

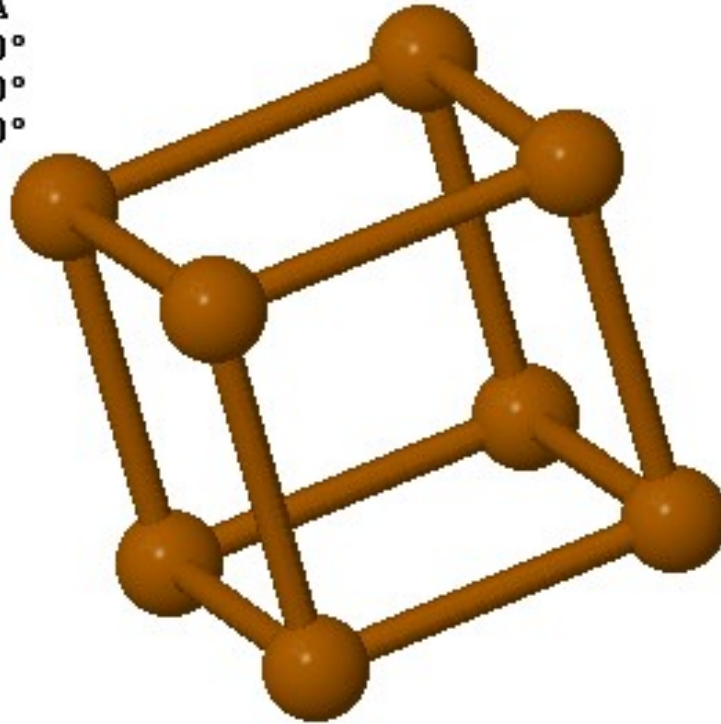
# Crystal structure

---

# simple cubic

Po

HM: P m  $\bar{3}$  m  
a=3.359Å  
b=3.359Å  
c=3.359Å  
 $\alpha=90.000^\circ$   
 $\beta=90.000^\circ$   
 $\gamma=90.000^\circ$



Number: 221

Primitive Vectors:

$$\vec{a}_1 = a\hat{x}$$

$$\vec{a}_2 = a\hat{y}$$

$$\vec{a}_3 = a\hat{z}$$

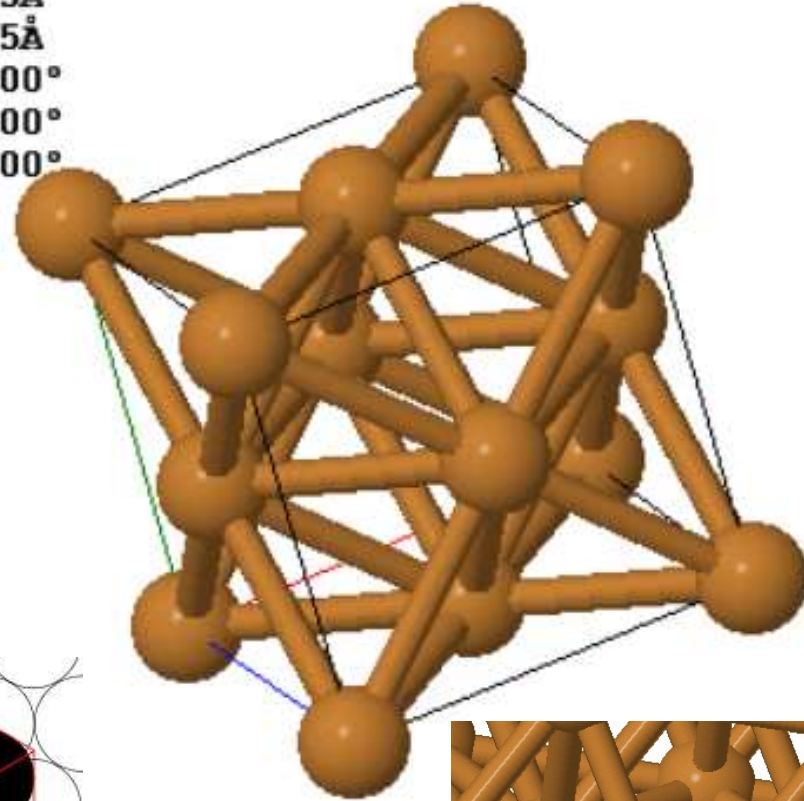
Basis Vector:  $\vec{B}_1 = (0, 0, 0)$

# fcc

Number 225

Al, Cu,  
Ni, Sr,  
Rh, Pd,  
Ag, Ce,  
Tb, Ir,  
Pt, Au,  
Pb, Th

HM:  $F m \bar{3} m$   
 $a=3.615\text{\AA}$   
 $b=3.615\text{\AA}$   
 $c=3.615\text{\AA}$   
 $\alpha=90.000^\circ$   
 $\beta=90.000^\circ$   
 $\gamma=90.000^\circ$



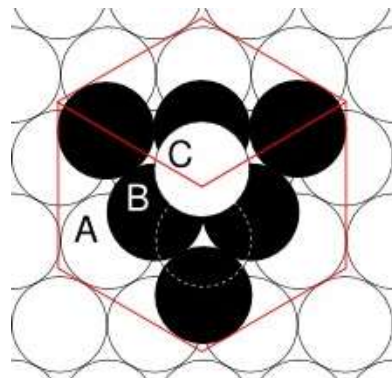
[111]

Primitive Vectors:

$$\vec{a}_1 = \frac{a}{2} \hat{y} + \frac{a}{2} \hat{z}$$

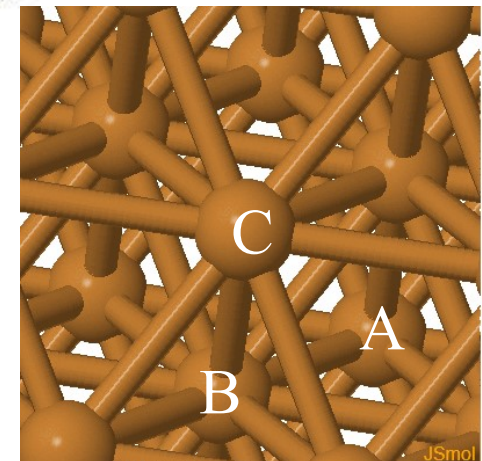
$$\vec{a}_2 = \frac{a}{2} \hat{x} + \frac{a}{2} \hat{z}$$

$$\vec{a}_3 = \frac{a}{2} \hat{x} + \frac{a}{2} \hat{y}$$



Basis Vector:

