

25. Optik

Jan. 21 2019

Parabolspiegel



de.wikipedia.org/wiki/Parabolspiegel

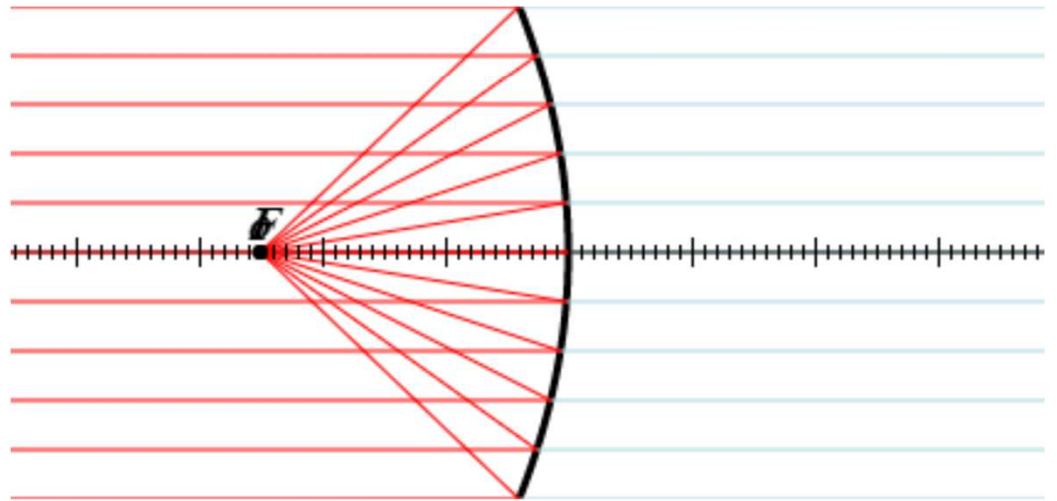
$F =$ [cm]

$x_o =$ [cm]

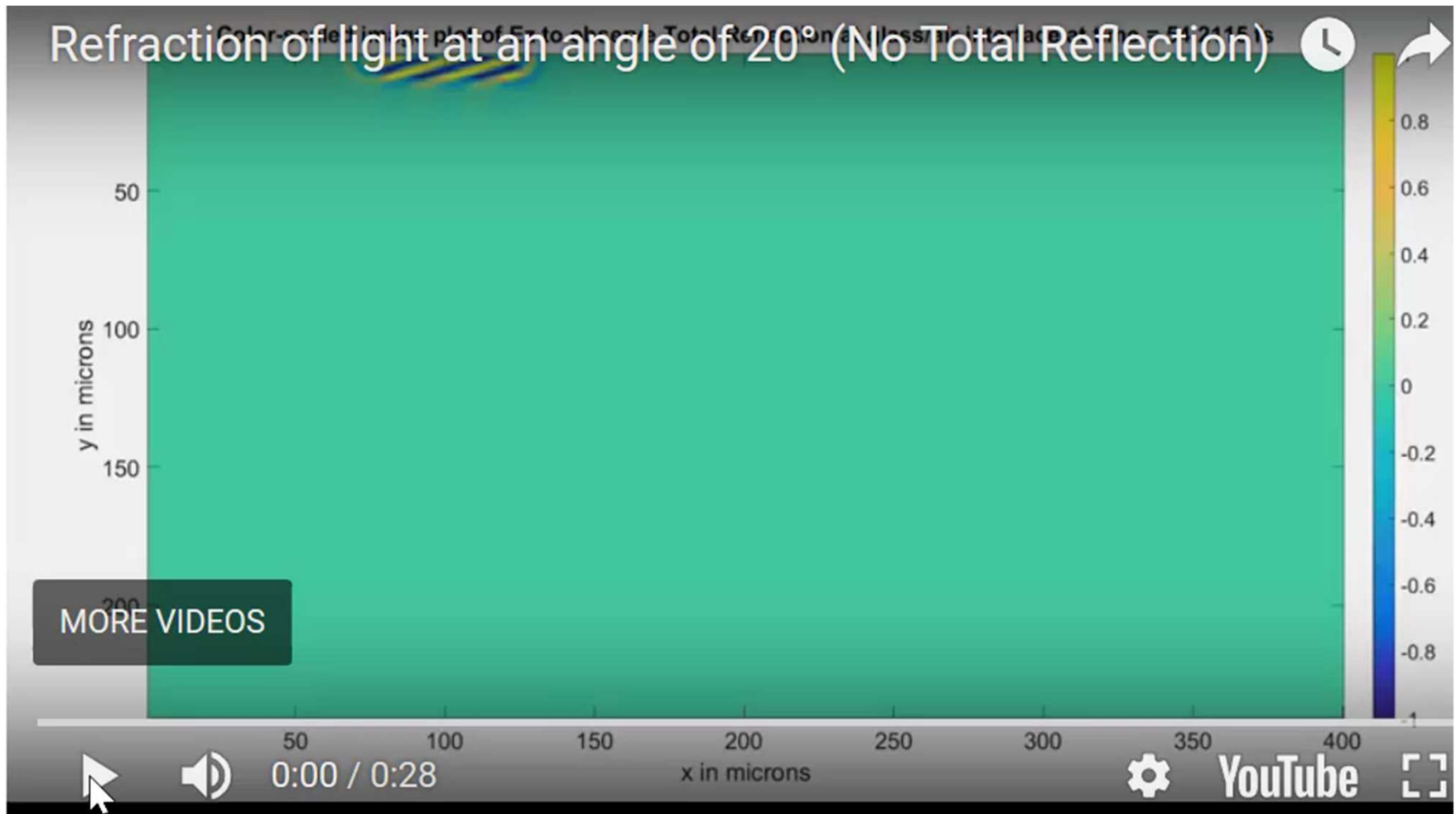
$y_o =$ [cm]

plot

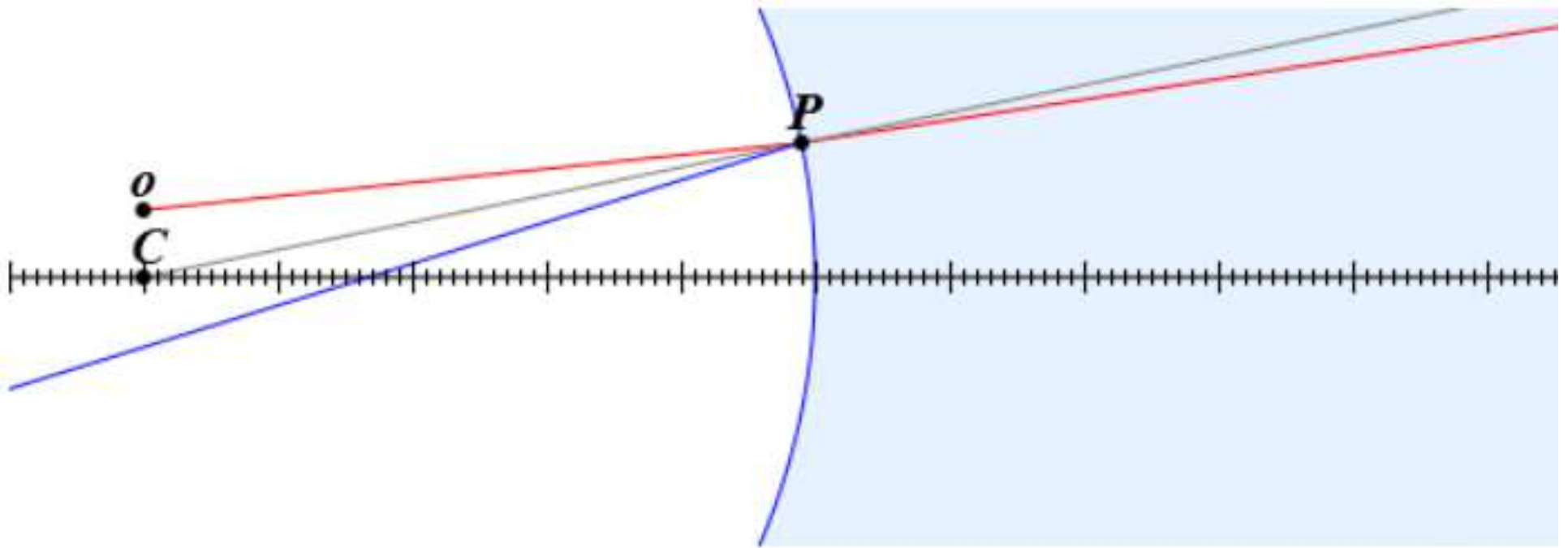
APP:
**Reflection from a
parabolic mirror**



