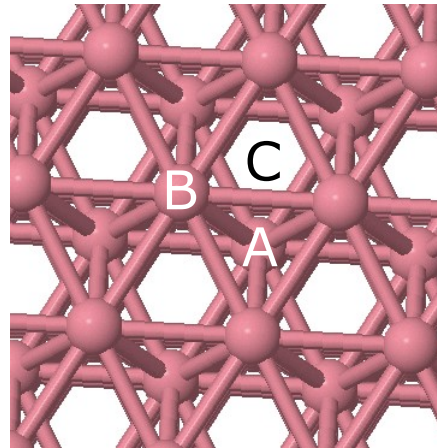
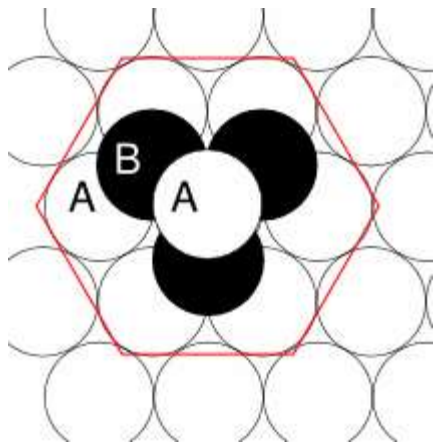
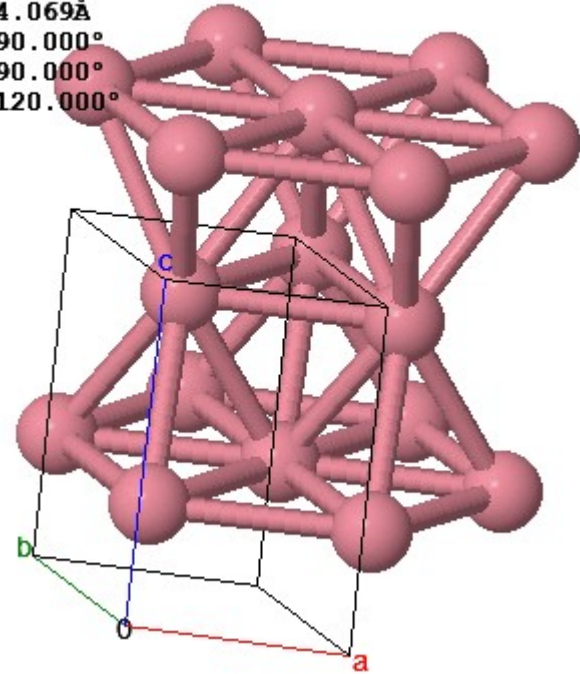
Mg, Be,  
Sc, Ti,  
Co, Zn,  
Y, Zr, Tc,  
Ru, Cd,  
Gd, Tb,  
Dy, Ho,  
Er, Tm,  
Lu, Hf,  
Re, Os,  
Tl

HM: P 63/m m c  
a=2.507Å  
b=2.507Å  
c=4.069Å  
α=90.000°  
β=90.000°  
γ=120.000°



## Hexagonal unit cell

HM: P 63/m m c  
a=2.507Å  
b=2.507Å  
c=4.069Å  
α=90.000°  
β=90.000°  
γ=120.000°



Hexagonal Bravais lattice  
Basis vectors:

$$\vec{B}_1 = (0, 0, 0) \quad \vec{B}_2 = \left(\frac{2}{3}, \frac{1}{3}, \frac{1}{2}\right)$$

# bcc

W Number 229

Na

K

V

Cr

Fe

Rb

Nb

Mo

Cs

Ba

Eu

Ta

Primitive Vectors:

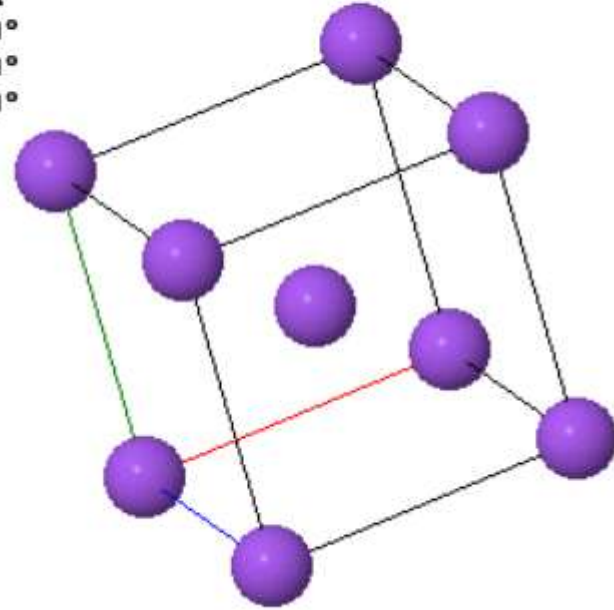
$$\vec{a}_1 = -\frac{a}{2}\hat{x} + \frac{a}{2}\hat{y} + \frac{a}{2}\hat{z}$$