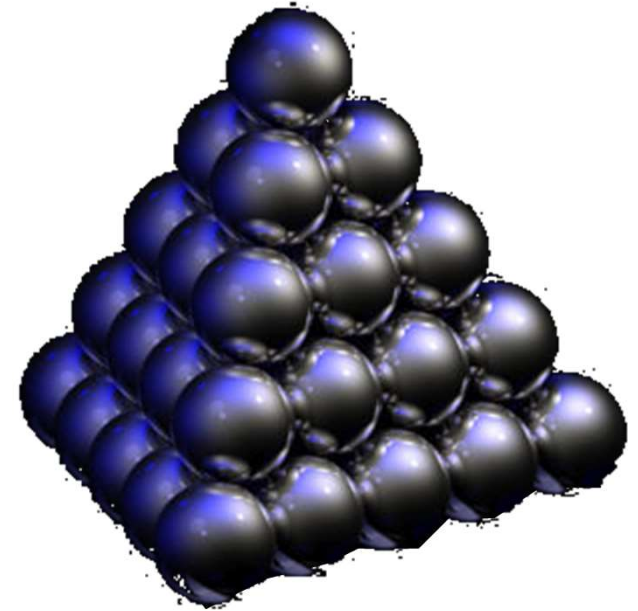
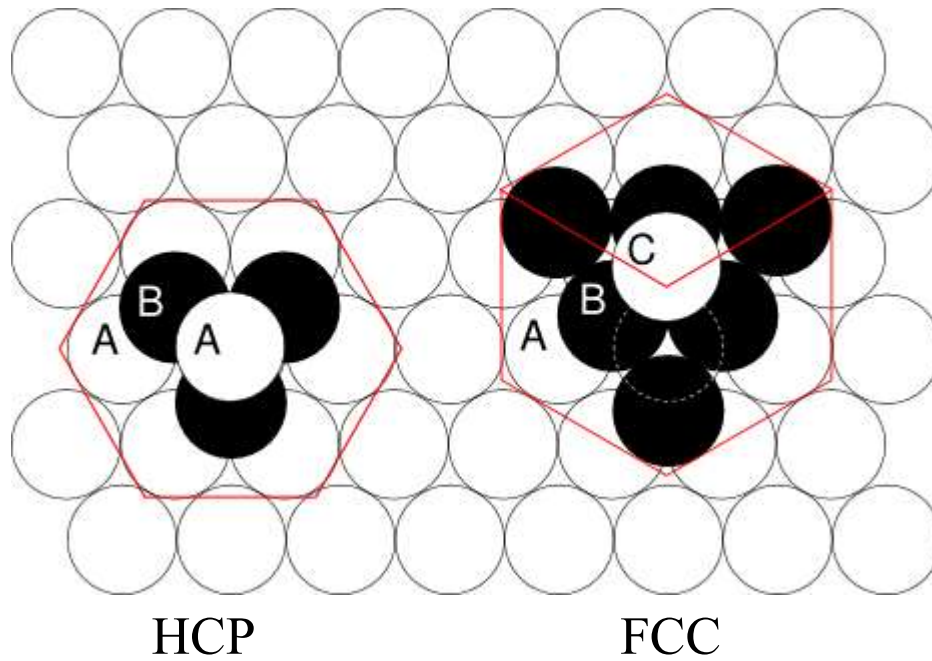
$$\vec{B}_1 = (0, 0, 0)$$



JSmol

# Close packing

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HCP = Hexagonal close pack

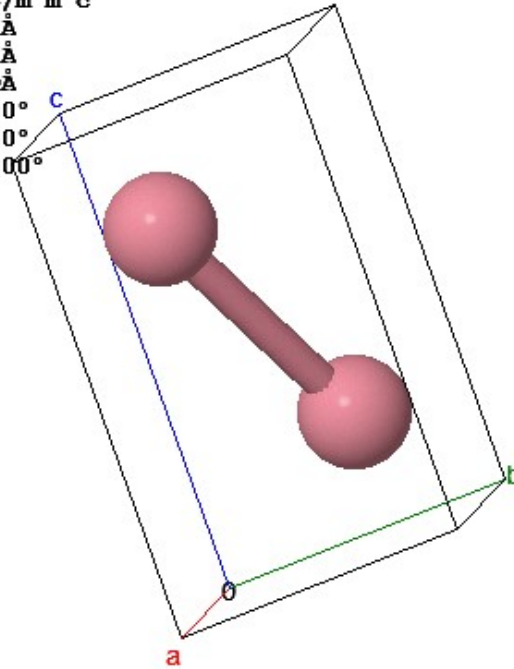
Hexagonal Bravais lattice with two atoms in the basis.

# hcp

Space group 194 Crystallographic unit cell

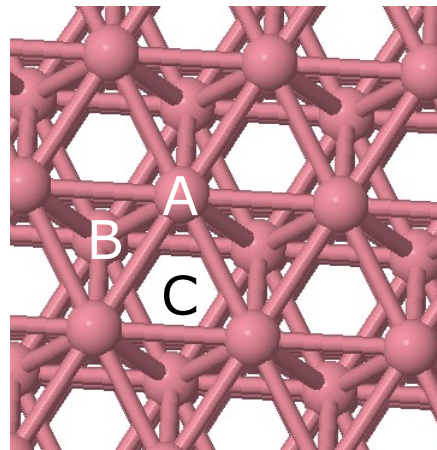
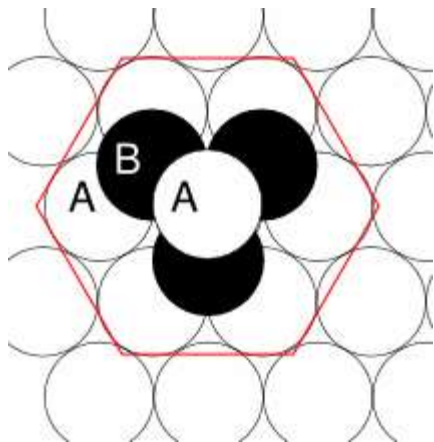
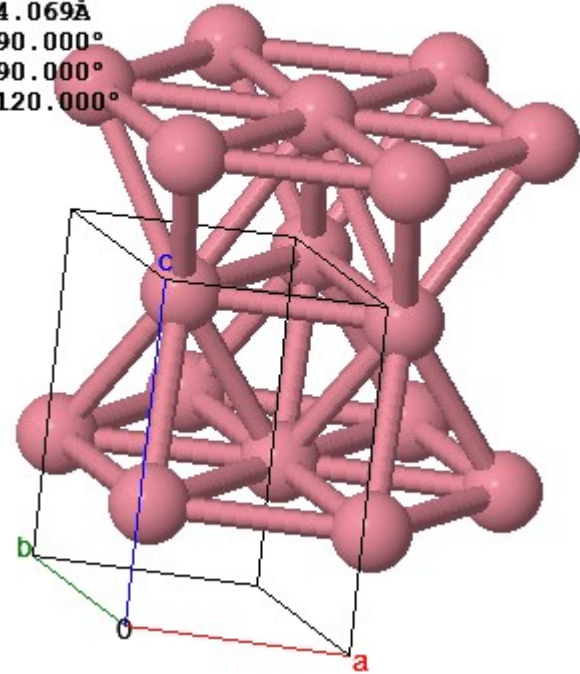
Mg, Be,  
Sc, Ti,  
Co, Zn,  
Y, Zr, Tc,  
Ru, Cd,  
Gd, Tb,  
Dy, Ho,  
Er, Tm,  
Lu, Hf,  
Re, Os,  
Tl