Snelliussches Brechungsgesetz

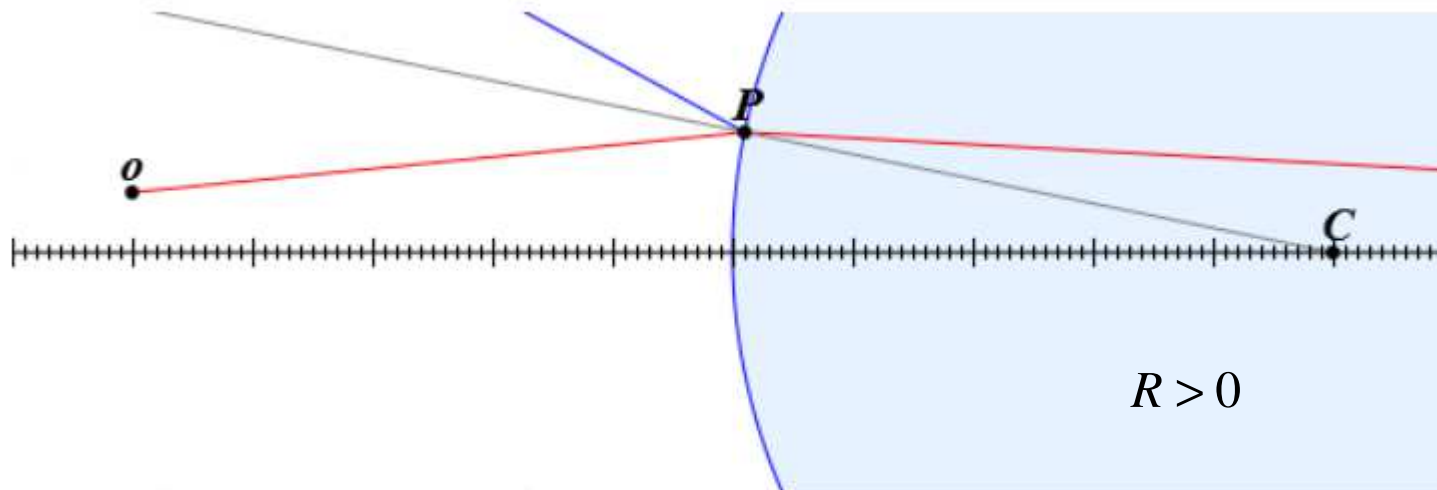
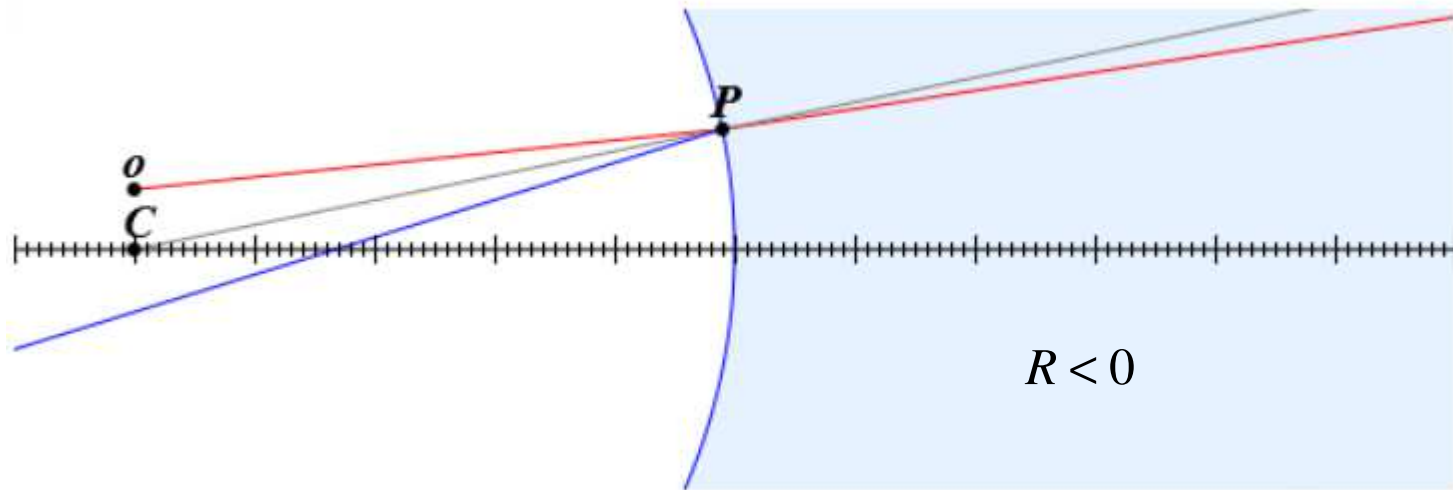


Brechung an einer gekrümmten Grenzfläche



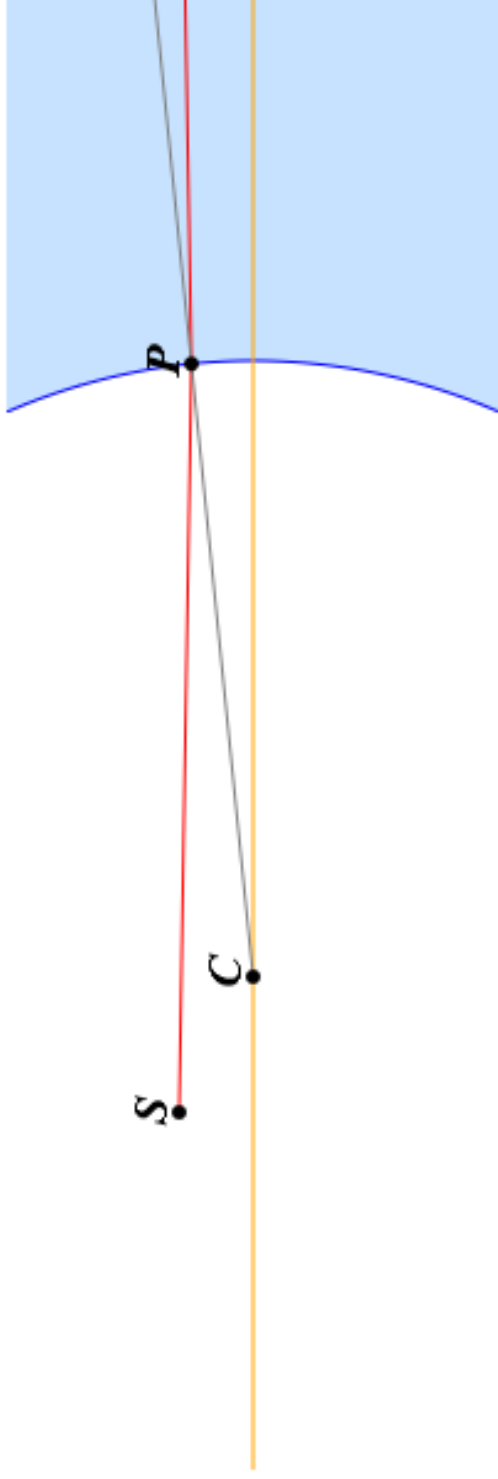
$$R < 0$$

Brechung an einer gekrümmten Grenzfläche



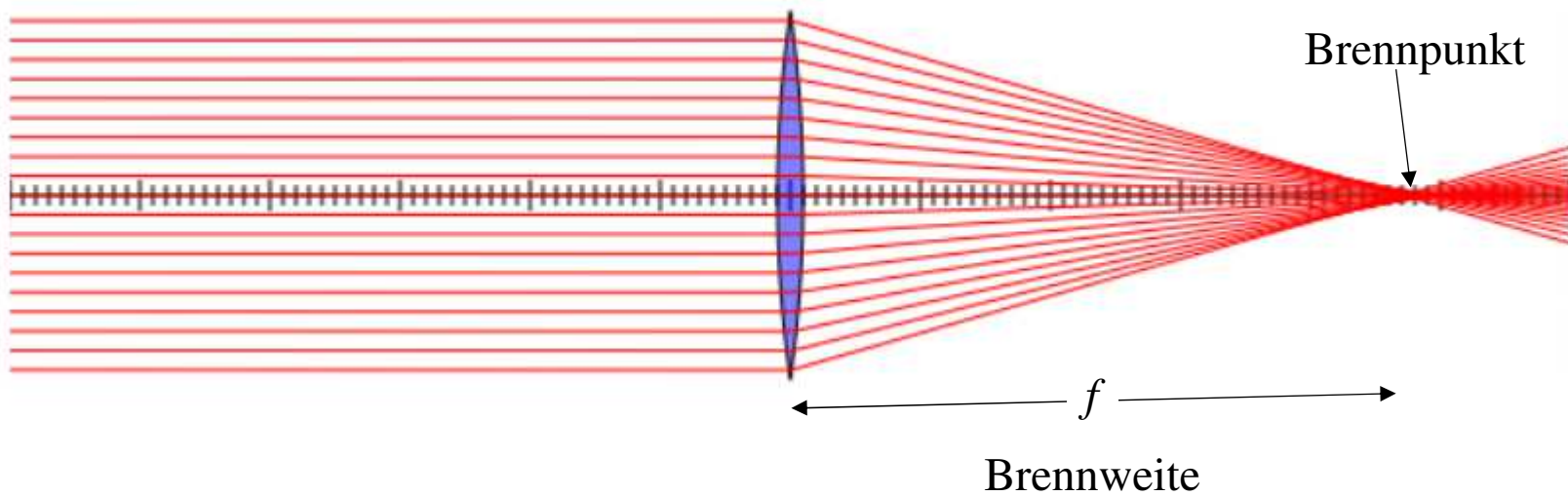
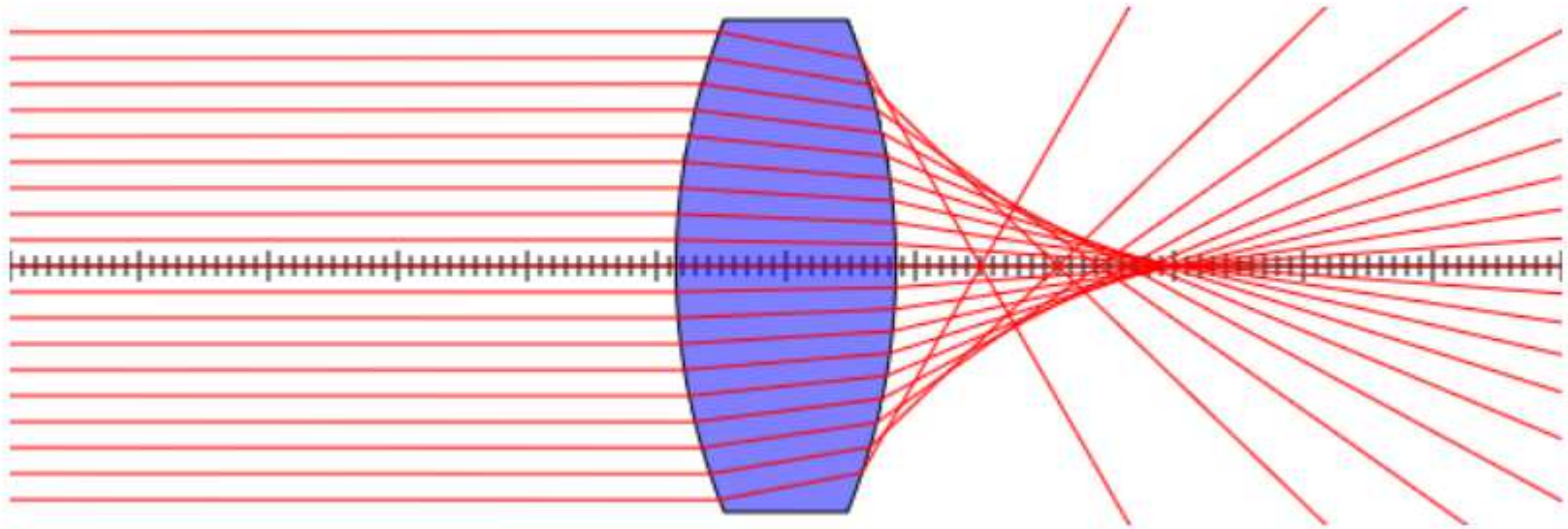
Brechung an einer konkaven Grenzfläche