$$\vec{a}_2 = \frac{a}{2}\hat{x} - \frac{a}{2}\hat{y} + \frac{a}{2}\hat{z}$$

$$\vec{a}_3 = \frac{a}{2}\hat{x} + \frac{a}{2}\hat{y} - \frac{a}{2}\hat{z}$$

Basis Vector:  $\vec{B}_1 = (0, 0, 0)$

HM: IM-3M  
a=4.291Å  
b=4.291Å  
c=4.291Å  
α=90.000°  
β=90.000°  
γ=90.000°

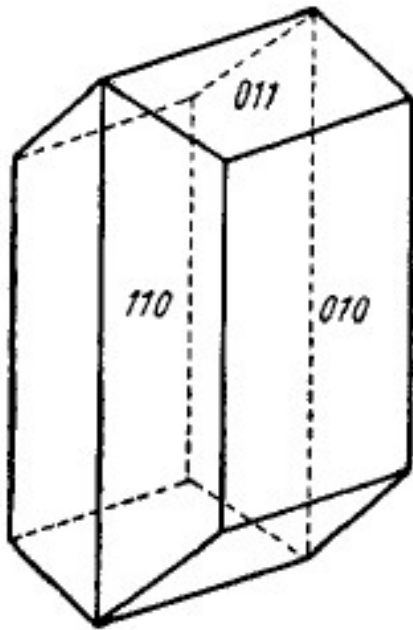


# Crystals

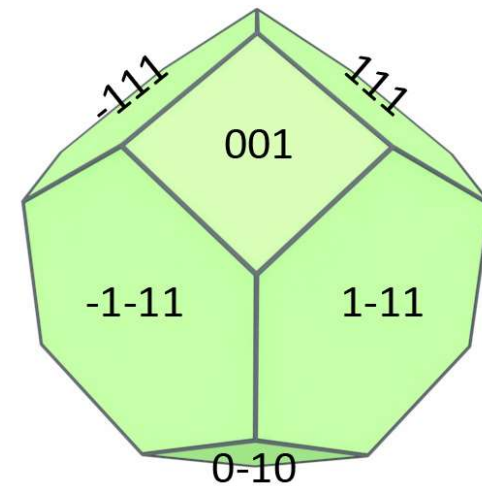
## rule of rationality

R. J. Haüy (1743-1822):

the indices of external planes of crystals are generally simple full numbers



orthorhombic  
Aragonit  $\text{CaCO}_3$



one possible morphology  
of a crystal with cubic structure

Bravais:

Planes with high atomic densities tend to dominate

# Sodalite

From Wikipedia, the free encyclopedia

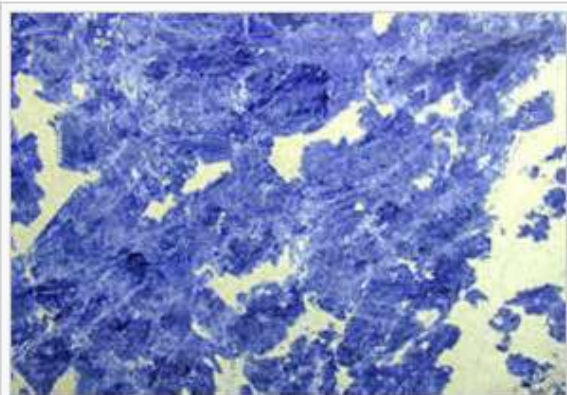
**Sodalite** is a rich royal blue mineral widely enjoyed as an ornamental gemstone. Although massive sodalite samples are opaque, crystals are usually transparent to translucent. Sodalite is a member of the sodalite group with *hauyne*, *nosean*, *lazurite* and *tugtupite*.

Discovered in 1811 in the *Ilimaussaq intrusive complex* in Greenland, sodalite did not become important as an ornamental stone until 1891 when vast deposits of fine material were discovered in *Ontario, Canada*.

## Contents [hide]

- 1 Properties
- 2 Hackmanite
- 3 Occurrence
- 4 References

## Properties [edit]



A sample of **sodalite-carbonate nephrite** from Bolivia, with a polished rock.

A light, relatively hard yet fragile mineral, sodalite is named after its *sodium* content; in *mineralogy* it may be classed as a *feldspathoid*. Well known for its blue color, sodalite may also be grey, yellow, green, or pink and is often mottled with white veins or patches. The more uniformly blue material is used in *jewellery*, where it is fashioned into *cabochons* and *beads*. Lesser material is more often seen as *facing* or *inlay* in

## Sodalite



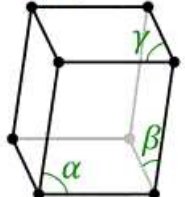
A sample of sodalite

## General

<b>Category</b>	Tectosilicates without zeolitic H <sub>2</sub> O
<b>Formula (repeating unit)</b>	Na <sub>8</sub> (Al <sub>6</sub> Si <sub>6</sub> O <sub>24</sub> )Cl <sub>2</sub>
<b>Strunz classification</b>	09.FB.10
<b>Crystal symmetry</b>	Isometric hextetrahedral H-M symbol: $\bar{4}3m$ Space group: $P\bar{4}3n$ <b>218</b>
<b>Unit cell</b>	$a = 8.876(6) \text{ \AA}$ ; $Z = 1$