HM: P 63/m m c  
a=2.507Å  
b=2.507Å  
c=4.069Å  
α=90.000°  
β=90.000°  
γ=120.000°



## Hexagonal unit cell

HM: P 63/m m c  
a=2.507Å  
b=2.507Å  
c=4.069Å  
α=90.000°  
β=90.000°  
γ=120.000°



Hexagonal Bravais lattice  
Basis vectors:

$$\vec{B}_1 = (0, 0, 0) \quad \vec{B}_2 = \left(\frac{2}{3}, \frac{1}{3}, \frac{1}{2}\right)$$

# bcc

W Number 229

Na

K

V

Cr

Fe

Rb

Nb

Mo

Cs

Ba

Eu

Ta

Primitive Vectors:

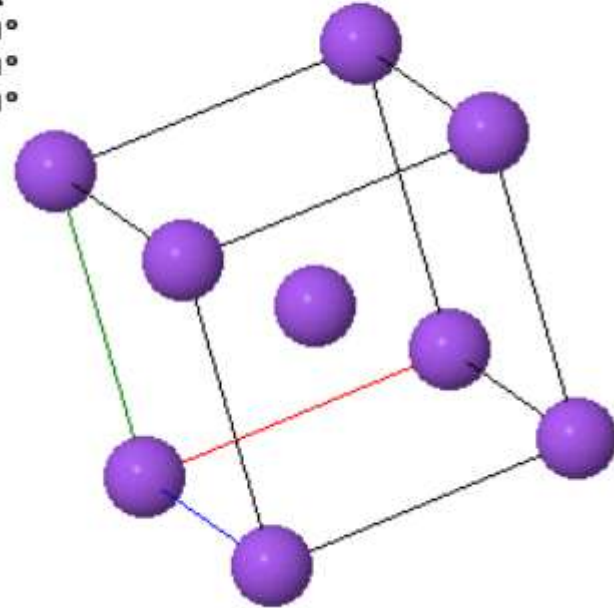
$$\vec{a}_1 = -\frac{a}{2}\hat{x} + \frac{a}{2}\hat{y} + \frac{a}{2}\hat{z}$$

$$\vec{a}_2 = \frac{a}{2}\hat{x} - \frac{a}{2}\hat{y} + \frac{a}{2}\hat{z}$$

$$\vec{a}_3 = \frac{a}{2}\hat{x} + \frac{a}{2}\hat{y} - \frac{a}{2}\hat{z}$$

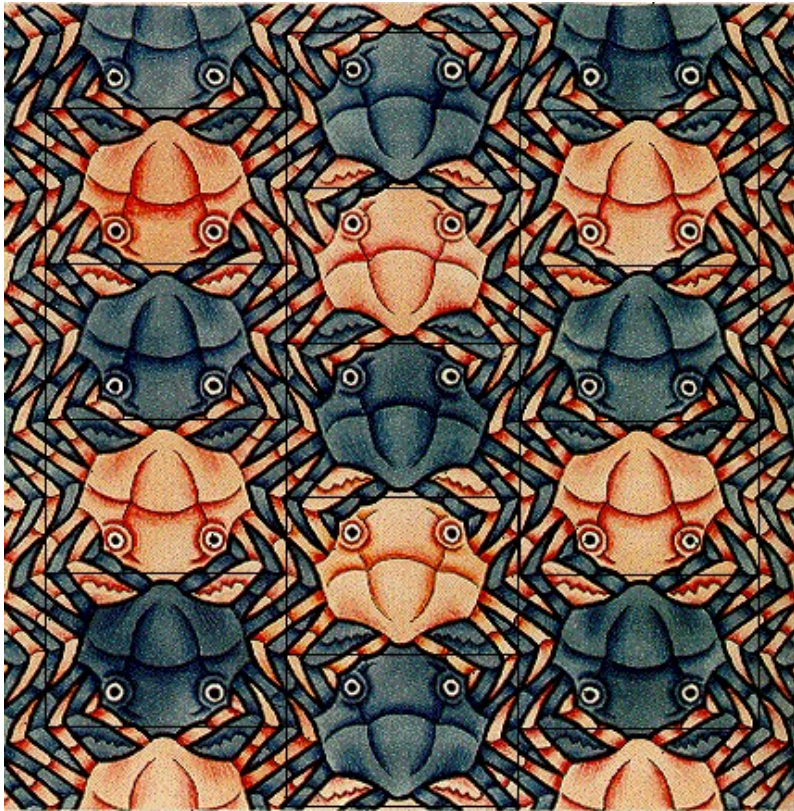
Basis Vector:  $\vec{B}_1 = (0, 0, 0)$

HM: IM-3M  
a=4.291Å  
b=4.291Å  
c=4.291Å  
α=90.000°  
β=90.000°  
γ=90.000°

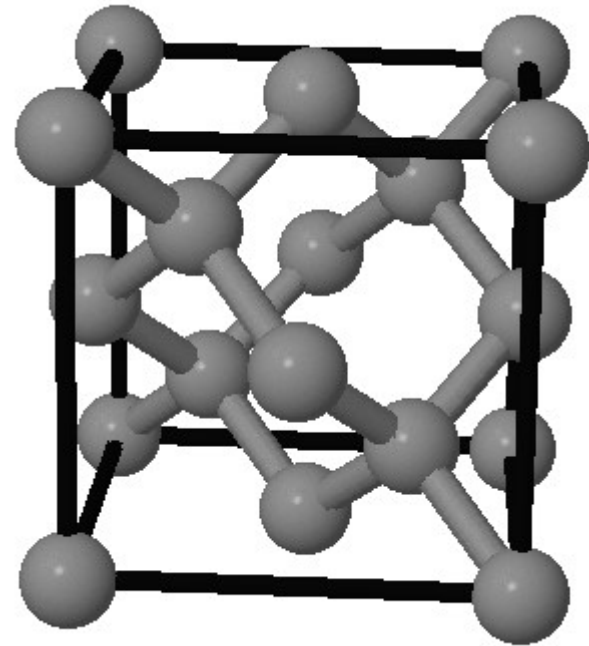


# Inequivalent atoms in the unit cell

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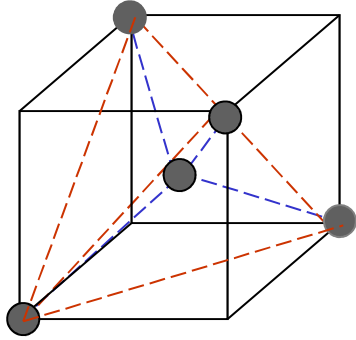