Eine konkave Grenzfläche sei durch einen Kreis mit dem Radius $R = 5$ cm und dem Mittelpunkt C an $(x_c = 0, y_c = 0)$ gegeben. Ein an der Position S ($x_0 = -1.1, y_0 = 0.60$) cm emittierter Lichtstrahl trifft auf diese Fläche am Punkt P in der Höhe $y_p = 0.50$ cm. Der Brechungsindex ist $n_1 = 1$ links und $n_2 = 1.4$ rechts der Grenzfläche. Wie groß ist der Winkel, welcher von der Normalen auf die Grenzfläche am Punkt P (die C und P verbindende graue Linie) und dem gebrochenen Strahl eingeschlossen wird?

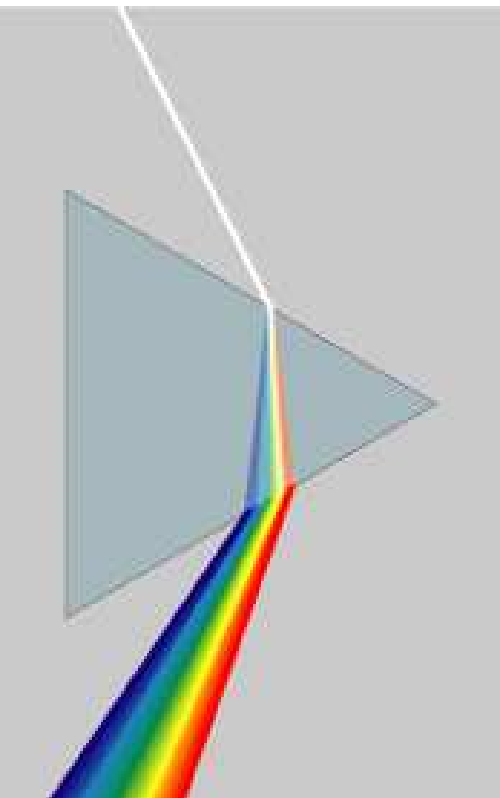


Lösung

Sphärische Aberration



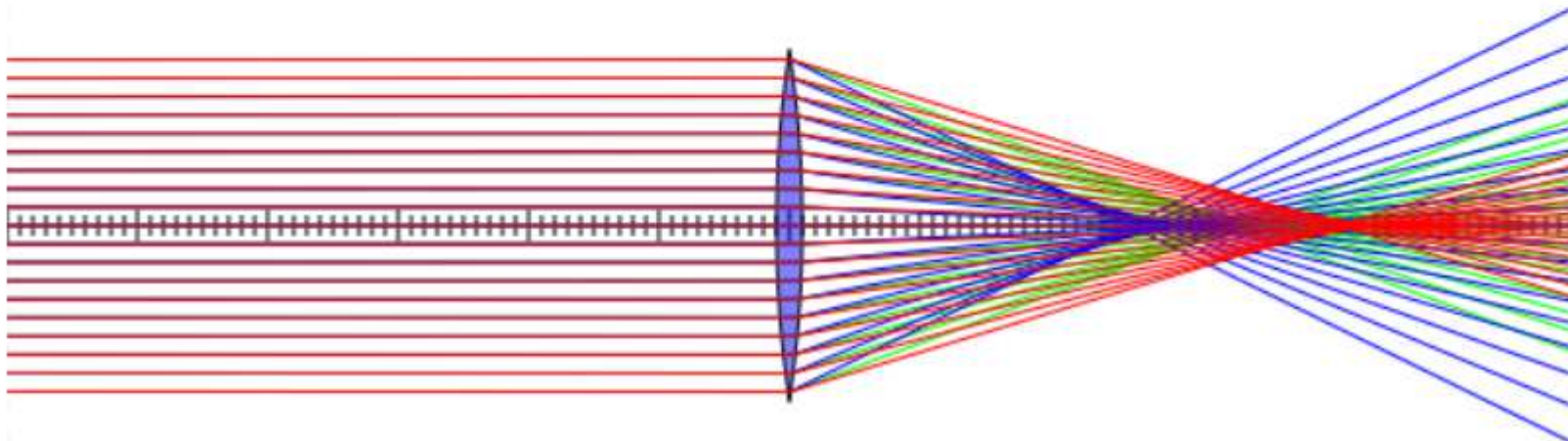
Dispersion



$n(\lambda)$
Brechungsindex

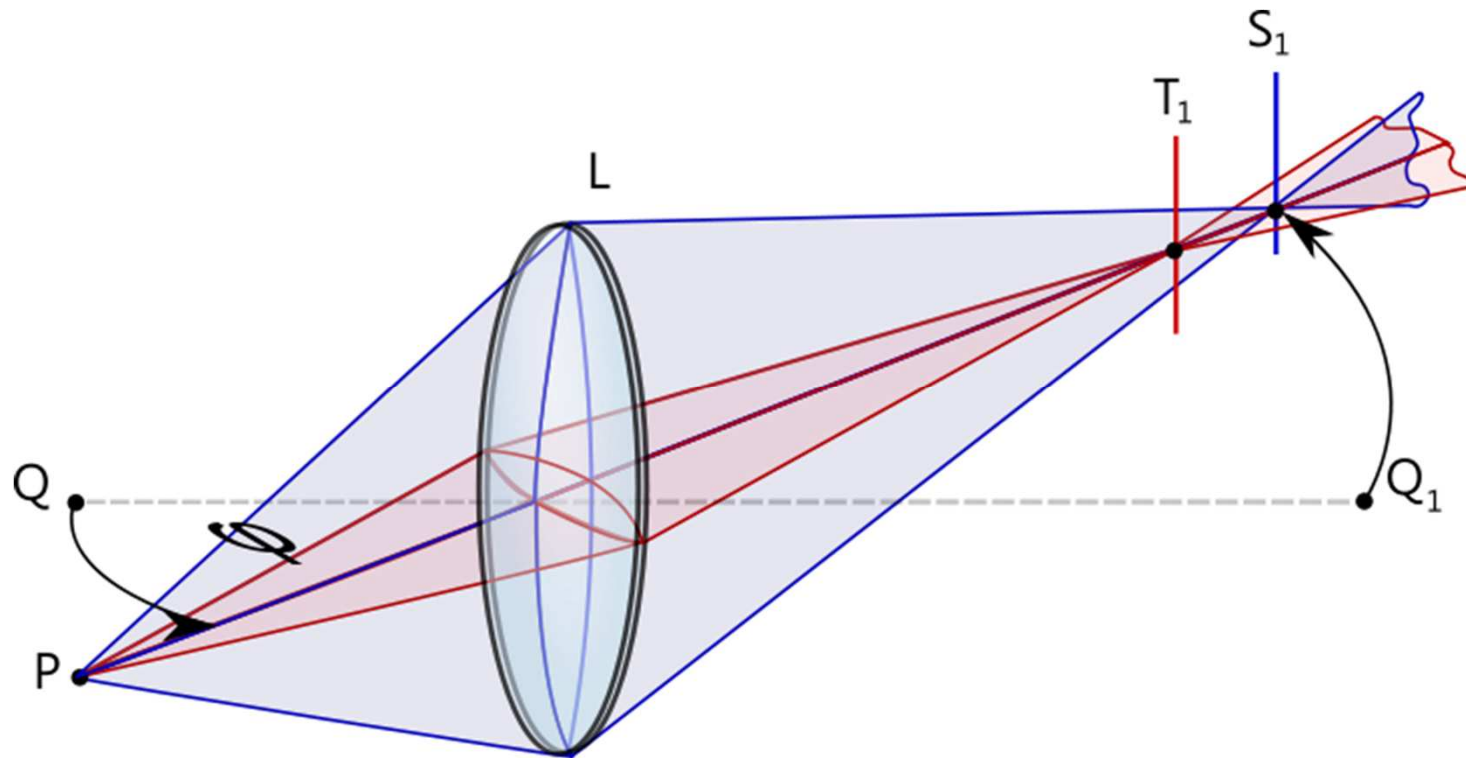
Chromatische Aberration

	Rot	Grün	Blau
$n_{\text{Umg}} =$	<input type="text" value="1"/>	<input type="text" value="1"/>	<input type="text" value="1"/>