## Identification

# The 32 Crystal Classes

Crystal system	Crystal Class	International symbol	Schoenflies symbol	Space groups	2-fold axes	3-fold axes	4-fold axes	6-fold axes	mirror planes	inversion	Examples	Number of symmetry elements
<b>Triclinic</b> $a \neq b \neq c$ $\alpha \neq \beta \neq \gamma$ 	triclinic-pedial	1	$C_1$	1: P1	-	-	-	-	-	n		1
	triclinic-pinacoidal	$\bar{1}$	$S_2 = C_i$	2: $P\bar{1}$	-	-	-	-	-	y		2
<b>Monoclinic</b> $a \neq b \neq c$ $\alpha \neq 90^\circ$ , $\beta = \gamma = 90^\circ$ 	monoclinic-sphenoidal	2	$C_2$	3: P2, 4: $P2_1$ , 5: C2	1	-	-	-	-	n		2
	monoclinic-domatic	$m$	$C_{1h} = C_s$	6: Pm, 7: Pc, 8: Cm, 9: Cc	-	-	-	-	1	n		2
	monoclinic-prismatic	$2/m$	$C_{2h}$	10: P2/m, 11: $P2_1/m$ , 12: C2/m, 13: P2/c, 14: $P2_1/c$ , 15: C2/c	1	-	-	-	1	y		4
<b>Orthorhombic</b> $a \neq b \neq c$ $\alpha = \beta = \gamma = 90^\circ$ 	orthorhombic-disphenoidal	222	$V = D_2$	16: P222, 17: $P222_1$ , 18: $P2_12_12_1$ , 19: $P2_12_12_1$ , 20: $C222_1$ , 21: C222, 22: F222, 23: I222, 24: $I2_12_12_1$	3	-	-	-	-	n		4

# International Tables for Crystallography

## Volume A: Space-group symmetry

First online edition (2006) ISBN: 978-0-7923-6590-7 eISBN: 978-1-4020-5406-8 doi: 10.1107/97809553602060000100

Edited by Th. Hahn



- | [contents](#) | [indexes](#) |
- | [contributors](#) | [editors](#) |
- | [sample pages](#) | [purchase](#) |
- | [explanation of the space-group data](#) |

Go to  No.

- 1 (P1)
- 2 (P-1)
- 3 (P2)
- 4 (P21)
- 5 (C2)
- 6 (Pm)
- 7 (Pc)
- 8 (Cm)
- 9 (Cc)
- 10 (P2/m)
- 11 (P21/m)
- 12 (C2/m)
- 13 (P2/c)
- 14 (P21/c)
- 15 (C2/c)
- 16 (P222)
- 17 (P2221)
- 18 (P21212)
- 19 (P212121)
- 20 (C2221)

Volume A treats crystallographic symmetry in direct or physical space. It contains extensive tables of the 17 plane groups, the 230 space groups and the 32 crystallographic point groups.

The first five parts of the volume contain introductory material: lists of symbols and terms; symbols; and unit-cell (coordinate) transformations. These are followed by the plane-group tables; the determination of space groups; synoptic tables of space-groups (Parts 6 and 7). For each group type, the following information is presented:

- headline with the relevant group symbols;
- diagrams of the symmetry elements and of the general position;
- specification of the origin and the asymmetric unit;
- list of symmetry operations;
- generators;
- general and special positions with multiplicities, site symmetries, coordinates and reflections;
- symmetries of special projections;
- extensive subgroup and supergroup data.

Parts 8 to 15 deal with the following aspects of symmetry theory: the mathematical approach to space groups; crystal lattices; point groups and crystal classes; symbols for symmetry operations; symbols for space groups; isomorphic subgroups of space groups; lattice complexes; and normalizers of space groups.