An element can have two distinct positions



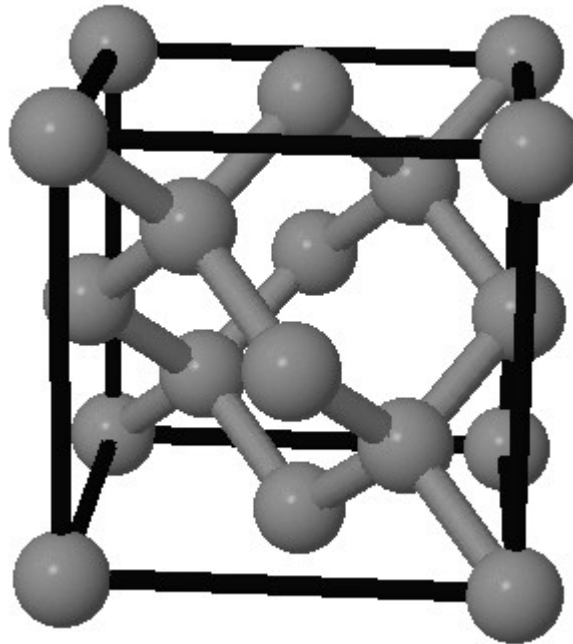
Diamond conventional unit cell

# Diamond



$$a = b = c, \quad \alpha = 90^\circ, \beta = 90^\circ, \gamma = 90^\circ$$

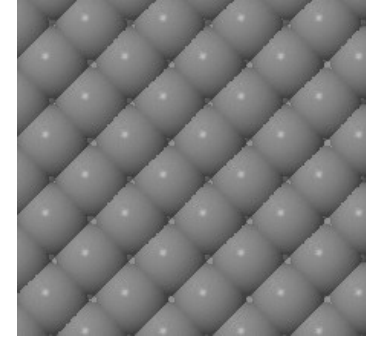
Space group: 227  
point group: m3m



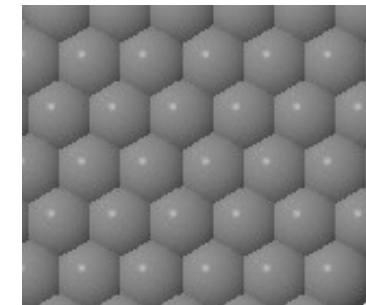
Primitive lattice vectors:

$$\vec{a}_1 = \frac{a}{2}\hat{x} + \frac{a}{2}\hat{y}, \quad \vec{a}_2 = \frac{a}{2}\hat{x} + \frac{a}{2}\hat{z}, \quad \vec{a}_3 = \frac{a}{2}\hat{y} + \frac{a}{2}\hat{z}.$$

Basis:  $\vec{B}_1 = (0, 0, 0), \quad \vec{B}_2 = (0.25, 0.25, 0.25).$



$$(100): \frac{2}{a^2}$$

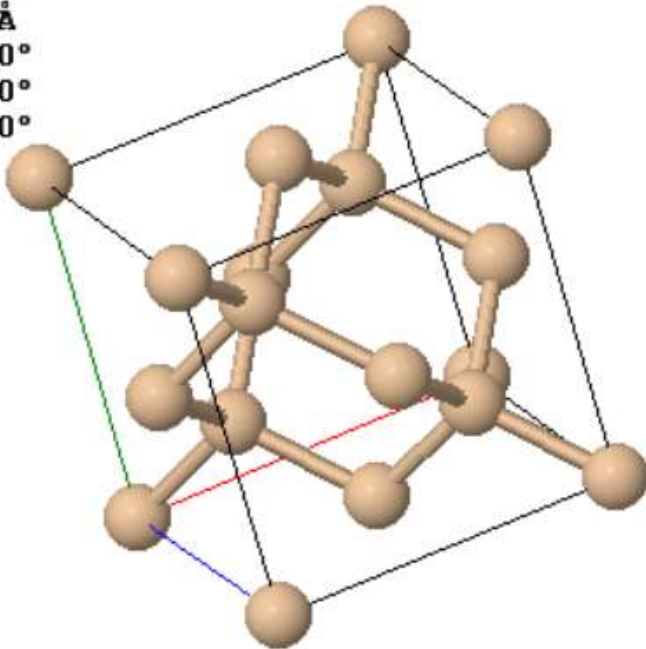


$$(111): \frac{4}{\sqrt{3}a^2}$$



# Silicon

HM:F d -3 m S  
a=5.430Å  
b=5.430Å  
c=5.430Å  
α=90.000°  
β=90.000°  
γ=90.000°



Conventional unit cell Primitive unit cell Asymmetric unit

2 x 2 x 2

3 x 3 x 3

5 x 5 x 5

Ball and Stick

Spacefill

H: 1

K: 0

L: 0

show HKL plane

hide HKL plane

draw atoms in HKL plane

Thickness of HKL planes:

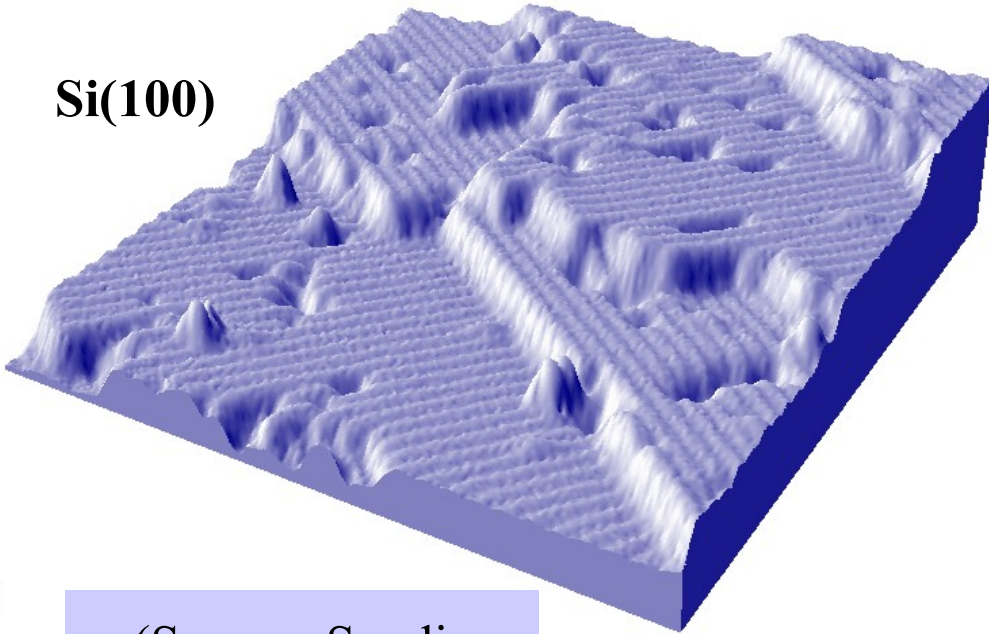


The conventional unit cell is a cube with sides of 0.543 nm. There are 8 atoms in the conventional unit cell. (The image can be rotated with a mouse.)