$n_{\text{Linse}} =$	<input type="text" value="2"/>	<input type="text" value="2.2"/>	<input type="text" value="2.5"/>
show:	<input checked="" type="checkbox"/> Rot	<input checked="" type="checkbox"/> Grün	<input checked="" type="checkbox"/> Blau
	<input type="button" value="plot"/>		



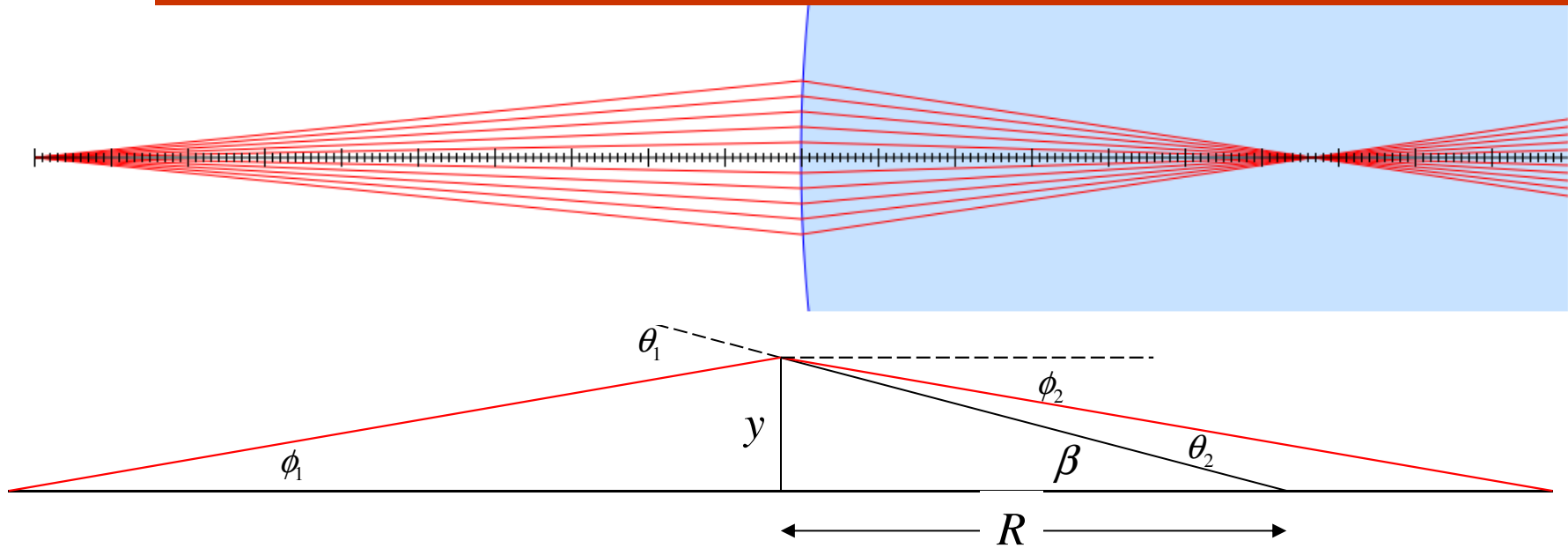
Astigmatismus

Die Brechung hängt von der Einfallsebene ab.



<https://en.wikipedia.org/wiki/Astigmatism#/media/File:Astigmatism.svg>

kleine Winkel zur optischen Achse



$$n_1 \sin \theta_1 = n_2 \sin \theta_2$$

$$\downarrow$$
$$n_1 \theta_1 \approx n_2 \theta_2$$

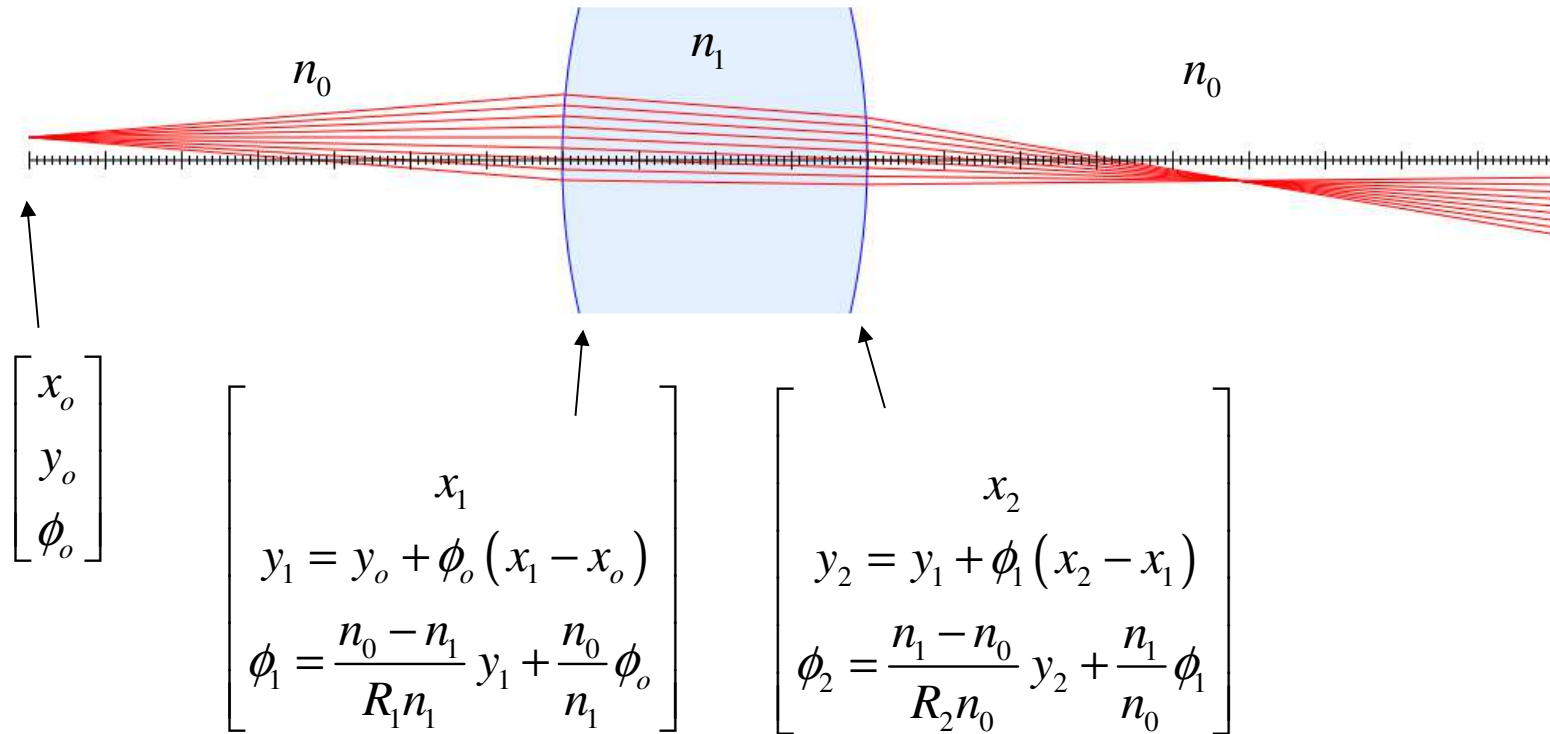
$$\theta_1 = \phi_1 + \beta$$

$$-\phi_2 + \theta_2 = \beta$$

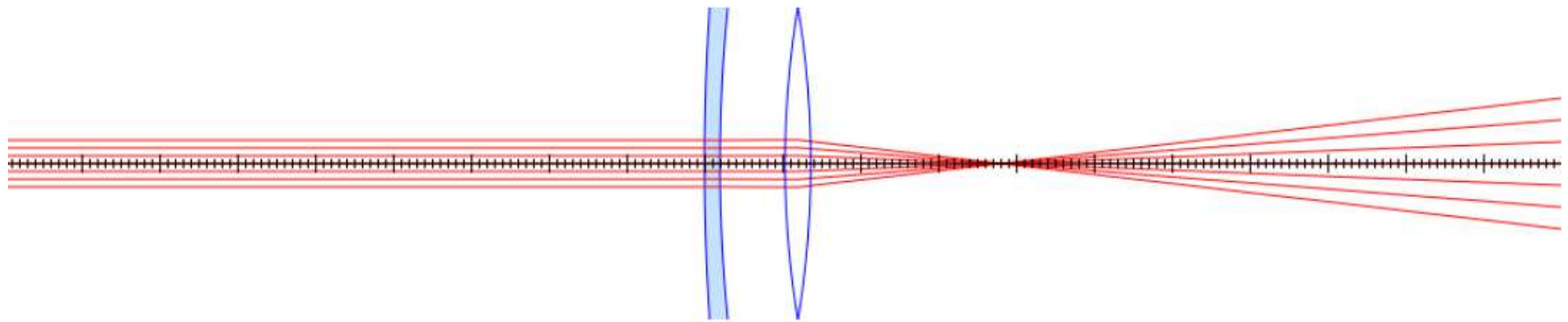
$$\beta \approx \frac{y}{R}$$

$$\phi_2 = \frac{n_1 - n_2}{n_2 R} y + \frac{n_1}{n_2} \phi_1$$

Linse (kleine Winkel)