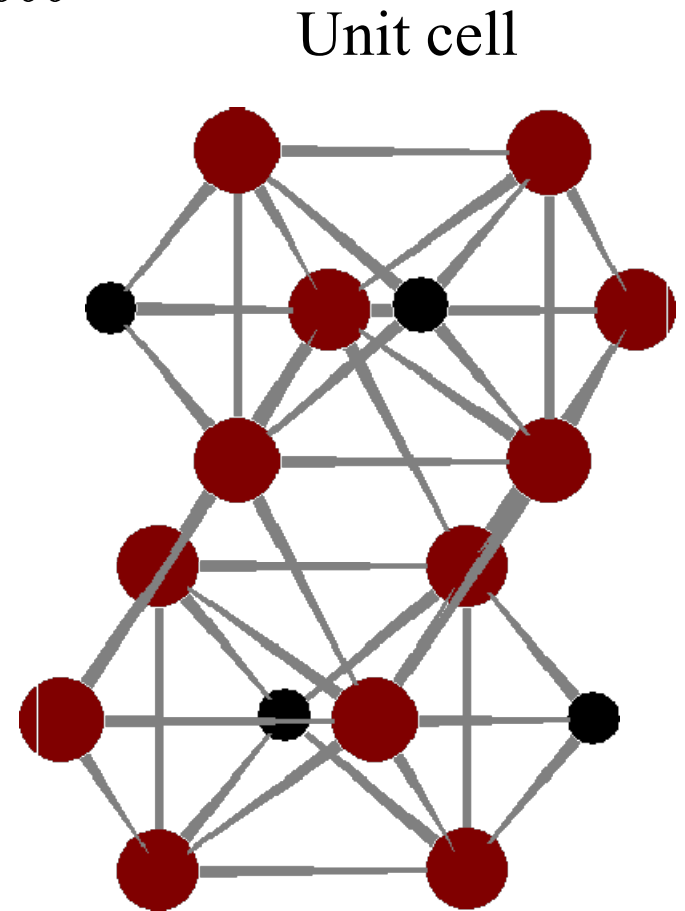
# Asymmetric unit

---

```
cell 5.09000 6.74800 4.52300 90.000 90.000 90.000
natom 3
Fe1 26 0.18600 0.06300 0.32800
Fe2 26 0.03600 0.25000 0.85200
C 6 0.89000 0.25000 0.45000
rgnr 62
Cohenite (Cementite) Fe3 C
```

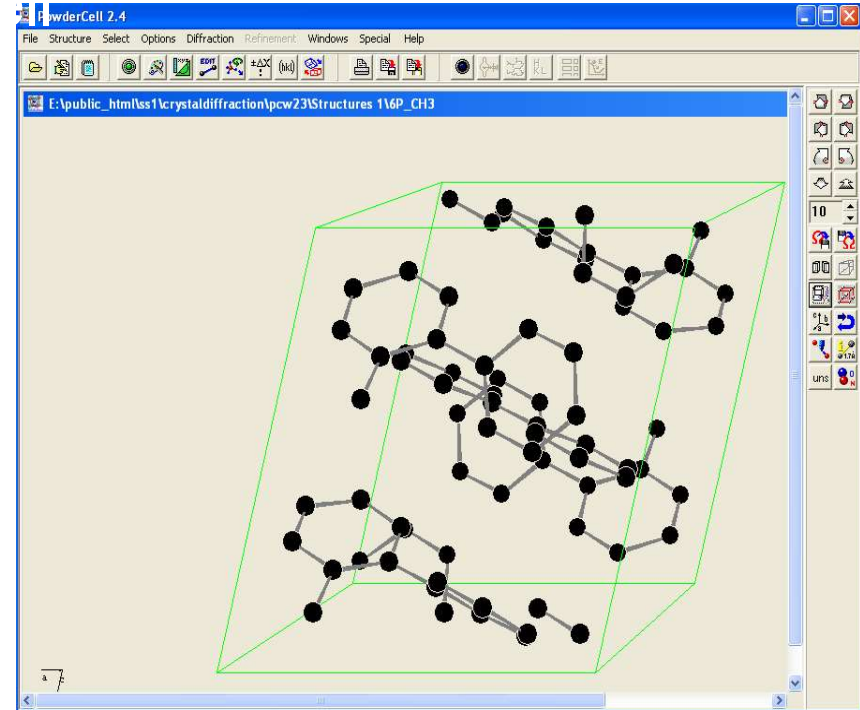


Asymmetric unit

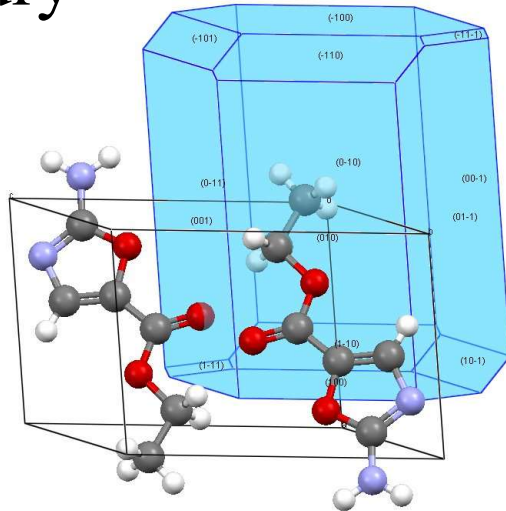


Unit cell

# PowderCell



# Mercury

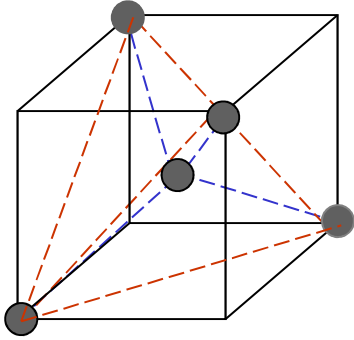


[http://www.bam.de/de/service/publikationen/powder\\_cell.htm](http://www.bam.de/de/service/publikationen/powder_cell.htm)