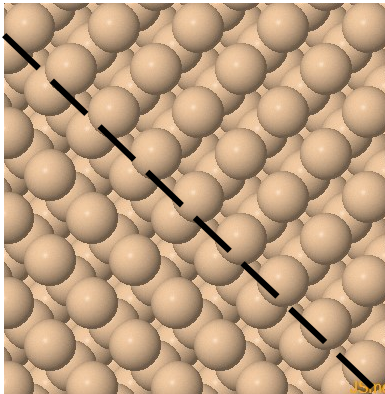
JSmol

# Silicon surfaces

Si(100)



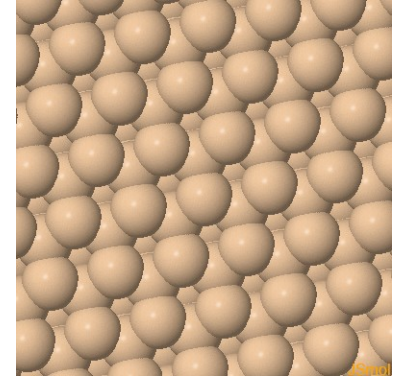
(Source: Sandia  
Nat.Labs.)



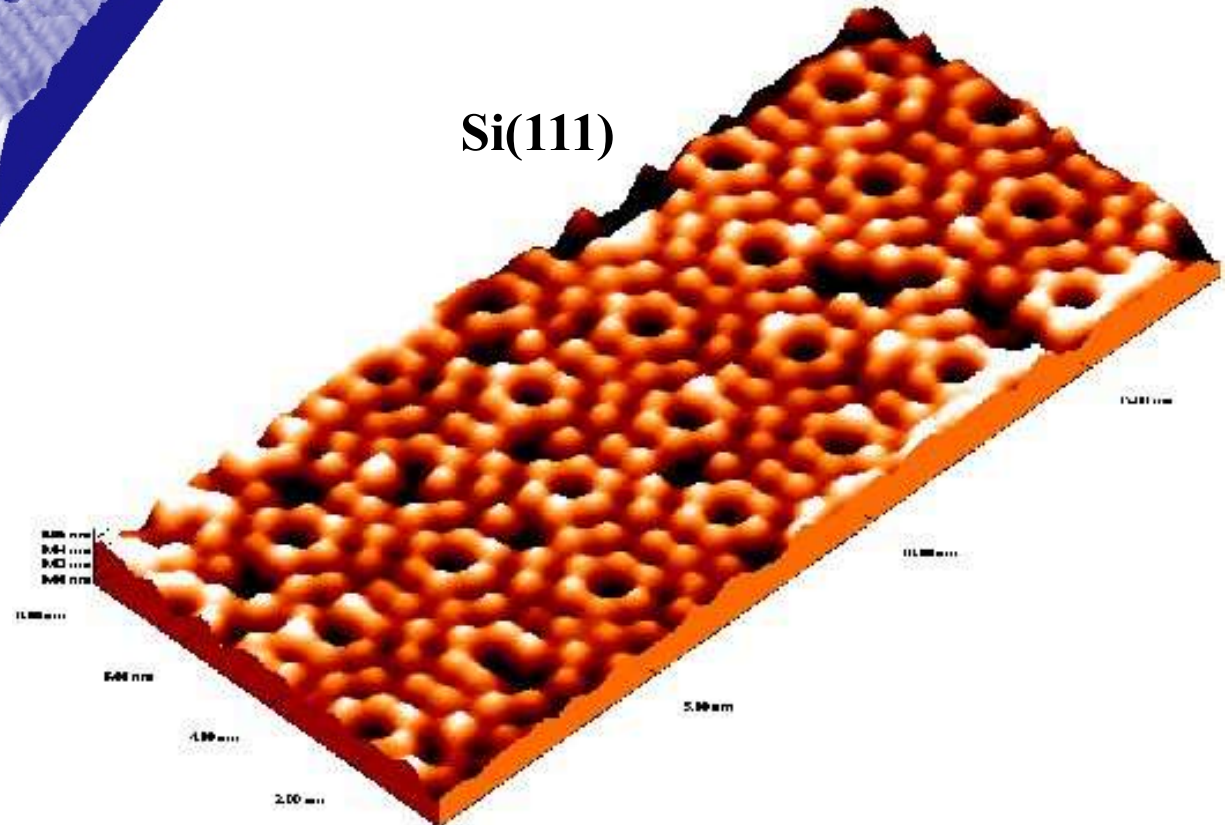
atomic  
step in  
Si(100)

unreconstructed

Si(111) →

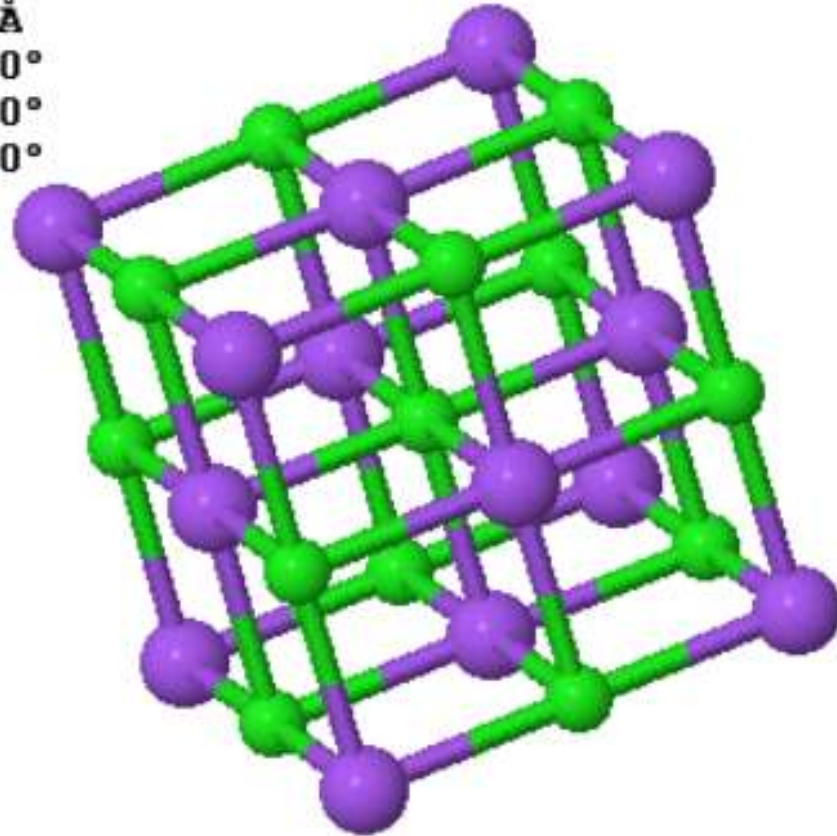


Si(111)