Ray tracing mittels Transfermatrixmethode



Zeichne optisches System

Brechung an planarer Grenzfläche

Brechung an konvexer Grenzfläche

Brechung an konkaver Grenzfläche

Bikonvexlinse

Bikonkavlinse

Linsensystem

Brille - Auge

Kondensorlinse

Immersionlinse

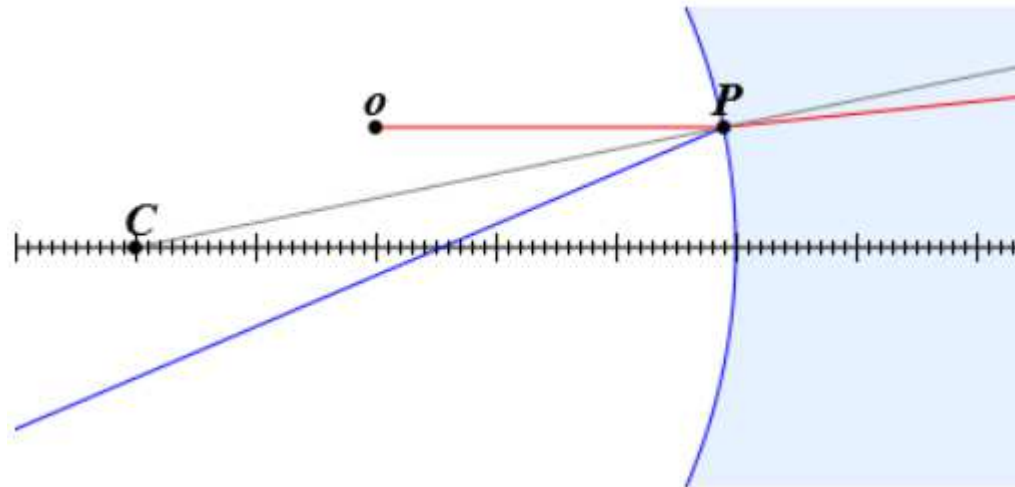
zwischen Grenzflächen

$$y_{i+1} = y_i + \phi_i (x_{i+1} - x_i)$$

bei Grenzfläche

$$\phi_{i+1} = \frac{n_1 - n_2}{n_2 R} y_i + \frac{n_1}{n_2} \phi_i$$

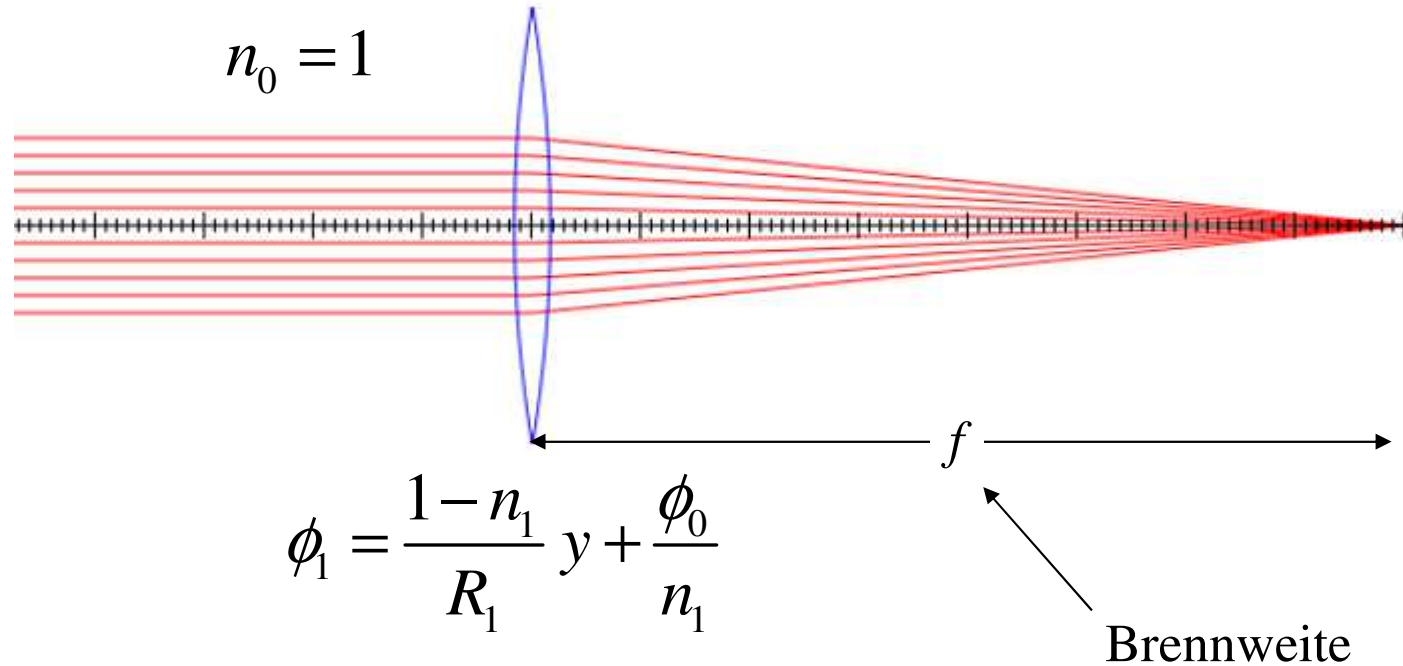
Brechung



Methode 1: mit Vektoren $n_1 \sin \theta_1 = n_2 \sin \theta_2$

Methode 2: kleinen Winkeln zur optischen Achse $\phi_{i+1} = \frac{n_1 - n_2}{n_2 R} y_i + \frac{n_1}{n_2} \phi_i$

dünne Linsen (kleine Winkel)



$$\phi_1 = \frac{1-n_1}{R_1} y + \frac{\phi_0}{n_1}$$

$$\phi_2 = \frac{n_1-1}{R_2} y + n_1 \left(\frac{1-n_1}{R_1} y + \frac{\phi_0}{n_1} \right)$$

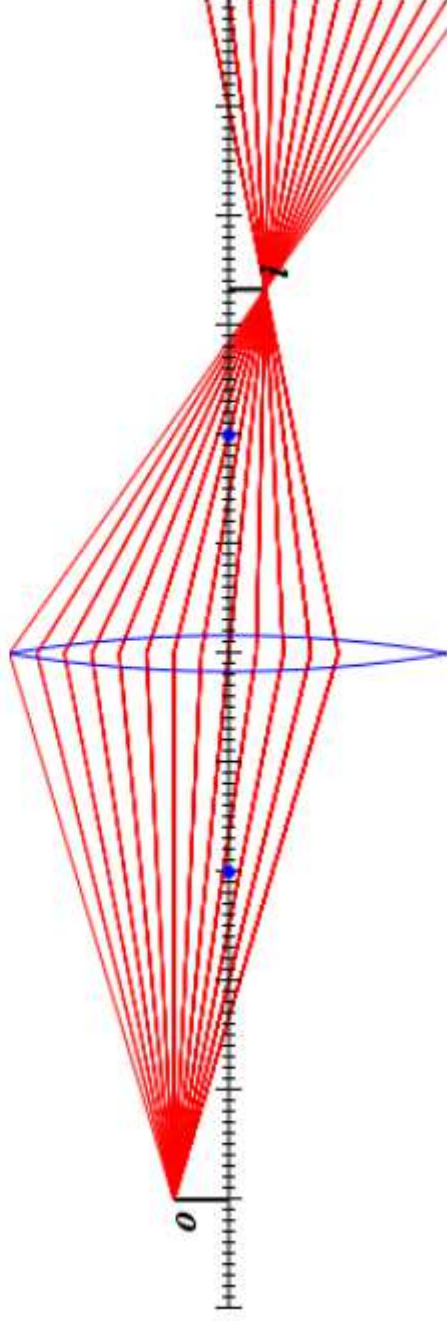
$$\phi_{i+1} = -\frac{y_i}{f} + \phi_i$$