<https://www.ccdc.cam.ac.uk/Community/csd-community/freemercury/>

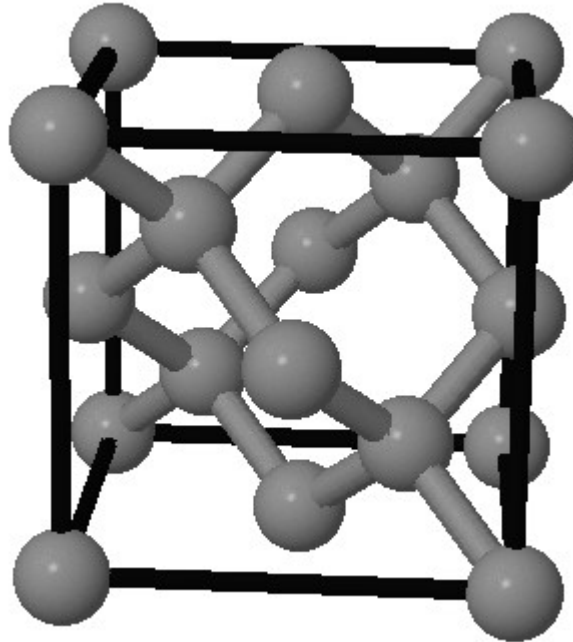


# Diamond



$$a = b = c, \quad \alpha = 90^\circ, \beta = 90^\circ, \gamma = 90^\circ$$

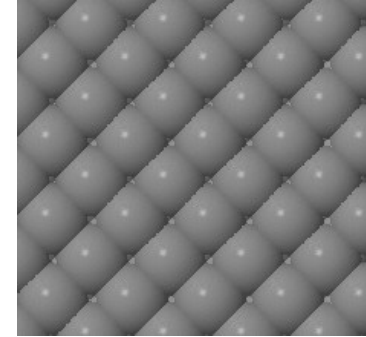
Space group: 227  
point group: m3m



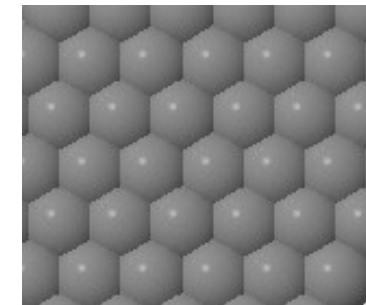
Primitive lattice vectors:

$$\vec{a}_1 = \frac{a}{2}\hat{x} + \frac{a}{2}\hat{y}, \quad \vec{a}_2 = \frac{a}{2}\hat{x} + \frac{a}{2}\hat{z}, \quad \vec{a}_3 = \frac{a}{2}\hat{y} + \frac{a}{2}\hat{z}.$$

Basis:  $\vec{B}_1 = (0, 0, 0), \quad \vec{B}_2 = (0.25, 0.25, 0.25).$



$$(100): \frac{2}{a^2}$$



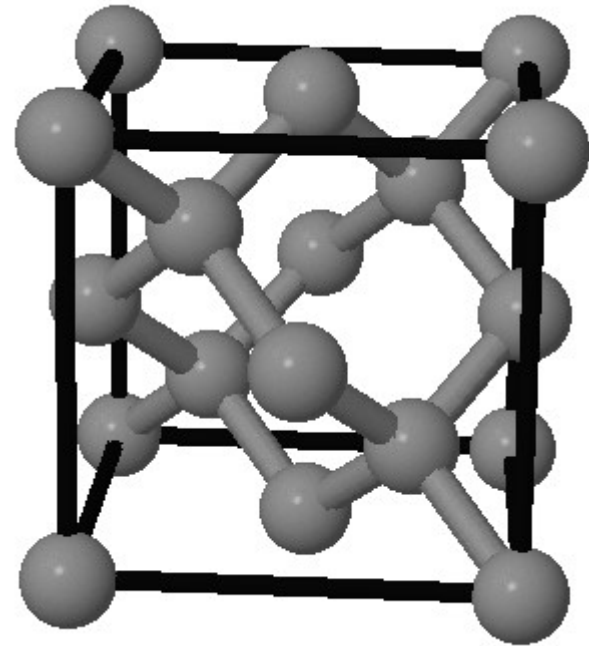
$$(111): \frac{4}{\sqrt{3}a^2}$$

# Inequivalent atoms in the unit cell

---



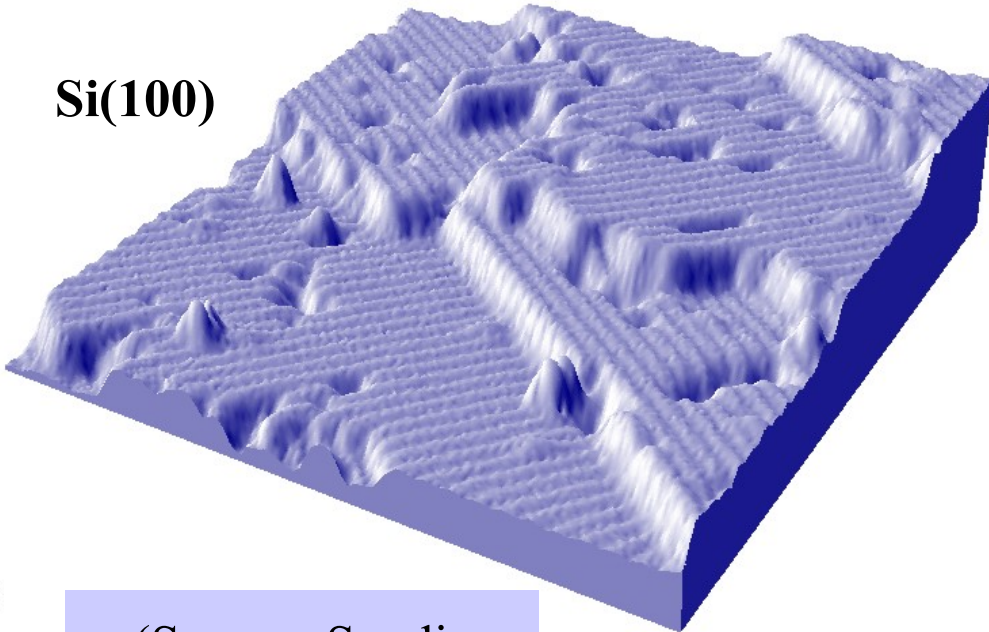
An element can have two distinct positions