# NaCl

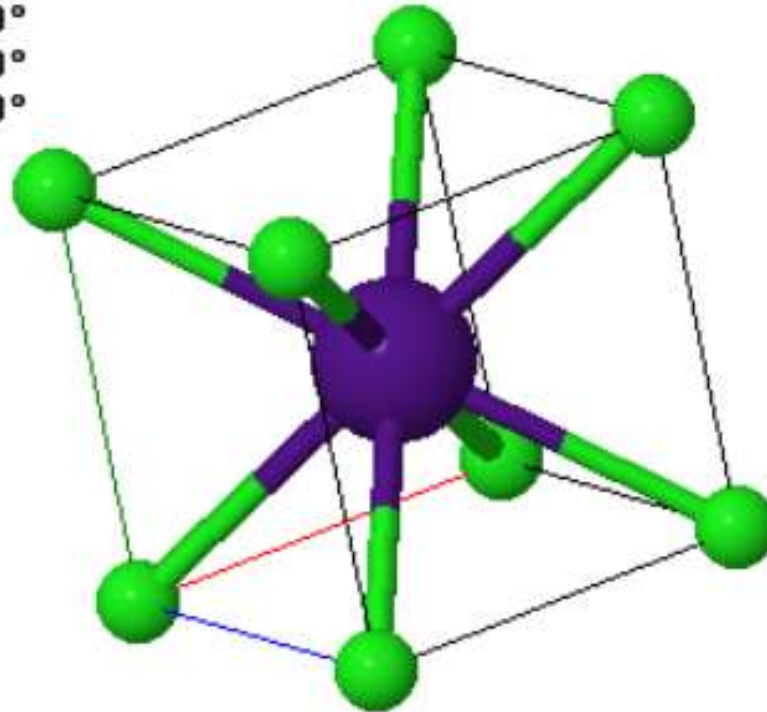
HM:  $Fm\bar{3}m$   
 $a=5.639\text{\AA}$   
 $b=5.639\text{\AA}$   
 $c=5.639\text{\AA}$   
 $\alpha=90.000^\circ$   
 $\beta=90.000^\circ$   
 $\gamma=90.000^\circ$



Number 225

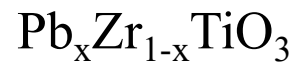
# CsCl

HM: PM-3M  
a=4.110Å  
b=4.110Å  
c=4.110Å  
 $\alpha=90.000^\circ$   
 $\beta=90.000^\circ$   
 $\gamma=90.000^\circ$

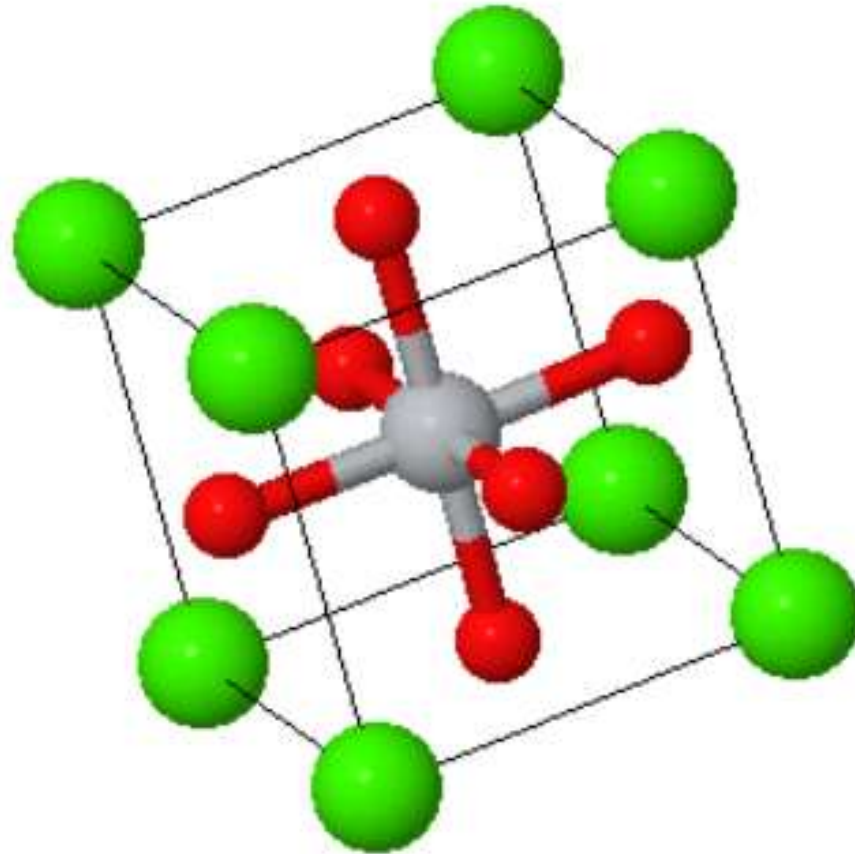


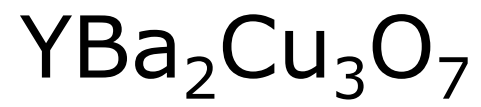
Number 221

# perovskite

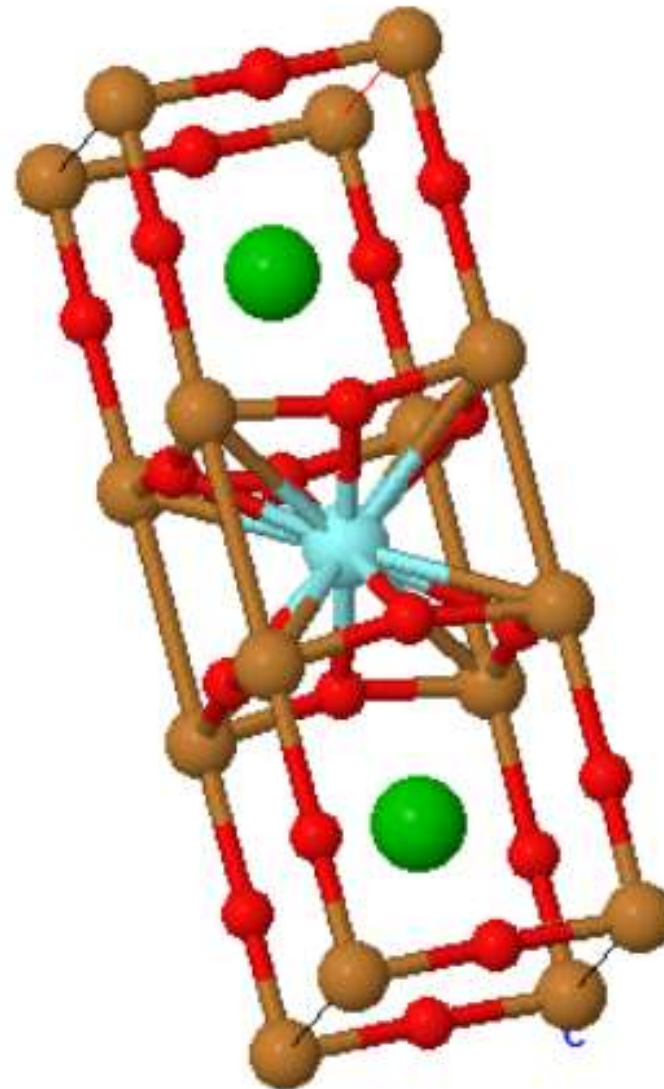


Number 221





HM: P m m m  
a=3.820Å  
b=3.885Å  
c=11.683Å  
α=90.000°  
β=90.000°  
γ=90.000°