$$\frac{1}{f} = (n_1 - 1) \left(\frac{1}{R_1} - \frac{1}{R_2} \right)$$

Abbildungsgleichung für dünne Linsen

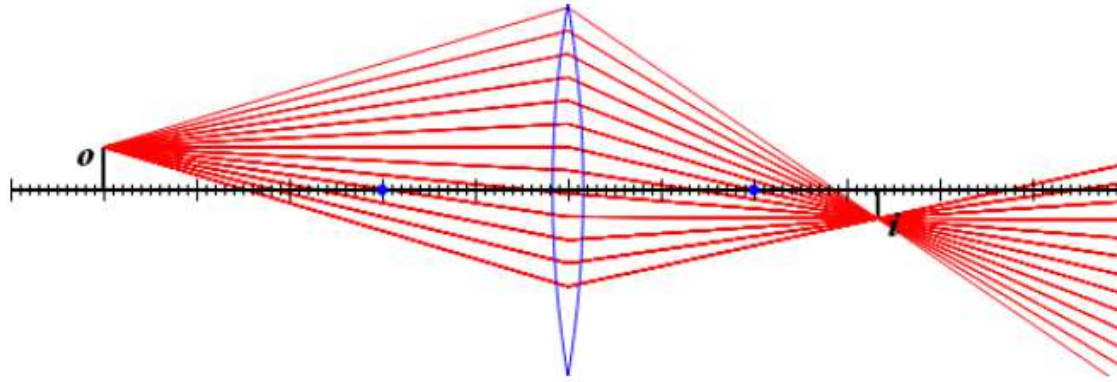
$f =$	<input type="text" value="2"/>	[cm]	<input type="range" value="2"/>
$x_o =$	<input type="text" value="-5"/>	[cm]	<input type="range" value="-5"/>
$y_o =$	<input type="text" value="0.5"/>	[cm]	<input type="range" value="0.5"/>
$x_i =$	<input type="text" value="3.33333"/>	[cm]	$D =$ <input type="text" value="50.0000"/> [m ⁻¹]
$y_i =$	<input type="text" value="-0.333333"/>	[cm]	$m =$ <input type="text" value="-0.6666667"/>

plot



$$-\frac{1}{x_o} + \frac{1}{x_i} = \frac{1}{f}$$

Abbildungsgleichung für dünne Linsen



$$x_i = \frac{fx_o}{f + x_o}$$



$$\frac{1}{x_i} - \frac{1}{x_o} = \frac{1}{f}$$

$$y_i = y_o \left(\frac{f}{f + x_o} \right)$$

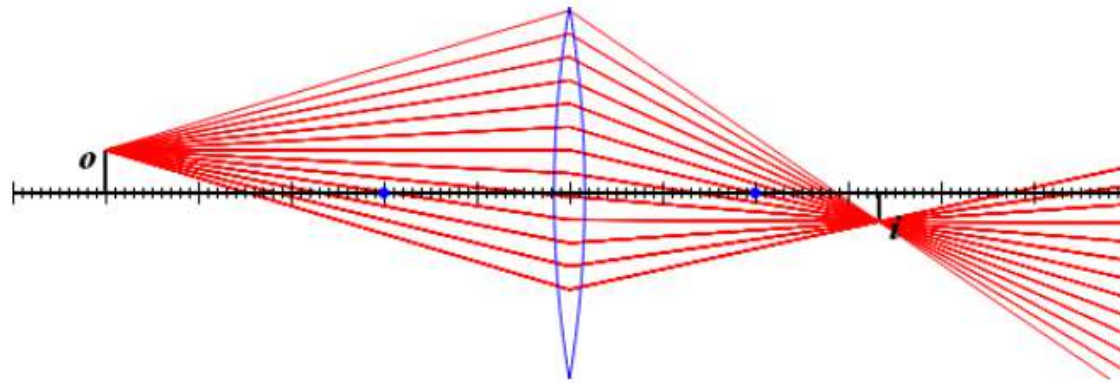


$$m = \frac{y_i}{y_o} = \left(\frac{f}{f + x_o} \right)$$

dünne Linsen

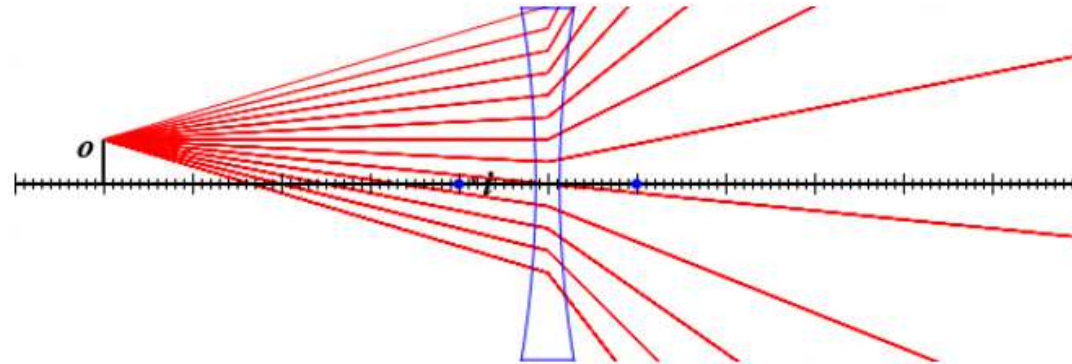
Sammellinse

$$f > 0$$



Zerstreuungslinse

$$f < 0$$

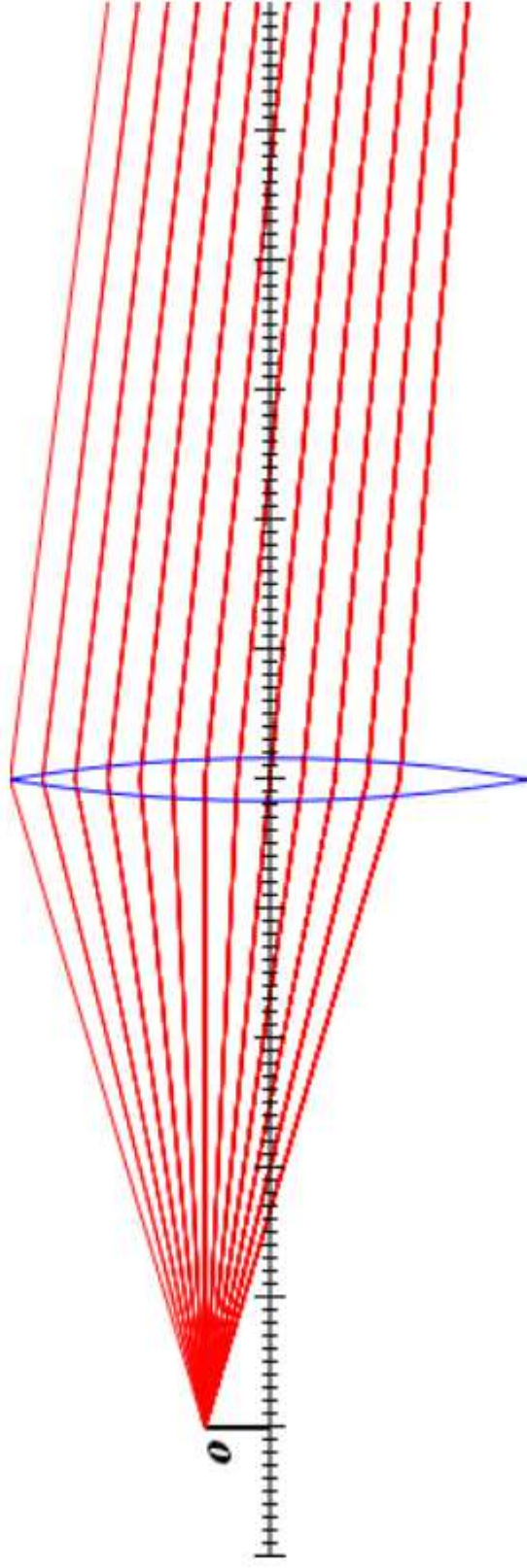


Brennweite

$x_o =$ [cm]

$y_o =$ [cm]

$x_i =$ [cm]



Wie groß ist die Brennweite dieser Linse (in cm, gerundet auf die erste Nachkommastelle)?