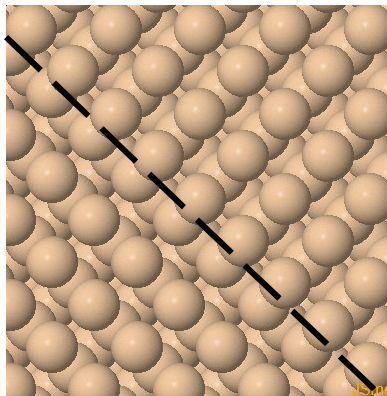
Diamond conventional unit cell

# Silicon surfaces

Si(100)



(Source: Sandia  
Nat.Labs.)

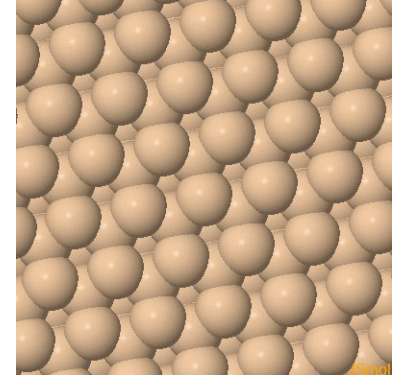


atomic  
step in  
Si(100)

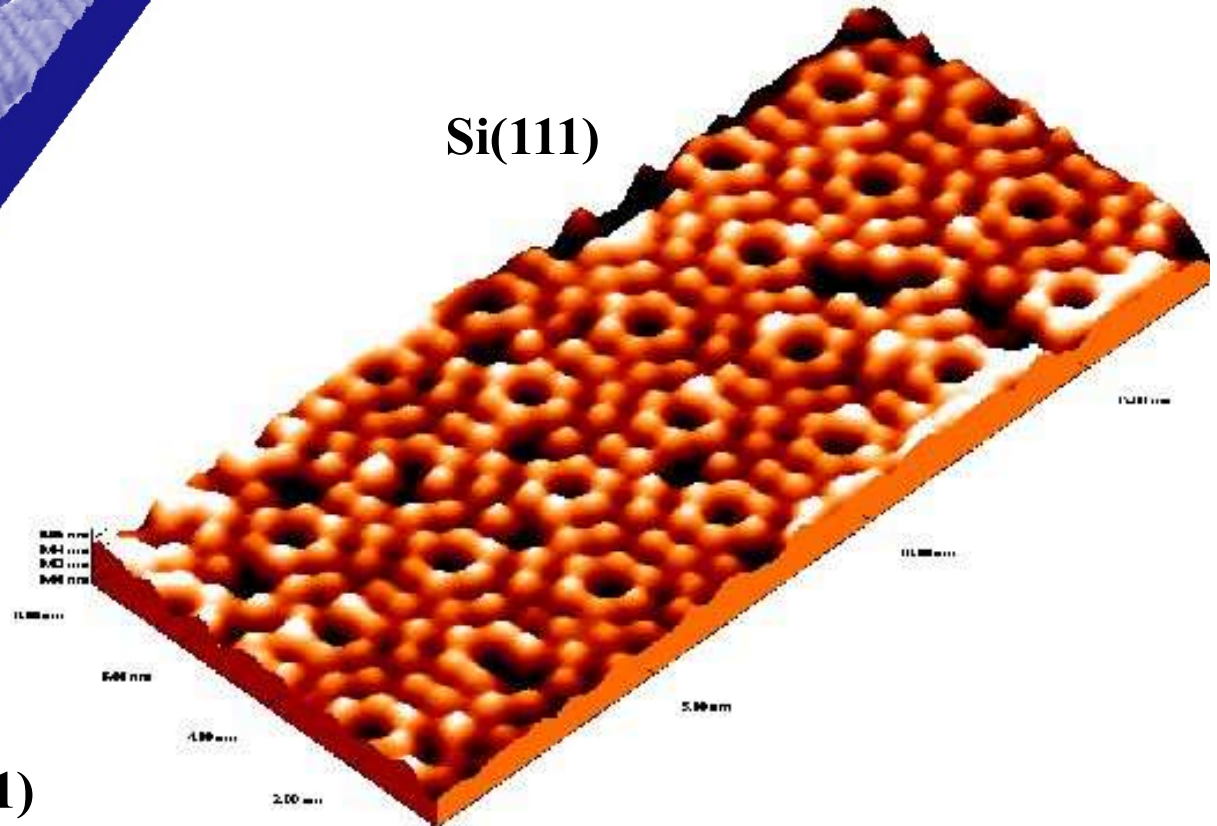
Si(20 1 1)