Number 47

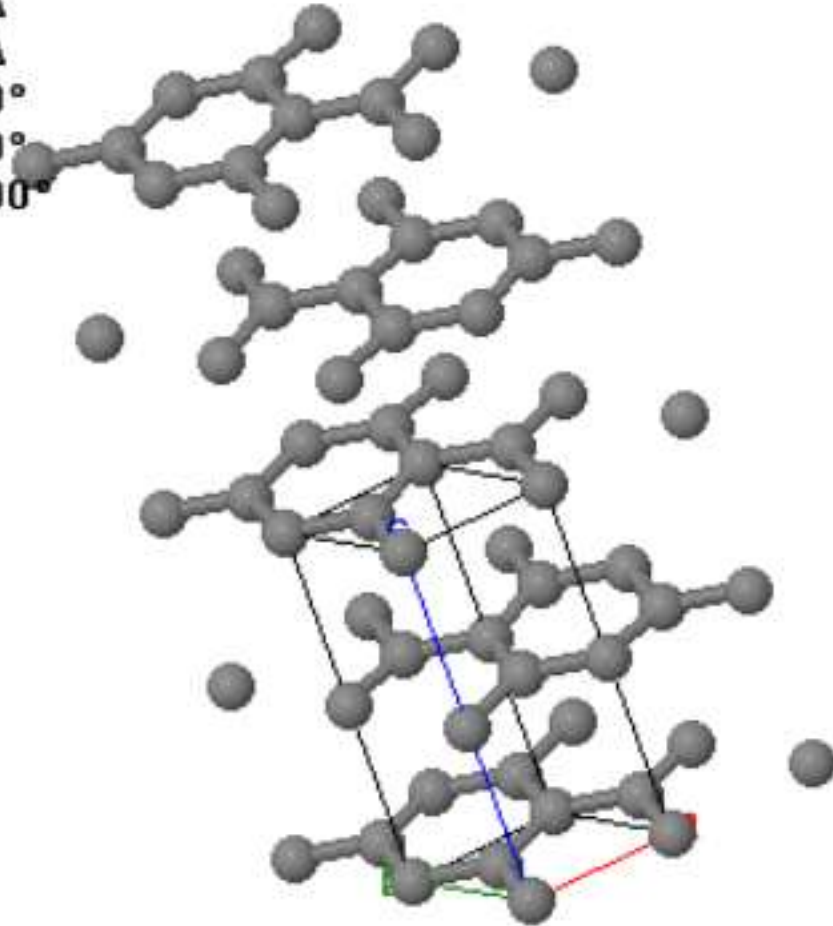
# graphite

Space group 194

4 inequivalent C  
atoms in the  
primitive unit cell

**Polytypes of carbon**  
graphite (hexagonal)  
graphene  
carbon nanotubes  
diamond  
rhombohedral graphite  
hexagonal diamond

HM: P 63 m c  
a=2.456Å  
b=2.456Å  
c=6.696Å  
α=90.000°  
β=90.000°  
γ=120.000°



# zincblende

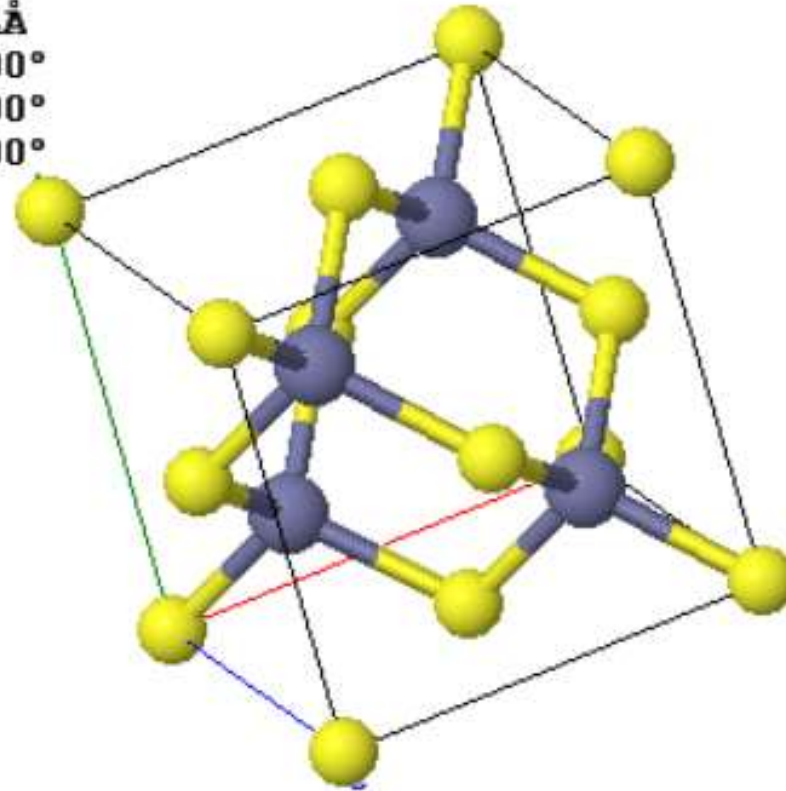
ZnS

GaAs

InP

HM:  $F\bar{4}3M$   
 $a=5.434\text{\AA}$   
 $b=5.434\text{\AA}$   
 $c=5.434\text{\AA}$   
 $\alpha=90.000^\circ$   
 $\beta=90.000^\circ$   
 $\gamma=90.000^\circ$