$f =$

Reelle und virtuelle Bilder

$f = 1$ [cm]

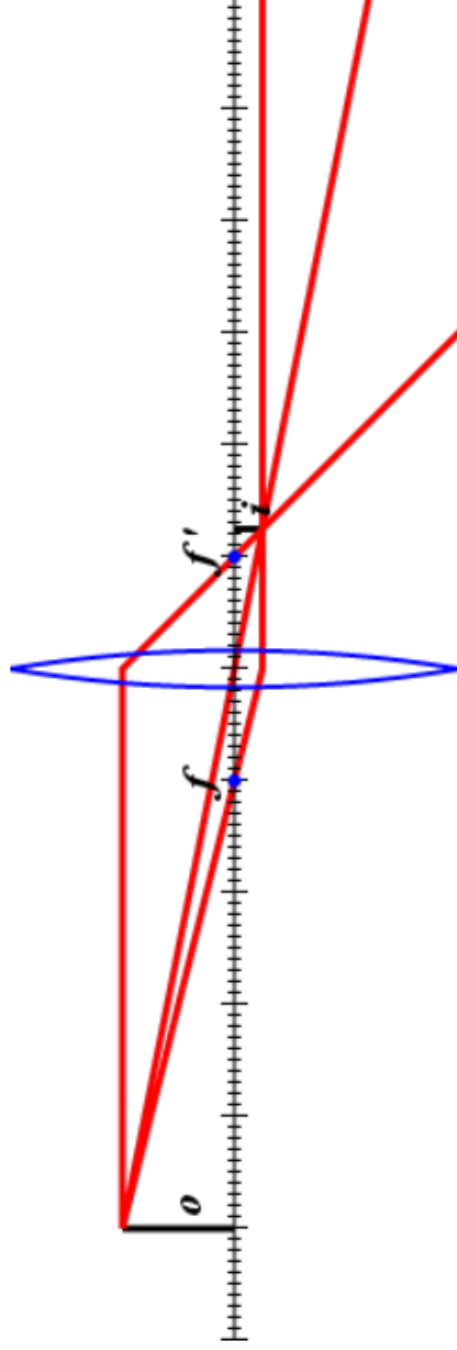
$x_o = -5$ [cm]

$y_o = 1$ [cm]

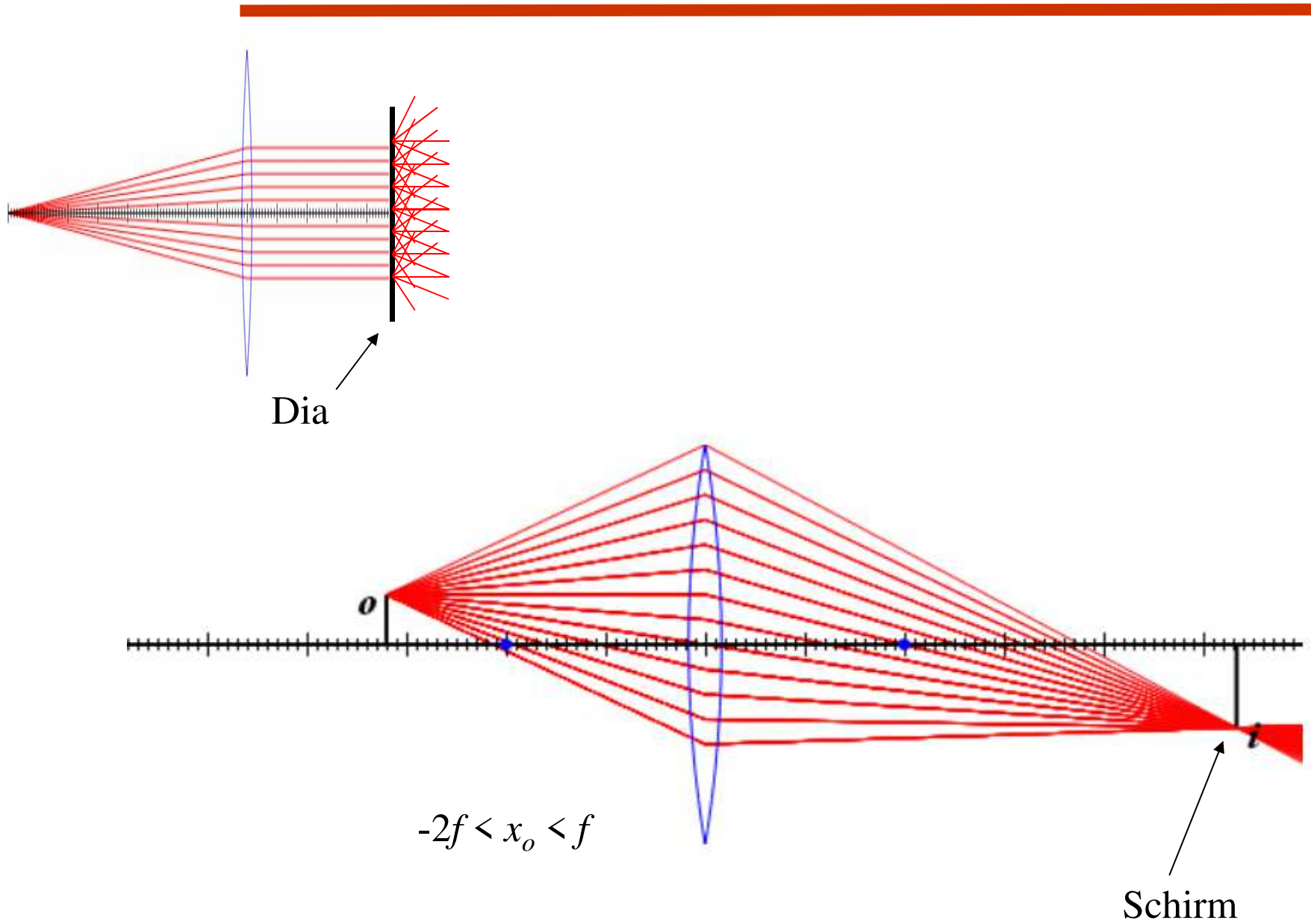
$x_i = 1.25000$ [cm] $D = 100.000$ [m⁻¹]

$y_i = -0.250000$ [cm] $m = -0.250000$

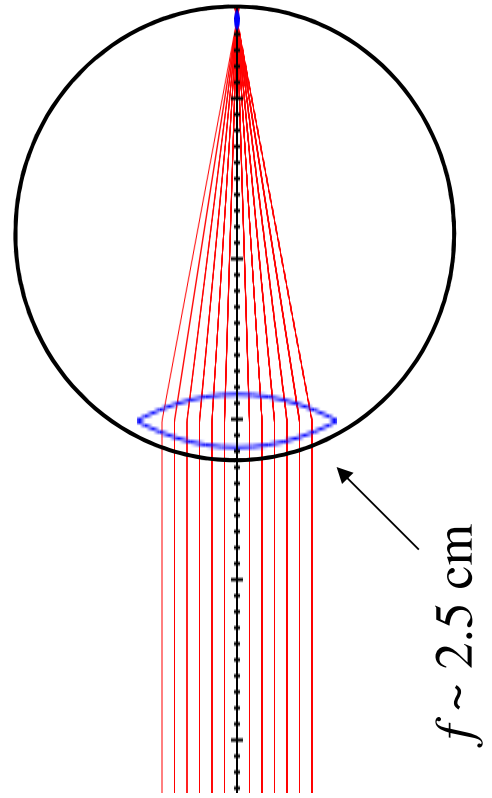
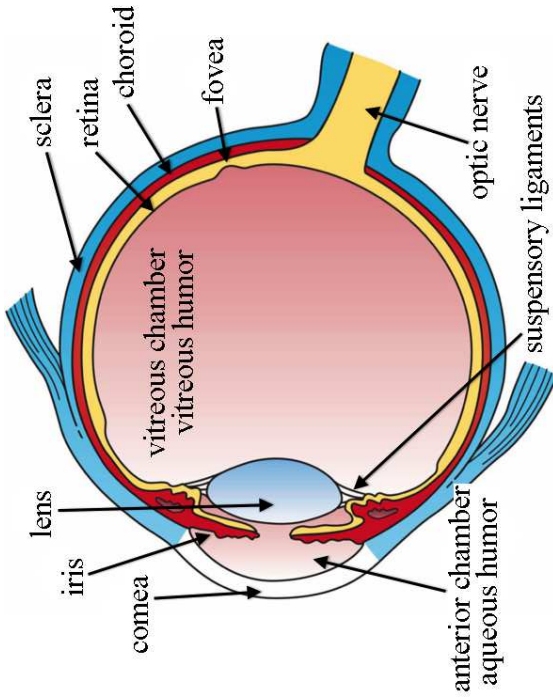
The image is real and inverted.



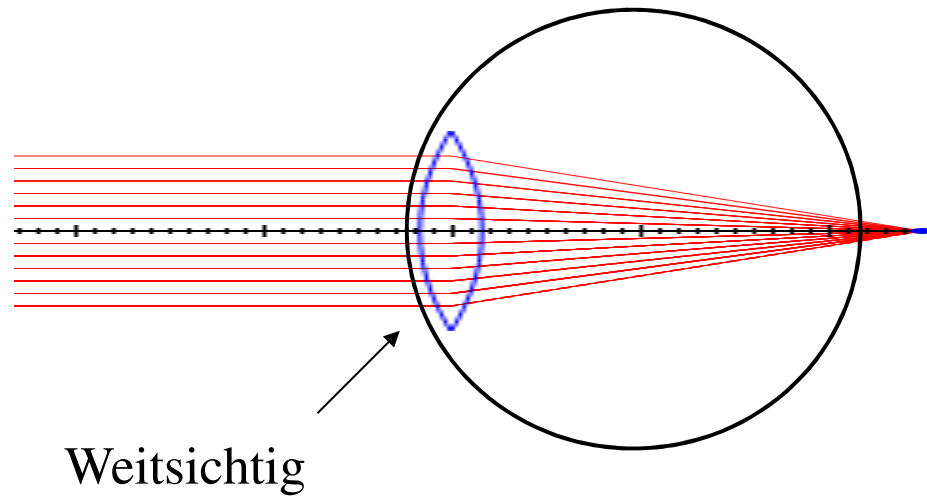
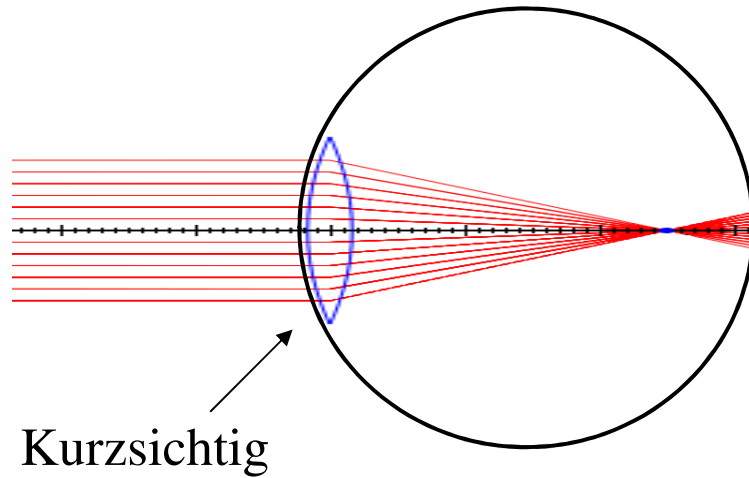
Diaprojektor