unreconstructed

Si(111) →

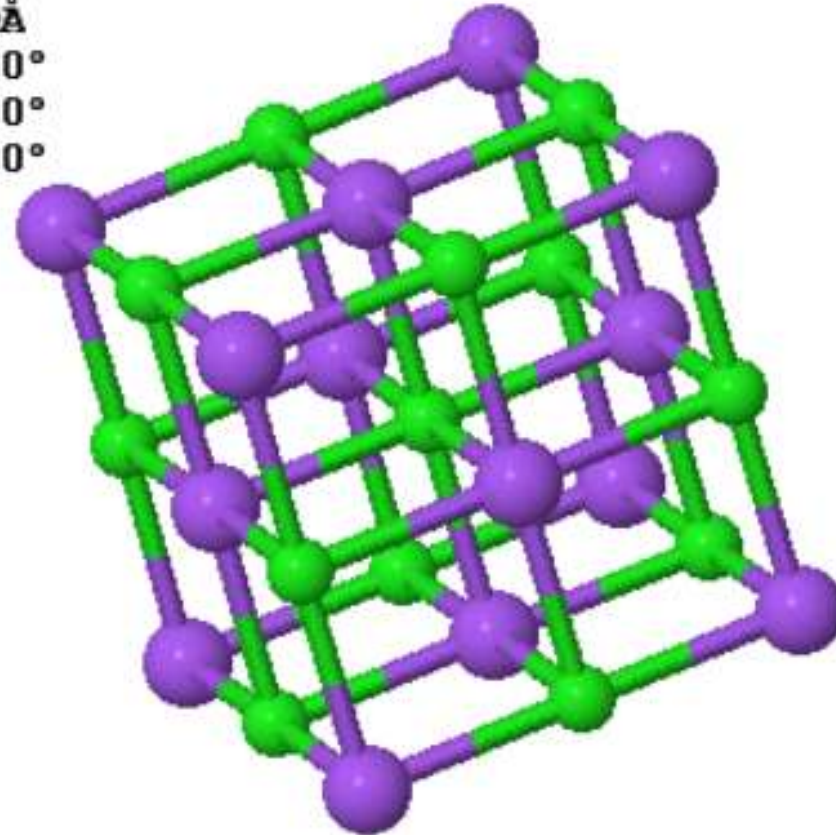


Si(111)



# NaCl

HM:  $Fm\bar{3}m$   
 $a=5.639\text{\AA}$   
 $b=5.639\text{\AA}$   
 $c=5.639\text{\AA}$   
 $\alpha=90.000^\circ$   
 $\beta=90.000^\circ$   
 $\gamma=90.000^\circ$