space group 216  
 $F\bar{4}3m$





# wurtzite

ZnS

ZnO

CdS

CdSe

GaN

AlN

HM:P 63 m c #186

$a=3.249\text{\AA}$

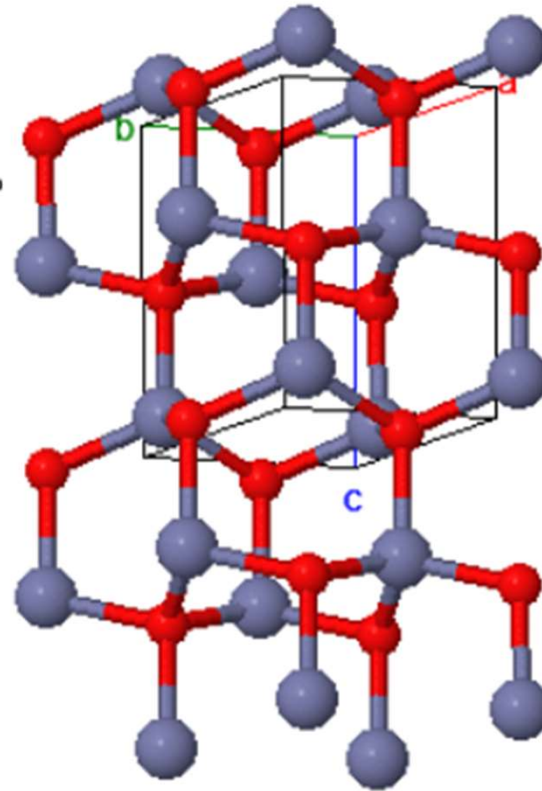
$b=3.249\text{\AA}$

$c=5.205\text{\AA}$

$\alpha=90.000^\circ$

$\beta=90.000^\circ$

$\gamma=120.000^\circ$

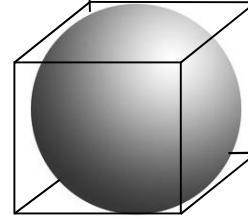
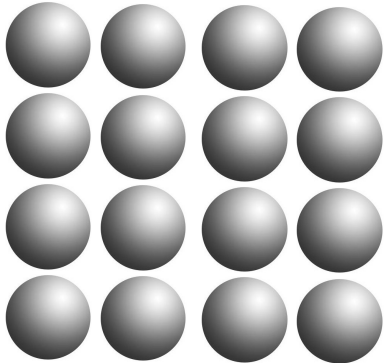


Number 186

There are 2 polytypes of ZnS: zincblende and wurtzite

# atomic packing density

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$$\frac{\frac{4}{3} \pi (L/2)^3}{L^3} = \frac{\pi}{6} \approx 0.52$$

fcc, hcp = 0.74

random close pack = 0.64

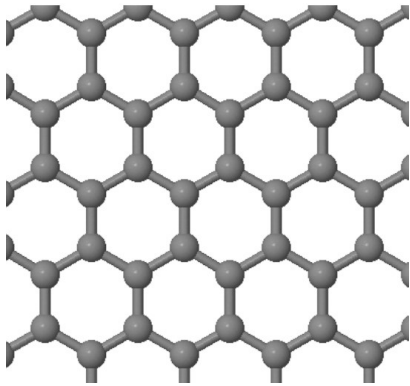
simple cubic = 0.52

diamond = 0.34

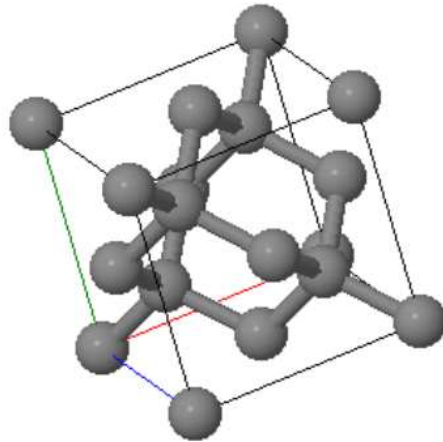
# Coordination number

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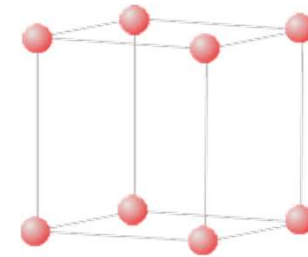
Number of nearest neighbors an atom has in a crystal



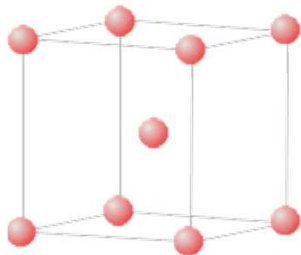
Graphene 3



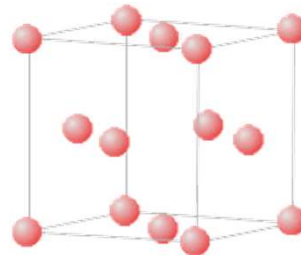
diamond 4



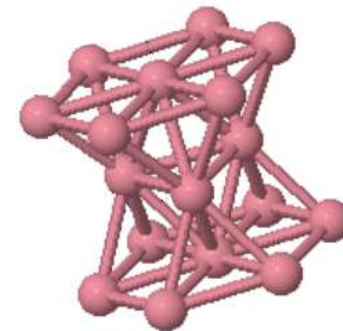
sc 6



bcc 8



fcc 12



hcp 12

## CIF files and programs to visualize crystal structures

Crystal structure data is often stored in a [CIF file](#). This is a text file that contains the asymmetric unit of the crystal, the symmetries of the space group, and a reference to the source where the data was first published. It is important to check the publication to see the conditions used during the experiment. Some experiments are performed at high temperatures or high pressures where the crystal structure can be different than at room temperature and ambient pressure. The links below will display a crystal structure and it's corresponding CIF file.

Simple Cubic, Polonium Po  $Pm\bar{3}m$  #221  
Face-centered Cubic (fcc)  $Fm\bar{3}m$  #225  
Body-centered Cubic (bcc)  $Im\bar{3}m$  #229  
Hexagonal, Boron nitride BN #194  
Hexagonal Close Packed (hcp)  $P63/mmc$  #194  
Perovskite, Calcium titanate  $CaTiO_3$  (perovskite)  $Pm\bar{3}m$  #221  
Caesium chloride  $CsCl$   $Pm\bar{3}m$  #221  
Rocksalt  $NaCl$   $Fm\bar{3}m$  #225  
Zincblende #216  
Wurtzite #186  
Diamond (C) #227  
 $\beta$ -Sn #141  
Graphite C  $P63mc$  #186

Sucrose P21 #4  
Magnetite  $Fe_3O_4$   $Fd3m$  #227  
Cementite  $Fe_3C$  #62  
Copper oxide CO (Tenorite) #15  
Pyrite  $FeS_2$  #205  
Rutile  $TiO_2$  #136  
Spinel  $MgAl_2O_4$  #227  
 $Sr_2FeMoO_6$  (double perovskite)  $I4/mmm$  #139  
 $YBa_2Cu_3O_7$  #47  
ZIF8 #1  
Zinc oxide ZnO (wurtzite)  $P63mc$  #186  
ZnS (wurtzite) #186

Prototypes

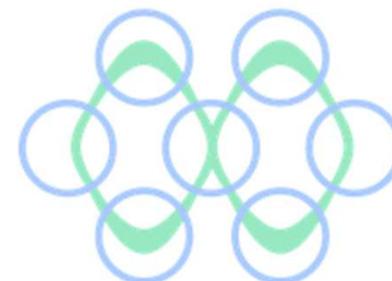
Periodic Table

Semiconductors

Ceramics



Inorganic Crystal Structure Database



Materials Project