Auge

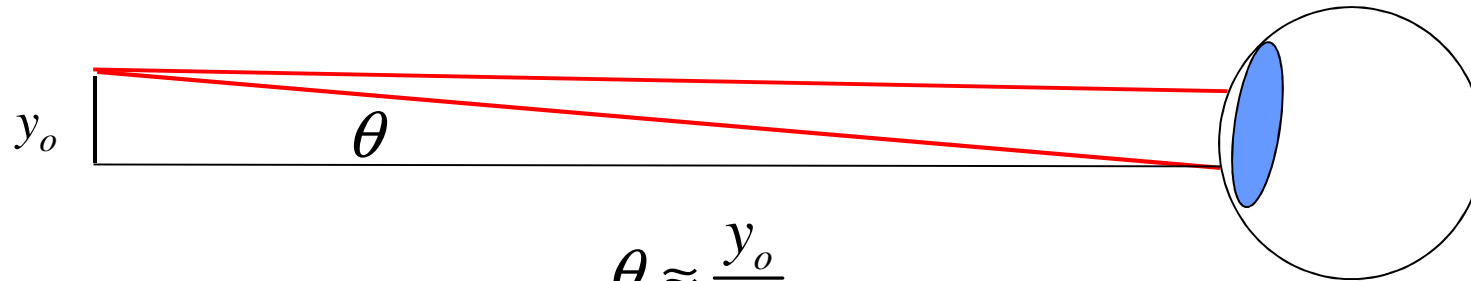


Auge

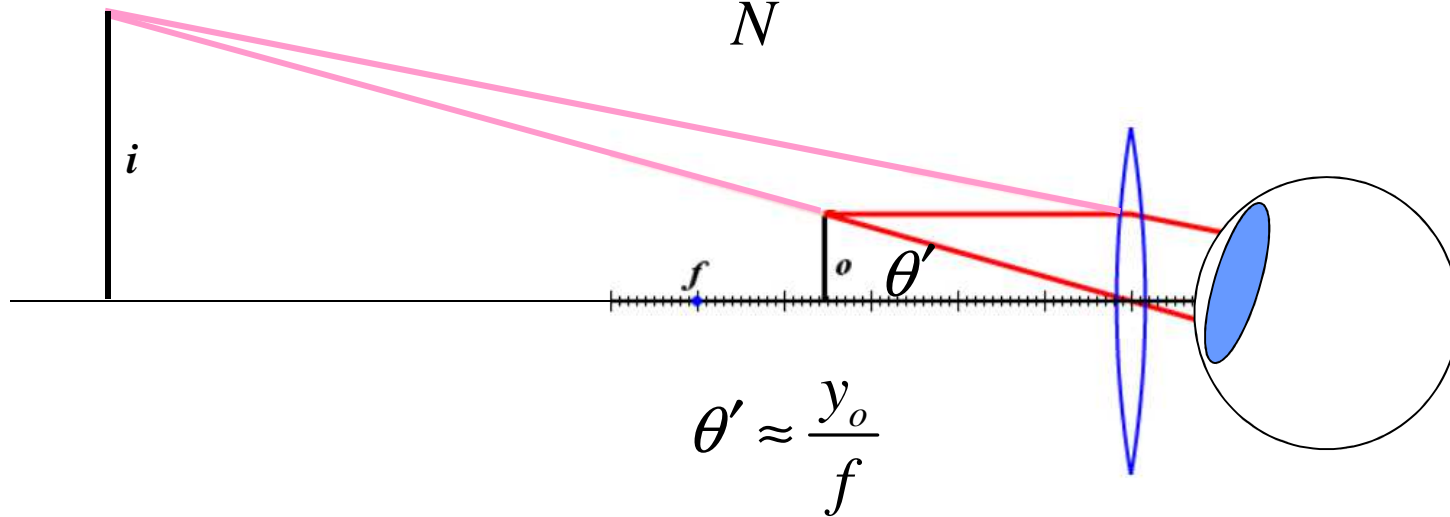


Lupe

Nahpunkt $N \sim 25 \text{ cm}$



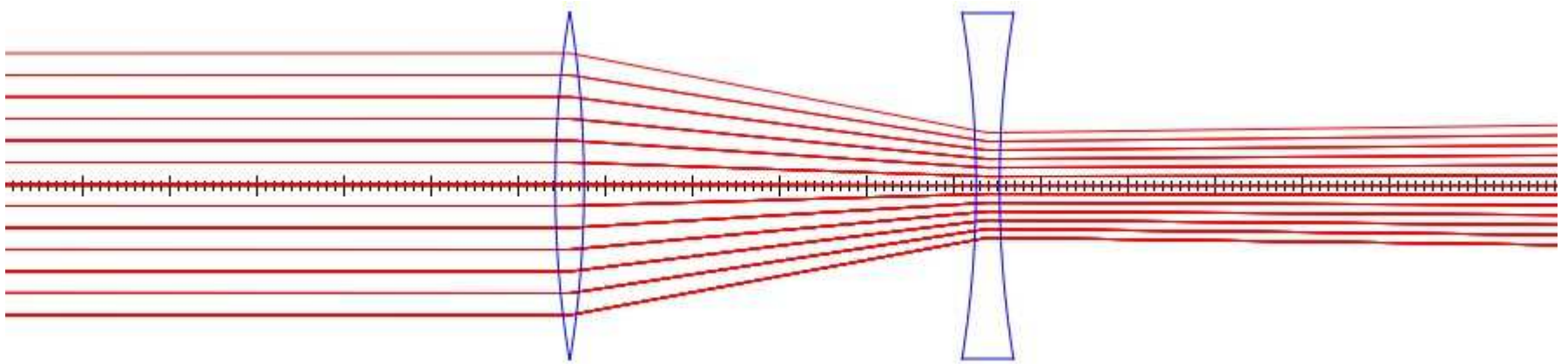
$$\theta \approx \frac{y_o}{N}$$



$$\theta' \approx \frac{y_o}{f}$$

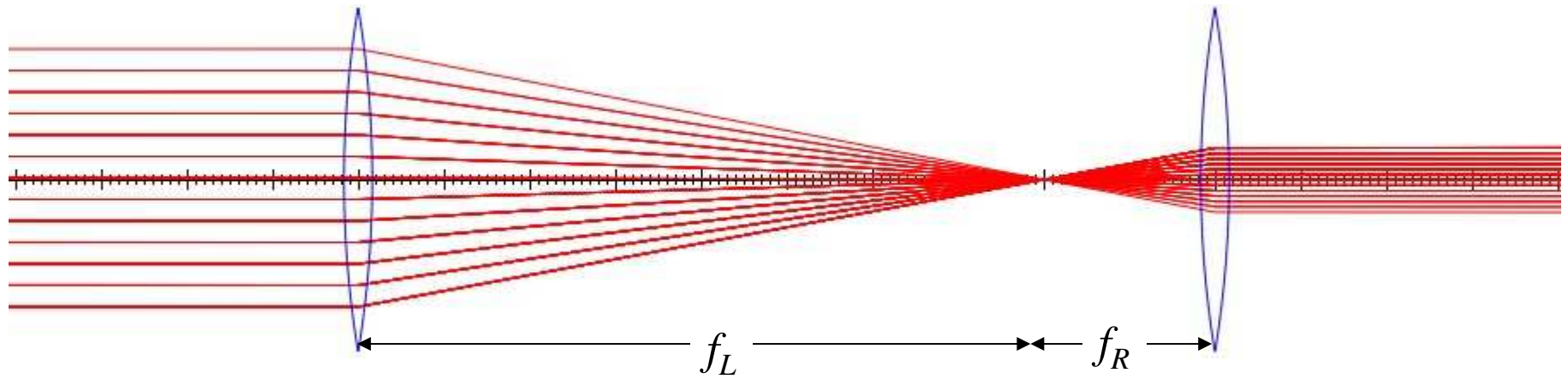
Vergrößerung $m \sim N/f$

Galilei'sches Teleskop



$$m = \frac{\theta_i}{\theta_o} = \frac{y_i x_o}{y_o x_i}$$

Keplersches Teleskop



$$m = \frac{\theta_i}{\theta_o} = \frac{y_i x_o}{y_o x_i}$$

Mikroskop