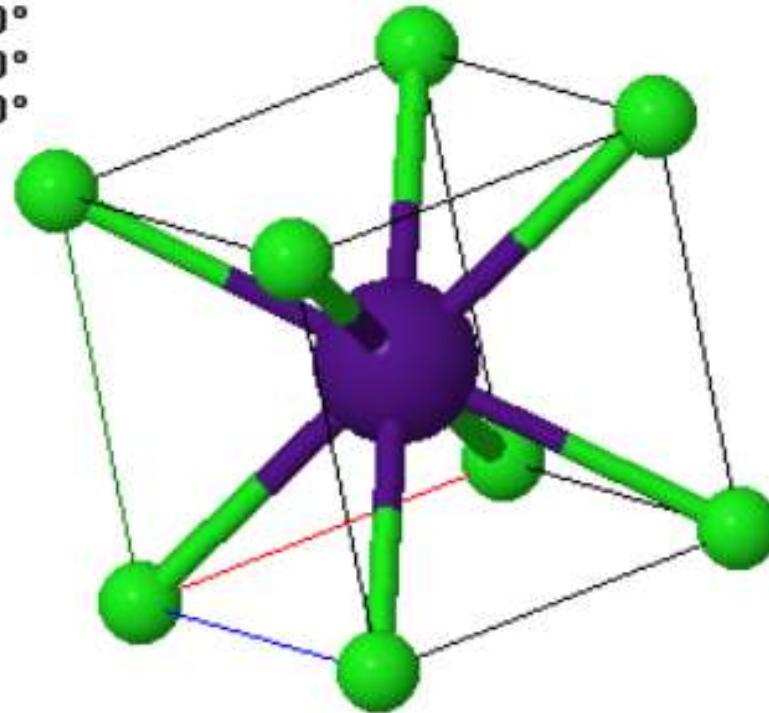


Number 225

Bravais: fcc

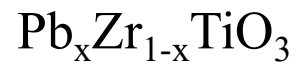
# CsCl

HM: PM-3M  
a=4.110Å  
b=4.110Å  
c=4.110Å  
α=90.000°  
β=90.000°  
γ=90.000°

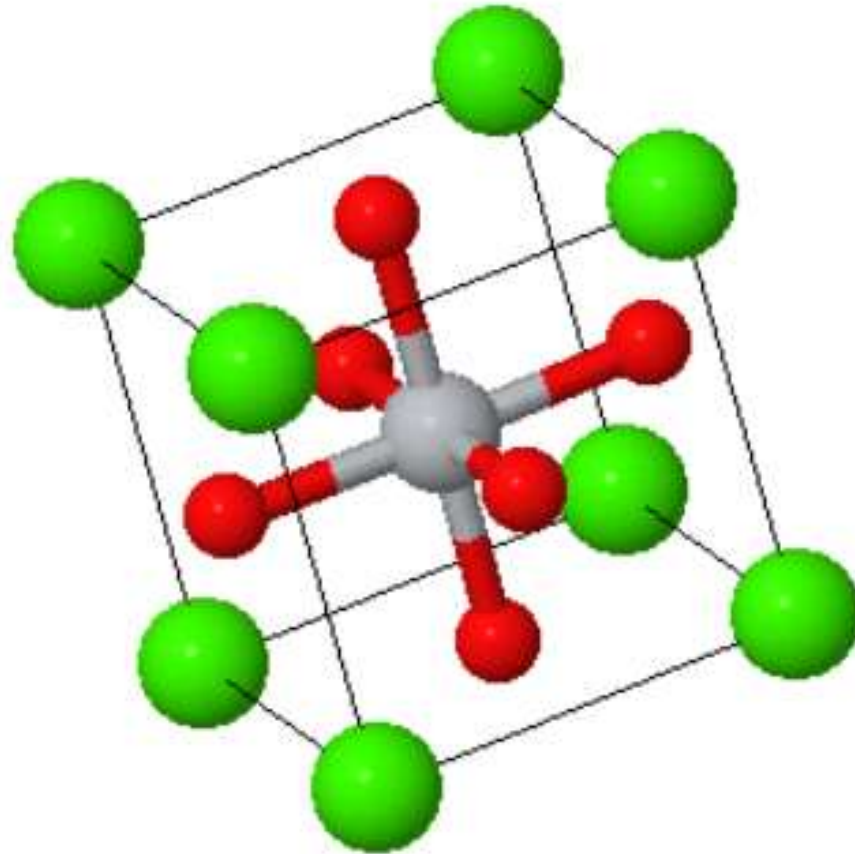


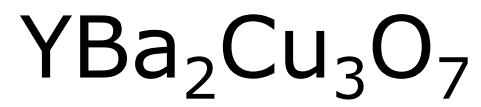
Number 221

# perovskite

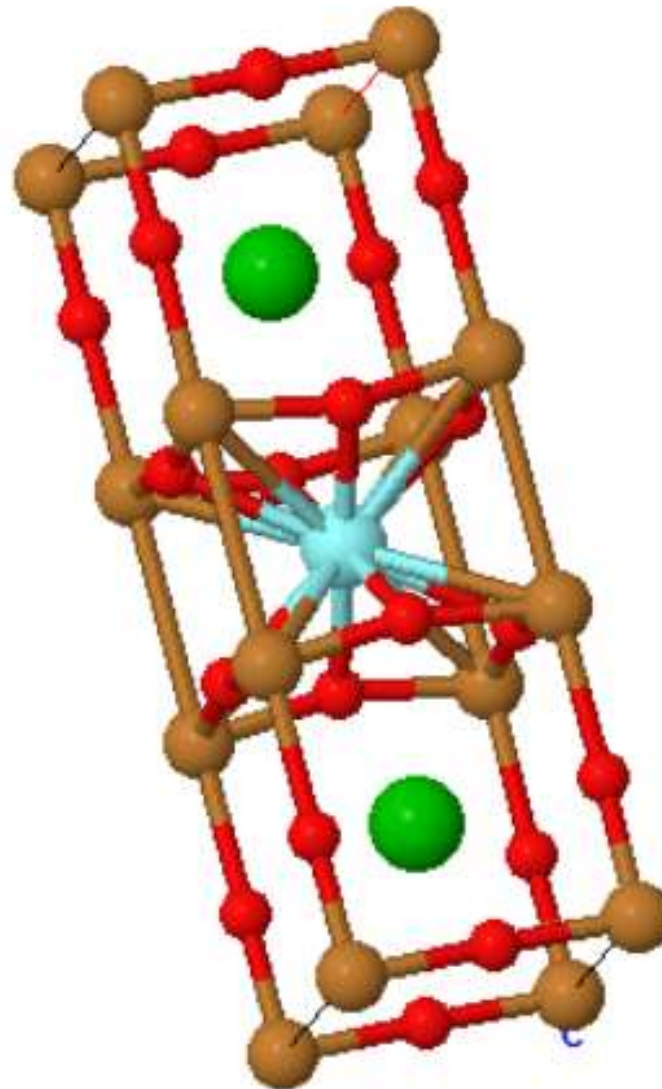


Number 221  
simple cubic





HM: P m m m  
a=3.820Å  
b=3.885Å  
c=11.683Å  
α=90.000°  
β=90.000°  
γ=90.000°



Number 47

# graphite

Space group 194

4 inequivalent C  
atoms in the  
primitive unit cell

**Polytypes of carbon**  
graphite (hexagonal)  
carbon nanotubes  
diamond  
rhombohedral graphite  
hexagonal diamond

HM: P 63 m c  
a=2.456Å  
b=2.456Å  
c=6.696Å  
α=90.000°  
β=90.000°  
γ=120.000°

